Simulating the D/H ratio of water formed in the early solar nebula

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Our solar system originated from a protoplanetary disk about 4.6 billion years ago. We simulate the formation of this disk by a three-stage model of the solar nebula (SN) which describes the hydrodynamic and chemical evolution of a cold cloud core consisting of gas and one mass percent dust. Considering the first two stages of this SN-model we have studied the formation and deuteration of water, which is an important precondition of life.

During the quasi-stationary stage of the cloud core, corresponding to the first SN stage, water has been formed on the surface of dust grains by the hydrogenation of oxygen. The gas and dust temperatures, which differ at the outer boundary of the core, are nearly 14 K and reach 9 K in its center. Therefore an icy mantle forms on the dust grains in less than 10^5 years and changes slowly afterwards. Because of the large abundance of hydrogen and a carbon to oxygen (C/O) ratio of 0.44 the major component of this mantle is water ice. We found that the water produced in the gas phase amounts to less than 20 ppm of the water formed on dust grains. In both phases, the deuterium enrichment \( \delta D \) relative to the Standard Mean Ocean Water varies at 1 AU from 15,050 to 63,100\(^\text{‰} \) (or a D/H ratio from 2 to 0.5\%) and indicates the low formation temperature of water molecules.

In the second stage of our SN-model, the collapse of the cold cloud core is simulated using a semi-analytical solution of the magneto-hydrodynamic equations. Due to relatively high temperatures around the center (10^2–10^3 K), this range is identified with the hot corino observed in regions of low mass star formation in our galaxy. There, the icy mantles of the grains vanish due to desorption of water molecules from their surfaces. As a result the water to hydrogen ratio in the gas phase increases to \( 10^{-5}–10^{-4} \). Since this water was formed in a cold region and a collision related destruction of water molecules (occurring at \( \sim 10^5 \) K) can be neglected everywhere except for the protostellar source in the core center (<10^-2 AU), the deuterium enrichment in the outer hot corino (1 AU) reaches \( \delta D \) of 2,210\(^\text{‰} \) (or D/H of 0.1\%) at the end of the main collapse phase. Different reasons for this high value are discussed.

Keywords: collapsing core, solar nebula, dust chemistry, D/H ratio of water

INTRODUCTION

The formation of low-mass stars is observable in the large hydrogen clouds located in a region from nearly 50 pc above to 50 pc below the central plane of our galaxy. Surveys of these large dark or even giant molecular clouds show that they have an inhomogeneous structure of filaments which themselves consist of dense cores surrounded by diffuse inter-core matter (André, 2013). The main fraction of these cores form low-mass stars if one assumes that the mass distribution of new born stars is similar to the one of field stars and considering that nearly 99% of field stars have a stellar mass \( \leq 1.4 \, M_\odot \) (LeDrew, 2001; Lada, 2006), where \( M_\odot \) denotes the solar mass. Observations of the Chamaeleon molecular cloud give rise to the assumption that starless cores can be in a collapsing prestellar or in an unbounded stage while protostellar cores contain relatively hot hydrostatic gas-dust spheres—the precursors of T-Tauri stars—and outflows (Belloche et al., 2011a, b). After a time between \( 10^5 \) and \( 10^6 \) years the gaseous envelope disappears and a T-Tauri star surrounded by a turbulent disk becomes observable.

Our SN-model is based on these three stages of low-mass star formation (Fig. 1). Its early part simulates the starless stage as a quasi-stationary cloud core and the protostellar stage as a collapsing cloud core. The material in each stage consists of the gas phase with about 99% of the total core mass and the dust phase. Both phases interact with each other thermally and chemically. The energetic equilibrium of the first stage corresponds to a spherical core constructed by Bonnor (1956) and Ebert (1957). Since a number of these cores are characterized by oscillations (Keto et al., 2006), which are mathematically similar to stellar pulsations, relatively long lifetimes...
early protostellar core can heat up to 10^2–10^3 K and is of the gas and dust phase correlate while the temperature range and vary between 5 and 15 K. The density profiles region lower values than in the outer. The related variation et al.}, 2013) have in the inner region lower values than in the outer. The related variation range and vary between 5 and 15 K. The density profiles of the gas and dust phase correlate while the temperature profiles of both phases differ (Meng et al., 2013).

In contrast to the starless core, the inner region of the early protostellar core can heat up to 10^2–10^3 K and is called hot corino. In the center of this hot corino a nearly hydrostatic gas sphere forms as the precursor of the protosun. The complete gravitational collapse of the cloud core proceeds relatively fast in approximately 0.5 Myr (Williams and Cieza, 2011), whereby half of the mass is accreted in less than 10% of this time period. Since the cloud core rotates, in the course of the collapse a geometrically thick disk forms with an increasing radius influenced by the rotation rate of the core and the time dependent accretion rate (Stahler et al., 1994). At the end of the collapsing core stage only 0.1–10% of the total stellar mass is contained in this disk. Consequently, the mean accretion rate in our SN-model must be less than 10^{-6} M_\odot/year. However, observations (Baraffe et al., 2009) have shown that the accretion rate can reach values higher than 10^{-4} M_\odot/year for short periods. These episodic accretion events are discussed in more detail by Stamatekos et al. (2012). In general, gravitational collapse simulations are performed numerically (e.g., Krumholz et al., 2007; Commerçon et al., 2008; Saigo et al., 2008; Schönke and Tscharnuter, 2011) or assuming that a self-similar solution (Barenblatt and Zeldovich, 1972) may exist for a special range of the collapsing core (Shu, 1977; Whitworth and Summers, 1985; Boily and Lynden-Bell, 1995; Fatuzzo et al., 2004). During the collapse, the spherical envelope vanishes and the vertical extension of the disk shrinks clearly.

The last stage of our SN-model, called late solar nebula, is not part of the reported study. However, the calculated abundances at the end of the major collapse phase are used as initial chemical values for the disk phase (Fig. 1). The major collapse phase has produced a massive protostar in the center of the core. Thus, our disk stage can be described by a geometrically thin but optically thick axially symmetric structure with approximately Keplerian rotation of its material (Takeuchi and Lin, 2002, 2005; Takeuchi et al., 2005). Both components of this material, i.e., the gas and dust phase, are partly decoupled in their dynamic and thermal evolution. Since the protostar evolves to a young highly active star in 1–3 Myr, the gas component of the disk evaporates and it becomes an optically thin disk. The dust coagulates to pebbles, which finally grow to proto-planets (Jansson and Johansen, 2014) and by stochastic accretion (Morbidelli et al., 2012) to planets.

We assume, that the chemical and dynamical evolution of the solar nebula proceeds according to the scheme presented in Fig. 1. This scheme reflects primarily an isolated star formation observed in Bok globules (Stutz et al., 2010) contrasting to clustered star formation (Battersby et al., 2014). One perceives, that the physical and chemical initial conditions of the collapsing cloud core and the rotating disk are determined by the processes, which govern the evolution in the quasi-stationary and in the collapsing core, respectively. In the presented study, we describe the two modules derived for the first two stages of our SN-model. The physical differences between both cloud cores require the construction of two independent modules to simulate the dynamical evolution of each core. However, in contrast to physics, the chemical processes in all three stages can be described by a single module to solve the rate equations which provide the time and radial dependent abundances of the chemical species in the gas and dust phase. In addition to

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Fig. 1. Flow chart of the SN-model consisting of three stages (boxes with black boundary), where the first and second stages are combined to model the early SN (see introducing text). The third stage, constructed by a rotating geometrically thin disk, is considered as late SN. Online version of this paper contains color figures.
the solver of the rate equations, the module contains a database comprising parameters for about 7,000 reaction rates. Dust phase reactions, occurring on the surface of the dust grains, are important for the first stage of our SN-model (Hasegawa et al., 1992; Hasegawa and Herbst, 1993). Due to the cold surfaces the dust grains accrete an ice mantle composed of adsorbed species since a number of species can be formed on abundances on cold dust grains only (H2O, CO, CH3, NH2, etc.). The gas phase reactions and their related parameters for the reaction coefficients are taken from the OSU-astrophysical database (Smith et al., 2004). In addition one needs a number of parameters for dust reactions and for the transitions from gas to dust species and vice versa. These data, given by Semenov (2006) and Semenov and Wiebe (2011), are incorporated into the “ALCHEMIC” code, which was developed and tested by Semenov et al. (2010).

The observation of the starless dense cores, which can be hydrostatic or prestellar cloud cores, provides knowledge concerning the thermal and kinematic structure as well as the chemical properties of these objects (Crapsi et al., 2007; Maret et al., 2007). In a number of cases the indirect retrieval of radial gas flow signatures (asymmetry between blue- and redshifted wings in the spectral profile of optically thick emission lines such as HCO+), requires an advanced observation techniques (Schnee et al., 2013) combined with a lot of modelling effort (Keto et al., 2014) to derive the putative radial profiles of the state values (density, temperature, and velocity) for prestellar cores. Currently, gravitationally bound, starless cores are considered as static, oscillating, or contracting spherical objects. In order to derive chemical abundances from emission lines observed in starless cores, one needs to understand the formation of these lines which depends not only on the chemical composition of the gas inside the core but also on the validity of the chosen physical core model (Keto et al., 2014). Recently, the water abundance of the prestellar core L1544 was derived from the core model (Keto et al., 2014). The abundance of deuterated water lines towards the hot corinos IRAS2A and IRAS4A in NGC 1333 by Taquet et al. (2013) and the observation of the proto-binary IRAS 16293-2422 by Persson et al. (2013). They observed the deuterium content of water given by the abundance ratio of the deuterated to the non-deuterated molecules (δD = [D/H]/[H2O]) in % which is often higher than the corresponding deuterium content of the Earth ocean (156 ppm) defined by the Standard Mean Ocean Water (SMOW). Hereafter, the deviation of D/H ratio from the SMOW is given as ΔD(%) = (0.5 × ([HDO]/[H2O])/D/ DSMOW – 1) × 1000. The ratios published by Taquet et al. (2013) vary for IRAS2A between 0.3% (ΔD = 8,600‰) and 8% (ΔD = 255,000‰) and for IRAS4A between 0.7% (ΔD = 21,400‰) and 3% (ΔD = 95,200‰). The observations of Persson et al. (2013) have given about 0.09% (ΔD = 1,880‰) for a slightly better spatial resolution and a closer target. Using Herschel data Emprechtinger et al. (2012) have obtained an even smaller value of ~0.02% (ΔD = -333‰) for the hot core NGC 6334 I towards a high-mass star forming region. Coutens et al. (2013) have even detected double deuterated water molecules by employing Herschel data and observing the colder envelope and the hot corino region towards IRAS 16293-2422. They obtained an abundance ratio of D2O/H2O ~ 0.5%. However, this ratio can be derived only if one places an additional translucent cloud layer around the IRAS 16293-2422 source.

It is the goal of this study to simulate the relative abundances for H2O, HDO and D2O using the first two stages of our SN-model (Fig. 1). A number of approaches to...
model the chemical evolution of dark clouds, prestellar or protostellar cloud cores have been presented (e.g., Boland and de Jong, 1984; Ceccarelli et al., 1996; Bergin et al., 1997, 2006; Nejad and Wagenblast, 1999; Drouart et al., 1999; Rodgers and Charnley, 2003; Doty et al., 2004; Lee et al., 2004; Aikawa et al., 2005, 2008, 2012; Wakelam et al., 2006, 2014; Garrod and Herbst, 2006; van Weeren et al., 2009; Visser et al., 2009, 2011; Thi et al., 2010; Sipilä, 2012; Furuya et al., 2013; Yang et al., 2013; Garrod and Weaver, 2013; Pagani et al., 2013; Hincelin et al., 2013; Taquet et al., 2014; Vaytet et al., 2014). These models consider point, radially or axially symmetric core models combined with a more or less complex chemical database. With the models most comparable to our approach (Aikawa et al., 2008, 2012; Wakelam et al., 2014) we will later compare our results. Models which complement our study since they have tested the chemical evolution in the disk phase (Thi et al., 2010; Furuya et al., 2013) allow to estimate the evolutionary trend of the water deuteration in the late solar nebula while other models (Pagani et al., 2013; Taquet et al., 2014) report on a chemical network considering not only the deuterium chemistry but also the influence of the two spin-energetic states of the hydrogen molecule. The latter have identified an important source of reducing the deuteration of water, the ortho hydrogen molecules and their ions. Finally, Vaytet et al. (2014) has studied the energetic influence of the ortho hydrogen molecule on the equation of state of the gas-dust mixture and, thus, the interaction between the chemical and hydrodynamic evolution of the cloud core.

Our model uses a cold, radially symmetric core as initial state for the formation of our sun with a fixed but arbitrary life time between 1 and 6 Myr. In order to provide a relatively self-contained presentation of our SN-model, in the next section we expound briefly the main aspects of the evolving cloud core without going into too much mathematical detail. These details are explained in Tornow et al. (2014b). The third section presents and explains the simulated water abundances and deuterium fractionation. Finally, we discuss the results and give a short outlook concerning open problems.

**MODEL DESCRIPTION**

The quasi-stationary core

We assume that our Sun has formed as a relatively isolated star from a cloud core with a mass of about 1 M\(_\odot\) and isotropic boundary conditions. Our quasi-stationary core model can be understood as a gas-dust sphere with radially symmetric gas temperature and density profile. The dominance of the gas with respect to dust results from the canonical dust to gas mass ratio given by 0.01. Further, the core is assumed to be located in a region with a low ISRF, whose intensity scaling amounts to maximally 3 Habing (1 Habing = 1.2 \times 10^{-4} erg/cm^2/s/\mu). The sphere is partially shielded from this field by thin inter-core material (\(A_v = 2\)), which corresponds to a radially symmetric gas shell having a constant gas density. The radial profiles of gas mass, \(M\), gas density, \(\rho\), gas pressure, \(P\), and gas temperature, \(T\), are computed from the Poisson and the momentum conservation equations as well as from the ideal gas equation

\[
\frac{\partial M}{\partial r} = 4\pi r^2 \rho \tag{1}
\]

\[
\frac{\partial P}{\partial r} = -\rho \frac{GM}{r^2} \tag{2}
\]

\[
P = \frac{k_B}{m_p} \rho T = n k_B T \tag{3}
\]

with the gravitational constant, \(G\), the Boltzmann constant, \(k_B\), the gas particle mass, \(m_p\), and the radius, \(r \in [0, R_c]\). The boundary conditions follow from core mass \(M_0 = M(R_c)\), shell density \(\rho_0 = \text{const.} = \rho(R_c)\) and tempera-

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**Table 1. Heating and cooling processes in the gas and dust phase considered in Eqs. (4) and (5) (ro-vib.: rotation-vibration)**

<table>
<thead>
<tr>
<th>Cooling</th>
<th>Heating</th>
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</thead>
<tbody>
<tr>
<td>(\lambda_{\text{He}}): radiation of excited ro-vib. lines of CO, CS, HCN</td>
<td>(\Gamma_{\text{He}}): cosmic ray ionisation of H, H(_2), He</td>
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<tr>
<td>(\lambda_{\text{He}}): radiative excitation of CO, (C^+) and finally (H_2) (increasing temp.)</td>
<td>(f\lambda_{\text{He}}): hot (H_2) molecules formed in the dust phase</td>
</tr>
<tr>
<td>(\lambda_{\text{H}_2}): collision with dust grains</td>
<td>(\Gamma_{\text{H}_2}): far UV radiation causing (H_2) dissociation</td>
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<tr>
<td>(\lambda_{\text{H}_2}): recombination of hot (e^-) with positively charged grains</td>
<td>(\Gamma_{\text{H}_2}): hot (e^-) from photo-ionization of (C) or dust</td>
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<table>
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<tr>
<th>Cooling</th>
<th>Heating</th>
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<tr>
<td>(\lambda_{\text{IR}}): infrared radiation of dust grains</td>
<td>(\Gamma_{\text{IR}}): absorption of UV radiation</td>
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ture $T_0 = T_c$. Since the gas of the central core is nearly molecular, the averaged mass of one gas particle can be written as $m_p = \mu_p m_H$, with the mass of a hydrogen atom $m_H$, $\mu_p = 2.34$ and the particle number density is given by $n = \rho/m_p$. A mass factor $\mu_p$ of 2.34 arises, since in addition to hydrogen molecules, the gas consists of a small mass fraction of helium and traces of so called metals (e.g., oxygen, carbon, iron). Two further equations are needed to determine the profiles of gas and dust temperature. They follow from the thermal balance between the cooling and heating processes which couple both phases to each other. Thus, we obtain for the gas phase

$$\Gamma_g - \Lambda_{\text{gas}} + \Gamma_{\text{photo}} - \Lambda_{\text{photo}} + f_I \Gamma_{\text{H}_2} - \mathcal{R}_\text{coll}(T - T_g) = 0 \quad (4)$$

and equivalently for the dust phase

$$\Gamma_{\text{dust}} + (1 - f_I)\Gamma_{\text{H}_2} - \Lambda_{\text{dust}} + \mathcal{R}_\text{coll}(T - T_d) = 0 \quad (5)$$

with the dust temperature, $T_d$. Equations (4) and (5) depend also on the dust density, $\rho_d$, and are valid at each radial grid point of the core and the shell. The meaning of the various parameters in the balance equations, explained in Table 1, are explicitly given in Tornow et al. (2014a).

To calculate the difference $\Gamma_{\text{dust}} - \Lambda_{\text{dust}}$ in Eq. (5), we employ the dust size distribution of Mathis et al. (1977) and the method of Zucconi et al. (2001) to solve the radiative transfer equation. Other size distributions (e.g., Zubko et al., 2004) cause deviations of <3% along the profile of the relative water abundance calculated from our SN-model (Tornow et al., 2014a). Since the coagulation of dust grains is less important for the early solar nebula, the chosen size distribution can be kept constant. However, the dust to gas mass ratio changes due to the motion of grains, which is caused by the radiation pressure of the surrounding ISRF. The grain velocity, $v_{d, \pi}$, depending on the grain size $a$, results from the conservation equation of the dust momentum (Whitworth and Bate, 2002). In order to save the computation power, we consider the mean grain size, $a$, averaged for the chosen size distribution. Since the velocity, $v_{d, \pi}$ is small, the momentum conservation can be written as a simple force balance

$$m_{d, \pi} r_{d, \pi}(t) = P_{\text{ISRF}}(\rho_d, \rho_{d, \pi}) - \pi a^2 \psi(\rho_d, \rho_{d, \pi}) P_{\text{ISRF}}$$

with $r_{d, \pi}(0) = r_{d, \pi}(t) = 0 \quad (6a)$

where $m_{d, \pi}$ is the dust mass of a single grain, $\rho_{d, \pi}$ is the dust density, $D_{\pi}$ is the deceleration of the grains because of the gas drag, $\psi$ is the attenuation of the radiation field, $P_{\text{ISRF}}$ is its radiation pressure, and $r_{d, \pi}(t)$ is the time dependent shift of the grain according to its initial position. Knowing the grain velocity, $v_{d, \pi} = r_{d, \pi}(t)$ one can find the dust density, $\rho_{d, \pi}$, by solving the continuity equation

$$\frac{\partial M_{d, \pi}}{\partial t} = -4\pi r^2 \rho_{d, \pi} v_{d, \pi} \quad \text{with} \quad \frac{\partial M_{d, \pi}}{\partial t} = 4\pi r^2 \rho_{d, \pi} \quad (6b)$$

One can assume, that the grain velocity and density change
only slowly with time. In order to solve Eqs. (1) to (6) we used an iterative method (Kupper, 2014), in which one inserts $\rho_{\partial, \pi}$ into Eqs. (4), (5), and (6a).

The temperature profiles of the gas and dust as well as the gas density profile are derived considering (1), (2) and (3). These data are then used to find the new profile of the dust density from Eq. (6b) and the next iteration step follows. The complete iteration procedure converges very fast to stable solutions. In Fig. 2a, the final results of these profiles are presented. The density profile corresponds to the Bonnor-Ebert sphere (BES) described by Bonnor (1956) and Ebert (1957). This sphere has a clearly defined radius, a final mass, and a regular density solution.

Due to Eqs. (4) and (5) one obtains different radial profiles for the temperature of the gas and dust phase (see Fig. 2), where the first profile varies between 9 and 13.7 K and the latter varies between 8.5 and nearly 15 K. Compared to the results published by Bergin et al. (2006) for the B 68 core the dust temperature is 1–2 K lower, but they have considered a lower far UV radiation intensity (0.2 Habing).

Figure 2b shows the initial and final profiles of the radial profile of the relative water abundance. In addition to the intensity of the ISRF, the rates of the photo-reactions depend also on the visual extinction $A_V$. Even if the difference between both profiles is fairly small ($\Delta A_V \sim 0.42$), the chemical abundance of H$_2$O or other molecules is also influenced.

The collapsing cloud core

In order to obtain a collapse model for the core with an arbitrarily high spatial resolution the magnetohydrodynamic (MHD) equations of a partially ionized gas are solved with a semi-analytical approach. The related MHD equations are the Poisson, continuity, momentum, and induction equation with the following expressions:

$$\frac{\partial \rho}{\partial t} + \frac{\rho u}{r} + \frac{\partial}{\partial r} \left( r u \right) = 0$$

$$\frac{\partial M}{\partial r} = 4\pi r^2 \rho \left( \frac{GM}{r^2} \right)$$

$$\frac{\partial M}{\partial t} = -4\pi r^2 \rho u + \frac{\partial}{\partial r} \left( r^2 \rho u \right) = 0$$

Due to the radial symmetry the radius, $r \in [0, R_C]$ and the time, $t \in [0, T]$ are the independent variables and $u$ and $b$ denote the gas velocity and the toroidal magnetic field of the collapsing core. $R_C$ and $T$ symbolize the size of the core and the collapse duration, respectively. A fitting relation which expresses the resistivity, $\eta$ as function of the gas temperature and the ionisation degree of the gas (actually one has to call it plasma) can be find in Machida et al. (2007) or in appendix of Tornow et al. (2014b). The gas to dust mass ratio, kept fixed during the collapse, corresponds to the one of a 6 Myr old quasi-stationary core (Fig. 2). Further, we used the equation of state (EOS) given by

$$P = \frac{\gamma}{\gamma - 1} \left( \frac{\rho}{\rho_s} \right)^{(\gamma - 1)/\gamma}$$

The parameters $K_p$ and $s$ depend on the time and $s$ corresponds to the ratio of the specific heat coefficients. Consequently, the conservation of energy

$$\frac{\partial}{\partial r} \left[ r^2 \frac{\partial u}{\partial r} \right] + \frac{1}{r} \frac{\partial}{\partial r} \left( r^2 \frac{\partial T}{\partial r} \right) + 4\pi r^2 \rho \left( \frac{\partial u}{\partial r} \right) = 0$$

$$\frac{\partial}{\partial t} \left[ r^2 \frac{\partial u}{\partial r} \right] + \frac{1}{r} \frac{\partial}{\partial r} \left( r^2 \frac{\partial T}{\partial r} \right) = 0$$

must be fulfilled. The total heat rate $w_H$ consists of Julian and frictional heat rates, the heat transport in the core according to heat conductivity $\kappa(\rho, T)$ and the sum $Q = \Gamma - \Lambda$ of energy loss and gain per unit time. Since the rota-
The D/H ratio of water is 533.

The viscosity parameter \( \tau_{VC} \) is chosen:

\[
\tau_{VC} = k_{\tau} \tau_c s_R C \quad \text{(Regev and Shaviv, 1981)}.
\]

The tuning value, \( k_{\tau} \), depending on Reynolds number, \( Re \), and sound speed, \( c_s \), is given by

\[
k_{\tau} = \left( \frac{\rho \omega}{\mu p \rho} \right) \leq \left( \frac{1}{13} \right) \leq \left( \frac{\rho \omega}{\mu p \rho} \right).
\]

Note, that the ratio \( \left( k_{\tau} T \right) / \left( \mu p \rho \right) \) gives the quadratic sound speed. Now, the following analytical expression for the gas density \( \rho \) is introduced into the MHD equations (7) and (8)

\[
\rho(r, t) = \begin{cases} 
\rho_1(r, t) & \text{if } 0 \leq r < \rho_0(t \leq T) \\
\rho_2(r, t) & \text{if } \rho_0(t \leq T) \leq r < \rho_1(t \leq T) \\
\rho_3(r, t) & \text{if } \rho_1(t \leq T) \leq r < \rho_2(t \leq T) \\
\rho_4(r, t) & \text{if } \rho_2(t \leq T) \leq r < R_C 
\end{cases}
\]

where the densities in the radial intervals are given in Table 2. The average velocity, \( \langle u \rangle \) in Eq. (13) is computed for each of these radial intervals and the unknown coefficients \( a_i, \rho_0, \gamma_i, X_i \), and \( \rho_0 \) correspond to 14 time-dependent functions. The resulting complete solution of the MHD equations is explained in Tornow et al. (2014b).

In this study the chemical processes are the main topic, but the consequential distributions of the state variables for our collapsing core model will be shown to simplify the understanding of the obtained results from the chemical simulations. According to Ceccarelli (2004), a hot corino is a region located close to the center of the collapsing cloud core, clearly smaller than 150 AU in a low-mass star forming target.

It seems necessary to note, that a determination of the outer boundary of the hot corino from observations is hard to achieve (Maret et al., 2004; Jørgensen and van Dishoeck, 2010). In particular the source IRAS16293-2422 identified as binary proto-stars has a large hot corino range \( R_{100K} = 133 \) AU (with \( R_{100K} \) outer boundary with \( T = 100 \) K). In contrast to the binary source, there is the “lukewarm hot corino” L1527 (IRAS 04368+2557) which has a much smaller value for \( R_{100K} = 20 \) AU (Hassel et al., 2008). However, according to Tobin et al. (2013), this object has a turbulent disk with a radius of 125 AU related to our optically thick disk stage (Fig. 1).

Figures 3, 4, and 5 illustrate the evolution of the gas temperature, density, and velocity on an Eulerian grid. One recognizes in Fig. 3, that the distribution of the temperature corresponds to an isothermal process in a large temporal and radial range. Accordingly, we call our model...
a cold collapse. The formation of the hot corino starts at ~0.13 Myr with $s = 4/3$ (see Eq. (11)). The temperatures are at least high enough to allow water desorption from the dust phase. The hot corino becomes a shell as soon as its central temperature is high enough to form a collisional hydrogen dissociation front ($T \sim 2,000$ K). Behind this front a hydrostatic source evolves by accreting matter from outwards. Its temperature increases slowly (due to a proceeding $H_2$ dissociation which requires 4.48 eV per molecule while the mean available thermal energy in the hot corino is only ~0.74 eV, Stahler and Pallas, 2004) and rises afterwards if all species are atomic. Hydrogen ionization starts and the protostellar source forms.

In Fig. 4 the iso-line $\rho_{\text{inn}} = 1\, \text{kg/m}^3$ (nearly air density) indicates the inner boundary of the hot corino while the outer boundary is located between the iso-lines $\rho_{\text{inn}} = 10^{-6}\, \text{kg/m}^3$ and $\rho_{\text{inn}} = 10^{-12}\, \text{kg/m}^3$ (Masunaga et al., 1998; Masunaga and Inutsuka, 2000). Compared with Fig. 3, the related temperatures at the iso-lines suggests that a typical adiabatic relation as given by Saigo et al. (2008) would produce a nearly ten-fold higher temperature in this range, i.e., our approach of a multi-zone density (see previous section), can be written as

$$\frac{\partial T}{\partial t} + \frac{u}{\rho} \frac{\partial T}{\partial x} = -\Lambda_k - \Gamma_k$$

(15)

where the symbols $\Gamma_k$ and $\Lambda_k$ contain all the formation and destruction processes for species $k$, respectively. Since the number of chemical species is very large, one should avoid solving thousands of coupled partial differential equations by simulating the chemical evolution of all species in the Lagrange frame (Lufkin and Hawley, 1993).

### Table 5. Initial abundances for the species (X) relative to the molecular and atomic hydrogen abundance given as 12 + log(x) with $x = X/(H + 2H_2)$ for the quasi-stationary cloud core (Wakelam et al., 2006; Kupper, 2014) and solar photosphere (Lodders et al., 2009).

<table>
<thead>
<tr>
<th>Species X</th>
<th>Cloud core</th>
<th>Solar photosphere</th>
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<tbody>
<tr>
<td>H$_2$</td>
<td>11.70</td>
<td>—</td>
</tr>
<tr>
<td>He</td>
<td>10.99</td>
<td>10.925</td>
</tr>
<tr>
<td>H</td>
<td>9.30</td>
<td>—</td>
</tr>
<tr>
<td>O</td>
<td>8.26</td>
<td>8.73</td>
</tr>
<tr>
<td>C$^+$</td>
<td>7.90</td>
<td>8.39</td>
</tr>
<tr>
<td>N</td>
<td>7.39</td>
<td>7.86</td>
</tr>
<tr>
<td>HD</td>
<td>7.18</td>
<td>—</td>
</tr>
<tr>
<td>S$^+$</td>
<td>4.96</td>
<td>7.14</td>
</tr>
<tr>
<td>Fe$^+$</td>
<td>3.44</td>
<td>7.45</td>
</tr>
<tr>
<td>Si$^+$</td>
<td>3.99</td>
<td>7.52</td>
</tr>
</tbody>
</table>

The chemical model of the gas and dust phase

**General aspects** The gas phase of our chemical model is based on the Nahoon model of Wakelam et al. (2006), while the dust phase reactions are taken from the Heidelberger “ALCHEMIC” code developed by Semenov and Wiebe (2011). In both stages of our SN-model all chemical abundances have been simulated with rate equations (Herbst and Klemperer, 1973; Prasad and Huntress, 1980; Langer and Graedel, 1989; Lee et al., 1996; Aikawa et al., 2008). If $k$ denotes the species number with $N = \max(k)$, the relative abundances are defined by

$$x_k = \frac{\rho_k}{\rho} = \frac{n_k}{n}$$

with $\rho = \sum_{i=1}^{N} \rho_i$ where the latter equality follows because of the introduction of an averaged particle mass $m_p$. For some $k_0$, one has $x_{k_0} = x_{H_2O}$ and $n_{H_2O} = n_{H_2O} = H_2O$ if one assumes that $\rho = \rho_0 + 2\rho_{H_2O}$, i.e., if one adds molecular and atomic hydrogen together, they are the dominant species. This is true for all non-ionized interstellar clouds keeping in mind that the second most frequent element in the universe, He, is chemically inert and considered by its mass only.

All species in the medium have the same streaming velocity which is set to $u = 0$ for the quasi-stationary core and $u = v_r$ (Fig. 5) for the radial inflow velocity of the collapsing core. Thus, the rate equations, corresponding to $N$ continuity equations (second form of Eq. (16) in the previous section), can be written as
which can be seen as a large bundle of paths oriented from the outer core boundary to the center. Then, the chemical evolution of an arbitrary gas pocket can be calculated along this path leading to a simplified version of Eq. (15). If we split the set \( \{x_k\}_{k=1}^N \) into two subsets, one for the dust phase and one for the gas phase: \( x_k \rightarrow (x_p, x_q^*) \), one obtains the two sets of differential equations

\[
\frac{dx_p}{dt} = \dot{\Gamma}_p - \hat{\Lambda}_p, \quad \frac{dx_q^*}{dt} = \dot{\Gamma}_q^* - \hat{\Lambda}_q^* \quad \text{with} \quad p = 1, N_p, \quad q = 1, N_q
\]

with the condition \( N_p + N_q = N \). Other conditions are of course mass and charge conservation. Both systems differ chemically but they are coupled to each other since the formation and destruction functions \( \dot{\Gamma}_p, \hat{\Lambda}_p, \dot{\Gamma}_q^*, \hat{\Lambda}_q^* \) depend on the relative abundances \( (x_p, x_q^*) \) and lead to an interaction between both phases. Numerically, both sets of the differential equation (16) are solved simultaneously and treated as one.

The initial abundances needed to solve the differential equation are given in Table 3. We use the KIDA database (http://kida.obs.u-bordeaux1.fr/models/kida.uva.2011.zip) which is related to the former OSU (Ohio State University) database, in order to simulate the reactions of 474 gas species and compute their corresponding coefficients (Wakelam et al., 2006, 2010, 2012) as well as to simulate the hot core or hot corino chemistry (http://kida.obs.u-bordeaux1.fr/models/osu_HighT.zip). The data to calculate dust surface reactions, which are desorption energies from these surfaces and the energetic potential barriers between grain sites (to compute the hopping or tunneling rates) on these surfaces, can be taken from the ALCHEMIC database of Semenov (2006) and Semenov et al. (2010) for about 200 dust species. A parser program was developed, which reads the described databases and constructs the temperature related system of coupled differential see above (16). In order to calculate the chemical abundances, we employed the DLSODES solver of the odepack (http://www.netlib.org/odepack/) (Brown and Hindmarsh, 1989), which iteratively solves the differential system for the species of the gas and dust phase simultaneously. Now the chemical reactions for all elements in Table 3 except for HD can be considered.

Further technical details concerning the simulation of the chemical reactions are discussed in Semenov (2006) and Kupper (2014). Especially the calculation of the formation and destruction function for the chemical species \((x_p, x_q^*)\) is explained there. Of course, our chemical simulation depends on the initial chemical conditions for the quasi-stationary core which are given in Table 3 while the chemical abundances obtained from this core after 6 Myr of evolution are the chemical input data of our collapsing core (see Fig. 1). Comparing the initial element abundances of the cloud core with the abundances of the solar photosphere given by Lodders et al. (2009), one recognizes that the gas in the cloud core is depleted of heavy elements, such as Si, Mg, Na, and Fe but also lighter ones such as C, O, and S. Both groups are refractory solid forming elements that produce for instance mineral or carbon clusters and are incorporated into dust grains. The temperature of the solar nebula (Fig. 3) is higher than the condensation temperatures of many minerals near the protostar (\( T > 1680 \) K, Lodders, 2003) and the grains vaporize quickly and transit from the solid to the gas phase. The C/O ratio, influencing the mineral building chemistry as well as the composition of ice mantles formed on dust grains, is 0.44 for the core and 0.46 for the solar photosphere, telling that our core model is slightly richer in oxygen compared to carbon.

The initial abundance distribution in Table 3 considers \( H_2 \), but neglects that the nuclear spin of the molecule gives rise to emergence of two isomers, denoted as ortho- and para-\( H_2 \). In general one considers a mixture of ortho- and para-\( H_2 \) whereby the ortho-isomer corresponds to a triplet quantum state with proton spins aligned parallel and the para-isomer is related to a singlet quantum state with proton spins aligned anti-parallel. In local thermal equilibrium the ortho-to-para ratio (OPR) for \( H_2 \) is calculated from the quotient of the corresponding rotational partition functions Gavilan et al. (2012). The equilibrium values for \( H_2 \), at 10 K is given by OPR_{\text{eq}} = 4 \times 10^{-7}. However, the indirect measurements of this ratio reported in the literature for cold cloud cores differ clearly from OPR_{\text{eq}}. According to Pagani et al. (2013) and Troscomp et al. (2009), it follows: 0.1 < OPR < 1. The OPRs derived from \( H_2O \) observations in the coma of comets are even larger and vary mainly between 2.5 and 3 (Dello Russo et al., 2005; Bonev et al., 2007, 2013). In addition, there are experiments investigating the OPR resulting from hydrogen molecules formed on porous amorphous water ice (Gavilan et al., 2012). The measurements provide an OPR of 2.91 with a large uncertainty. Overall, these data suggest a relatively high abundance of ortho-\( H_2 \) (compared to the equilibrium abundance) in the gas and dust (ice) phase of cold cores. However, since our chemical network is very complex and, in the collapsing core stage, the density and temperature gradients are very large, we have to perform an appropriate decrease of the number of species before adding ortho-H\(_2\) to it. If the simplified network provides nearly the same results as those obtained in the presented study we have a network designed for water. Perhaps, a similar procedure can be done for other species or a small set of them. However, at the end of the next section we will come back again to the influence of a relatively large OPR.
Aspects of \( \text{H}_2\text{O}, \text{HDO} \) and \( \text{D}_2\text{O} \) formation. In addition to the water abundance the deuterium to hydrogen ratio (D/H) is an interesting parameter which contains information on the thermal conditions of the gas-dust material in which the water has been formed (Cazaux et al., 2011). Since it is the goal of this study to determine the evolution of the water abundance and the D/H of water in the gas and dust phase during the early stages of the solar nebula, we will explain the formation of water in more detail. First, the system of differential equations needs to be extended by including all the deuterium bearing species. To achieve this purpose, we applied the method proposed by Albertsson et al. (2013) but also used the published reactions (Brown and Rice, 1986a, b; Flower et al., 2004; Hiraoka et al., 2005; Howe and Millar, 1993; Howe et al., 1994; Millar et al., 1989; Osamura et al., 2005; Roueff et al., 2007; Tielens, 1983; Walmsley et al., 2004; Willacy, 2007). This way, the species number increases to about 1,900 and the number of reactions increase to about 17,330 for both phases. The energy barrier of thermal surface desorption differs with mass (Kristensen et al., 2004; Willacy, 2007). This way, the species number increases to about 1,900 and the number of reactions increase to about 17,330 for both phases. The energy barrier of thermal surface desorption differs with mass (Kristensen et al., 2011). We have chosen a factor of 1, 1.003 and 1.039 based on the mass of \( \text{H}_2\), HD, and \( \text{D}_2 \) (Kupper, 2014).

\( \text{H}_2\text{O} \) is formed in the gas phase by hot neutral reactions (Charnley, 1997), which become possible because of the increasing temperature due to the gravitational compression of the core. Typical reactions are

\[
\begin{align*}
\text{H}_2 &+ \text{O} \rightarrow \text{HD} + \text{O} \\
\text{HD} + \text{O} &\rightarrow \text{D} + \text{O}_2 \\
\text{H}_2 + \text{OD} &\rightarrow \text{D}_2 + \text{O} \\
\text{D}_2 + \text{O} &\rightarrow \text{O}_2 + \text{D} \\
\end{align*}
\]

The neutral reactions require at least temperatures between 160–230 K to proceed efficiently and surmount the activation energy barrier (Ceccarelli et al., 1996; Charnley, 1997). In the cold cloud core, i.e., for temperatures lower than 20 K, large abundances of H, D, O, OH, and OD species are adsorbed on the surface of dust grains and, due to the high mobility of H and D on these surfaces (Matar et al., 2008), \( \text{H}_2\text{O}, \text{HDO} \), and \( \text{D}_2\text{O} \) are produced by surface reactions (Dalieu et al., 2010). In particular, a few of them (last two columns below) are emphasized theoretically by Tielens (1983), and theoretically and in the laboratory by Mokrane et al. (2009) and Chaabouni et al. (2012).

A deuterium enrichment of the water ice mantle is caused by the higher sticking probability of small deuterated species (Matar et al., 2010). In addition, during the sublimation a sudden H-D exchange reaction is activated leading to the process \( \text{H}_2\text{O} \rightarrow \text{HDO} \) (Matar et al., 2008). However, so far one has not observed clear evidence for a favored formation of single HD or OD species compared to H\(_3\) or OH (Hama et al., 2012). In the gas phase of cold cores the direct formation of water molecules is less effective. Accordingly, \( \text{H}_2\text{O} \) molecules and the deuterated compounds formed on the grain surface can be desorbed non-thermally via the influence of cosmic rays and far UV photons. At the end of our cold collapse the dust temperature in the hot corino region is high enough for a thermal desorption of the water molecules from the grain surfaces without changing the high D/H ratio of these molecules. A reduction of the high D/H ratio would occur, however, if UV radiation and X-rays lead to the dissociation of \( \text{H}_2\text{O}, \text{HDO} \), and \( \text{D}_2\text{O} \) combined with a reformation of these molecules by the already mentioned hot neutral reactions in the gas phase. This process starts as soon as the proto-star enters its T-Tauri phase while being surrounded by a solar nebula arranged in a stationary optically thick disk (compare Fig. 1). In cold cores the amount of ions is fairly low causing a low rate of ion-molecule reactions. In the outer translucent region of the core the gas phase water not adsorbed on dust grains is dissociated by the far UV radiation. The typical ion reactions which form water and its deuterated compounds are already proposed by Glassgold and Langer (1976).

The reactions in the first and second line are characterized by charge transfer and the ones in the last line are called dissociative recombination (Larsson et al., 2012). These reactions occur in diffuse (0.1 < A\(_V\) < 1), translucent (1 < A\(_V\) < 5) but also in dark (5 ≤ A\(_V\)) clouds which belong to the cold neutral matter phase of the interstellar medium (Turner, 1993, 2000; Hollenbach et al., 2012). In these dark clouds having a complete UV shielding the relative abundances of water with respect to hydrogen is less than 10\(^{-8}\) (Bergin and Snell, 2002) which is in agreement with the data mentioned in the Introduction and in

\[
\begin{align*}
\text{H} &+ \text{O} \rightarrow \text{OH} \\
\text{H} + \text{OH} &\rightarrow \text{H}_2\text{O} \\
\text{O}_3 &+ \text{D} \rightarrow \text{O}_2 + \text{OD} \\
\text{OD} &+ \text{OD} \rightarrow \text{D}_2\text{O} \\
\text{H}_2\text{O} &+ \text{D}_2\text{O} \rightarrow \text{2HDO}. \\
\end{align*}
\]
agreement with the resulting ionization fraction which is typically \(10^{-8}\) (de Boisanger et al., 1996). Deuterium fractionation can be understood by considering the exothermal reaction \(H_3^+ + HD \rightarrow H_2D^+ + H_2\) which has a difference in the bond dissociation energy equivalent to 232 K (Roueff et al., 2007). Thus, in cold dense cores the right arrow is favored leading to an enhancement of the ratio \(H_2D^+/H_3^+\) with respect to the HD/H\(_2\) abundance. However, this is the point to mention the OPR again. For the gas phase species \(H_2D^+\) in Eq. (19) and an OPR \(>> 0\), the following reactions (among many others) must be added to the chemical network:

\[
\begin{align*}
\rightarrow p \cdot H_3^+ + HD & \quad \text{with} \quad 7.7 \times 10^{-11} \\
\rightarrow o \cdot H_3^+ + HD & \quad \text{with} \quad 8.3 \times 10^{-11} \\
o \cdot H_2D^+ + o \cdot H_2 & \quad \text{with} \quad 9.2 \times 10^{-11} \\
\rightarrow p \cdot H_2D^+ + p \cdot H_2 & \quad \text{with} \quad 1.8 \times 10^{-10} \\
\rightarrow o \cdot H_2D^+ + p \cdot H_2 & \quad \text{with} \quad 2.35 \times 10^{-10}.
\end{align*}
\]

Comparing the Langevin reaction rates in Eq. (19') the first two relations are less important than the other ones but can cause a de-deuteration of the gas species (Flower et al., 2006). The influence of three initial OPR values \(10^{-4}, 10^{-3}\) and 3) of \(H_2\) on the D/H ratio of water and other species observed in the coma of comets or in the interstellar ice was studied very recently by Taquet et al. (2014) using a semi-empirical model of a collapsing cloud core and a well-elaborated chemical network. For the maximum increase of OPR by a factor of \(3 \times 10^3\), they found a small decrease of the D/H for water in the gas phase (a factor of \(2.5\)) and a large decrease for the ice phase (a factor of \(27.2\)). We will keep this result in mind and will use it for our conclusions.

**RESULTS**

In Subsection "The chemical model of the gas and dust phase" we have sketched how to compute the chemical interaction between the gas and the dust phase. Here, we will also use primarily the notation ice phase. In our case the species of the ice phase are the same as the species of the dust phase, since in contrast to the dust mantle its nucleus does not change chemically in our model. However, this is not always the case. Water formed by hot neutral reactions could be chemisorbed by fractal dust grains in large abundances in a temperature range around 900 K (King et al., 2010).

**Formation of \(H_2O\) and isotopologues in the quasi-stationary core**

We have to underline that the chemical evolution of the partially shielded core is studied, but not the one of the gas shell. Otherwise, we would have to apply special techniques developed for the photon-dominated regions, which are explained and discussed by Hollenbach and Tielens (1999).

From the simulated chemical data set for each grid point of the core, we obtain the relative gas phase abundances of \(H_2O\) and its isotopologues \(x_{H_2O}, x_{HDO}, x_{D_2O}\) as well as the corresponding relative abundances for the ice species \(x_{H_2O}^*, x_{HDO}^*, x_{D_2O}^*\) which are presented and discussed in the following. According to our results, the ice mantle forms in \(10^5 - 10^6\) years on the dust grains of the quasi-stationary core and changes slowly afterwards. The most frequent ice species are \(H_2O\) and CO, but due to the composition in Table 3 \(H_2O\) is the dominant one, i.e., \(x_{CO}^*/x_{H_2O}^* \leq 0.13\). A general comparison between gas and ice phase shows that the maximum abundance \(x_{H_2O}^*\) in the gas phase is nearly \(10^{-10}\) (Fig. 6) and much lower than \(x_{H_2O} = 1.7 \times 10^{-4}\) (Fig. 8). The abund-

---

**Figure 6.** Radial and temporal distribution of the \(H_2O\) abundance in the gas phase \(x_{H_2O}\). The patterns of the HDO and D\(_2\)O abundance distributions are quite similar to the one of \(H_2O\).

**Figure 7.** Radial and temporal distribution of the abundance ratio \(x_{HDO}/x_{H_2O}\) in the gas phase. The percentage variation of the abundance ratio between 0.01 and 1% corresponds to a deuterium enrichment \(\delta D\) between \(-800\) and \(+31,000\)‰.
dance profiles in both phases change slightly with time because of the thermal and UV related evaporation (Semenov, 2006). Recent results have shown that the model of Öberg et al. (2009a, b) produces a higher evaporation rate, which conforms better with observations (Caselli et al., 2012). According to Wakelam et al. (2014), desorption due to exothermic chemical reactions is even more important but not included in our model. One recognizes a transit range around 5,000 AU given by the condition that the visual extinction $A_V$ is high enough ($A_V = 5–6$ mag) to completely shield the far UV radiation which otherwise can destroy H$_2$O molecules or desorb OH species as well as their isotopologues.

There is a small inward motion of the shielding zone caused by an interaction between chemical processes and the inward motion of the dust grains (even for the relatively low UV intensity of the standard ISRF). The transit regions for HDO and D$_2$O are located in the same radial range but show a lower propensity for inward motion. The variabilities of the $D/H$ and $D_2/H$ ratios (Fig. 7) comprise about three to four magnitudes. In addition, both have the maximum in the range of 5,000 AU.

The distributions of the ratios $x^*_{\text{HDO}}/x^*_{\text{H}_2\text{O}}$ and $x^*_{\text{D}_2\text{O}}/x^*_{\text{H}_2\text{O}}$ are characterized for $\tau > 1–2$ Myr by small time and clear radial variations just as the relative abundances themselves. The H$_2$O abundances in the inner core are slightly lower while the deuterated species present the lower values in the outer core range (Figs. 9 and 10). Further we should mention that the temporal evolution of $x^*_{\text{H}_2\text{O}}$ and $x^*_{\text{HDO}}$ in the inner core proceeds contrastively and that $x^*_{\text{D}_2\text{O}}$ stays relatively constant with time. If one considers the chemical reactions in Eq. (18) one sees that the formation of H$_2$O on the dust surfaces is driven primarily by the abundance of O which cannot be destroyed by UV radiation, while the formation of HDO and D$_2$O depends more on O$_3$ or even O$_5$ (Minissale et al., 2013). Models for the corresponding reaction rates and for the quantum tunneling of O (Jing et al., 2012; Chaabouni et
D/H ratio of water 539

al. et al., 2012; Minissale et al., 2013) are derived partly based on the formation model of H2, HD, and D2 in the ice phase (Cazaux and Tielens, 2004). In addition, the gas phase O2, also needed for the O3 formation, is more abundant in the inner region of the core than in the outer region.

A comparison of Fig. 7 with Fig. 11 shows that the D/H ratios in both phases have very similar profiles and variability ranges. However, in the dust phase, the radial profiles of x^H2O differ clearly from those of x^HDO and x^D2O. The decreases of the HDO and D2O abundance below 10^{-6} and 10^{-8} at r > 6,000 AU, respectively, in contrast to the small increase of the H2O abundance (Figs. 8, 9, and 10) reflect the destruction of gas phase O2 by far UV photons. Of course, OH is also dissociated, but can be formed much more easily on the dust surface, again. Thus, one realizes that the profile of the visual extinction influences the abundances of dust phase HDO and D2O more strongly and contrary to the dust phase H2O because of the different formation mechanisms (Eq. (18)).

Formation of H2O and isotopologues in the collapsing core

Generally, the gas phase of our collapsing core is chemically influenced by the desorption of volatiles like H2O or CH3OH, super-volatiles like CO2 or CH4 (Belton, 2010), and the UV radiation entering the core from the outer boundary. If one travels on a Lagrange path into the core center, four chemical zones appear successively. They do not necessarily agree in their boundaries with the density zones presented earlier (see Subsection “The collapsing cloud core”). However, in the same way as the density zones, the chemical zones have time dependent boundaries influenced by the UV radiation and the increasing temperature due to the collapse. At the beginning of the collapse, the ice remains chemically unchanged and is transported with the gas flow into the inner region of the core. If the temperature reaches ~30 K the CO/H2O ratio drops quickly to ~10^{-4}, i.e., CO joins the gas phase while water is still locked-up in the dust. Based on the UV radiation and the thermal desorption the four zones are characterized as follows:

1. The photo-dominated zone reaching about 4–6 AU into the core;
2. The gas-depleted zone mainly influenced by cosmic rays and marginally by UV radiation in its outer part; the temperature at its inner boundary (7–10 AU) is high enough for the thermal desorption of CO (~30 K) denoted as a super ice line (SIL);
3. The transition zone with a gas phase enriched by the super-volatiles and located between the SIL and the radius (~2 AU) where the temperature is high enough for thermal desorption of H2O, which is denoted as water ice line (WIL); and
4. The hot corino zone between WIL and the dust destruction line, where the temperature is higher than the maximum condensation temperature of the minerals found in the SN.

Concerning these chemical zones, the huge part of the collapsing core belongs to the gas-depleted zone. The chemically interesting zones are the transition and the hot corino zone (HCZ). However, near the inner boundary of the HCZ, the jet forming region is located (Ramsey and Clarke, 2011) since the dust destruction causes the injection of metals into the gas phase. The related increase of the degree of ionisation drives the magnetic interaction between a T-Tauri star and a rotating disk. Nevertheless, we are primarily interested in finding the initial chemical abundances of the planet forming disk range, i.e., the initial values of the last stage of our SN-model so far does not consider jets. Hence we can restrict the complete region of the chemical evolution during the collapse to an interval r ∈ [0, 1 AU, R_{CE}] with R_{CE} ≤ 4,000 AU.

Based on this restriction we have selected a set of Lagrangian paths and calculate the chemical evolution of...
of deuterium enrichment values are $x*_{HDO}/x*_{H2O}$ in the gas phase. We find $x*_{HDO}/x*_{H2O}$ \in [10^{-4}, 0.1] AU and $x*_{HDO}/x*_{H2O}$ \in [0.05, 0.08] AU for the dust phase. The related intervals of WIL locations given by $1.5 AU < r_{WIL} < 0.625$, one finds indeed a relatively broad range for undepleted and depleted zone.

Figure 12 illustrates that the HCZ is related to the region in which water is enriched due to its desorption from the icy dust mantles, while Fig. 13 presents the corresponding pattern of the H$_2$O abundance $x*_{HDO}$ for the gas phase. Both figures show that for early collapse times the WIL moves further out due to the increasing temperature. Zooming into Fig. 12 and considering the interval $0.6 < r < 0.625$, one finds indeed a relatively broad range of WIL locations given by $1.5 AU < r_{WIL} < 2.25 AU$, where $r_{WIL}$ denotes the radial position of the WIL.

The interval corresponds to the region between Mars and the inner Main Belt boundary and the maximum relative water abundance is $1.7 \times 10^{-4}$. However, a zoom-in of Fig. 13 shows that significant depletion of ice phase water, $x*_{HDO,dep} = 0.1 x*_{HDO,undep}$ (dep abbreviated for depleted and undep for undepleted) occurs for $r \leq 1 AU$. Indeed one finds that the minimum relative abundance is $1.1 \times 10^{-10}$, while the maximum is $1.8 \times 10^{-4}$. The available thermal energy in the outer range of the HCZ is not high enough to produce large amounts of gas phase water via hot neutral reactions (Eq. (17)). These reactions can proceed efficiently only beyond the white line in Fig. 3, i.e., if $0.1 \leq r \leq 0.8 AU$. At the end of the collapse and for $r = 1 AU$, the maximum gas and ice phase abundances are quite similar:

$$\text{max}(x*_{HDO}) = 1.2 \times 10^{-4} \quad \text{and} \quad \text{max}(x*_{HDO}) = 1.6 \times 10^{-4}.$$  

However, the ice phase minimum violates our criteria for a significant ice phase depletion because of $\text{min}(x*_{HDO}) = 4.8 \times 10^{-5}$, which tells us that the desorption process is not finished in the HCZ and will continue in the disk phase. Since $R_C$ is lower than the complete core radius, $R_C$, the abundances presented in Figs. 12 and 13 originated mainly from the gas-depleted and the transition zone. Accordingly the water ice on the surface of dust grains as well as the one in the gas phase remain unchanged until the corresponding gas pockets reach the IL. Hence, our Lagrange paths symbolize large-scale water inflows at super-sonic velocities (Fig. 5).

The abundance ratios of the HDO and D$_2$O molecules $x*_{HDO}/x*_{H2O}$ and $x*_{D2O}/x*_{H2O}$, of the gas phase, are shown in Figs. 14 and 15. Beyond the super ice line SIL, most of the gas pockets on the Lagrange paths have a slowly varying ratios in both phases. One obtains for the gas phase $x*_{HDO}/x*_{H2O} \sim 0.01$ and $x*_{D2O}/x*_{H2O} \sim 0.003$ in the gas-depleted zone.

For the ice phase we obtain $x*_{HDO}/x*_{H2O} \sim 0.04$ and $x*_{D2O}/x*_{H2O} \sim 10^{-4}$ with a much lower variability in the same zones. Concerning the deuterium enrichment one gets $\delta D = 31,050$‰ for the gas phase and an even larger value $\delta D = 127,200$‰ for the dust phase. For the transition zone, one realizes that the gas phase ratios $x*_{HDO}/x*_{H2O}$ and $x*_{D2O}/x*_{H2O}$, in contrast to the related abundances, start changing after the gas pocket has reached the its outer boundary which is equivalent to the SIL. For both gas phase abundance ratios, $x*_{HDO}/x*_{H2O}$ and $x*_{D2O}/x*_{H2O}$ in the inner transition zone ($r \leq 7 AU$), an interesting pattern is seen from Figs. 14 and 15 shown as a first decrease and a subsequent increase of them. This decrease/increase pattern repeats somehow if one moves further inwards. The outer pattern of $x*_{HDO}/x*_{H2O}$ shows a strong variation since it decreases from $-0.01$ to less than $10^{-3}$ and increases to $0.3-0.5$, in total 2.5 magnitudes. The more inner pattern are smoother and vanish finally. In case of $x*_{D2O}/x*_{H2O}$, the ratio drops from $10^{-3}$ to $10^{-4}$ and rises to $0.03$, i.e., about 2.5 magnitudes as well. It seems that these oscillations...
seen in the abundance ratios enlighten slight differences in the abundance profiles of HDO and D₂O with respect to the related profile of H₂O. In addition, one has to note that in the transition zone the desorption of water and its isotopologues starts very slowly and initially does not produce molecule abundances higher than those produced by gas chemistry. Keeping this in mind, the oscillations in the Figs. 14 and 15 are a very natural phenomenon.

**Conclusions and Outlook**

**Conclusions**

Water has been formed in large abundances (1.8 × 10⁻⁵) and with a very small radial variability in the cold quasi-stationary core, which is the first stage of our SN-model (Fig. 1). These are large amounts that are locked-up as ice mantles on the surface of the dust grains (Fig. 8). The gas phase abundance of water depends on the non-thermal desorption efficiency of H₂O molecules from the ice phase. Its maximum (~10⁻¹⁰) occurs in the middle core region (Fig. 6) while the minimum is located at its outer boundary where desorbed water molecules dissociate because of the far UV flux from the ISRF entering the partially shielded core from outside. Since both gas- and dust-phase water form on cold grain surfaces or by ion molecule reactions with a very low efficiency in the cold gas phase, the related profiles of the D/H ratios (δD/δH₂O and δD/δH₂O) in both phases are almost equal (Figs. 7 and 11). The fairly large variability of these profiles is seen comparing the ratios between 0.001 (δD = 0.0000006) and 0.01 (δD = 0.0000006) in the inner core and 10⁻⁴ (δD = 0.0000006) in the outer region. It is caused by the influence of the far UV flux since the photo-dissociation of gas phase O₂ reduces the amount of adsorbed O₃ on the dust surfaces and therefore the formation of gas-phase HDO and D₂O. Accordingly the UV radiation of the ISRF can reduce the D/H ratio of water in the dust and gas phase to 10⁻⁴ or to a negative deuterium enrichment value, respectively. The gas phase water abundance of a cold core on the verge to collapse was observed by Caselli et al. (2012) from Herschel data of L1544. They derived a relative abundance above 1.7 × 10⁻⁵ which nearly agrees with the highest values of our simulations. Consequently, we need to improve the used photo-desorption model and include the data reported by Öberg et al. (2009, a, b). The abundance of ice phase water is hard to be observed, but the derived value of 6 × 10⁻⁴ added to the observations by Caselli et al. (2012) is comparable to the observed fractional water abundance towards the Orion hot cores which is a high mass star forming region (Neill et al., 2013). Our maximum values of 3 × 10⁻⁴ to 6 × 10⁻⁴ are found in the middle or upper core, but there are also observations towards the low mass star forming site NGC1333, which are even smaller (Kristensen et al., 2010) than our value. The deuterium fractionation of water (δD/δH₂O) varies between 0.02% and 8% for the observed regions described in the Introduction, which nearly agrees with the observations.

The chemical abundances obtained from Stage 1 of our SN-model determine the gas and dust-phase composition at the beginning of the core collapse. We derived a semi-analytical model reproducing a cold outside-in collapse to include the next stage of the solar nebula evolution. Comparisons with other collapse simulations (Schöne and Tscharnuter, 2011; Saigo et al., 2008) have shown that these models produce a similar radial density distribution but find higher velocities and temperatures in the inner core region. The main important reason for these differences is the use of a polytropic equation of state (11). According to Wardle et al. (2014), there is some interaction between the chemistry and the dynamics mediated by their state equation. This interaction needs to be considered in the future by adding an additional term to Eqs. (4) and (5), and by adding the energy conservation equation to our set of MHD equations (7)–(10). Our collapse model provides radially symmetric time-dependent density, temperature and velocity distributions which are used to compute a large set of Lagrange paths, symbolizing an inflow stream of the gas-dust material. This type of inflow signature was found by Mottram et al. (2013) in the observed water transition lines towards proto-stars in order to study the gas flow velocity of collapsing cores. They have found evidence for large-scale super-sonic inflows (compare with Fig. 5) of water with Herschel and determined that these flows occur on a scale between core and envelope, i.e., 3 × 10⁻⁴ to 10⁻³ AU for IRAS 15398, L1527, or L1157. For NGC1333-IRAS4A these flows extend over the envelope, i.e., the related scale is ≥10⁸. Moreover, based on these observations they suggest an outside-in rather than inside-out collapse in agreement with the model presented here.

Our cold collapsing core with its small hot corino delivers enough energy at 1 AU (located in the HCZ) to increase the relative abundance of gas phase water by thermal desorption to 1.2 × 10⁻⁴ while the dust phase is only slightly depleted (0.5 × 10⁻⁴). In the region between Venus and Mercury the gas phase abundance is even higher (1.7 × 10⁻⁴). These data agree with the observed water abundances between 10⁻⁴ to 10⁻³ in the outflow region of NGC1333 (Kristensen et al., 2010). Lower values of 3 × 10⁻⁴ and 5 × 10⁻⁷ are found for the middle and envelope region of IRAS 16293-2422 (Parise et al., 2005) which could not be reproduced in our model. There seem to be two possible explanations; First of all, IRAS 16293-2422 is a binary protostar at least and perhaps in the disk phase already. Second, our model only takes into account the radial range of the HCZ and the non-thermal desorption rate. Concerning the related D/H ratio, the related gas and...
dust phase ratios $^{13}$C/O and $^{13}$C/H at 1 AU vary in the interval [0.001, 0.1] and [0.03, 0.05] (or based on the deuterium enrichment: $\Delta D$ (‰) $\in$ [2,200; 320,000] and $\Delta D^+$ (‰) $\in$ [95,200; 159,300]), respectively. A comparison of these values with observations towards NGC 1333 which vary from 0.003 to 0.08 for IRAS2A and from 0.007 to 0.03 for IRAS4A, shows a fairly well agreement. Aikawa et al. (2012) have obtained similar values for their model of the deuterium fractionation of a protostellar core. There is a large variability for the D/H ratio due to oscillations in the transition and outer hot corino zone ($1 < r < 10$ AU, Fig. 14), but observations will not resolve this. For hot corinos or hot cores the obtained deuteration is slightly too large (Wakelam et al., 2014). Indeed for the IRAS 16293-2422 hot corino one gets 0.09% (Persson et al., 2013) while for the hot core of NGC 6334 I (Emprechtinger et al., 2012), the D/H ratio of 0.02% is even smaller. A source for a de-deuteration could be an OPR ratio between 0.1 and 1 (Pagani et al., 2013). Based on their model, Taquet et al. (2014) report a maximum decreasing factor of 2.3 for the gas phase water and 27 for the dust phase assuming OPR = 3. A further source could be a cosmic ray ratio higher than $10^{-13}$ (Wakelam et al., 2014). Moreover, the temperature and size of the hot corino can increase during the disk phase because of the transition of the young proto star to a T-Tauri star and the related increase of stellar radiation. Indeed recent disk models (Willacy and Woods, 2009; Thi et al., 2010; Furuya et al., 2013) produced a higher dust and gas temperature in the central plane region of the inner disk and obtained a lower D/H ratio of water in this region.

**Outlook**

As already mentioned, we plan to extend our chemical module by allowing a variable OPR and an improved non-thermal desorption. In addition we will add the disk stage, since water in special regions (near the dust sublimation layer and on the surface of a flaring disk) is destroyed by energetic radiation (Bruderer et al., 2009) and re-formed by hot neutral reactions. As a consequence, these processes influence the D/H ratio of water and need to be considered. In addition, the dust sublimation layer (and thus the inner boundary of the HCZ) is located near the outflowing jets (Goicoechea et al., 2012) suggesting an extension of the disk model according to the approach of Comb et al. (2010).

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