

Will my engine ride the beam?

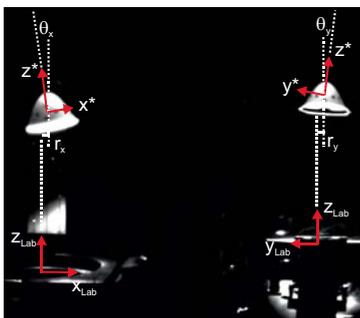
Perfect Beam-Riding

- Restoring lateral momentum coupling

$$c_{m,i} = \frac{\Delta p_i}{E_L} \approx \frac{m \cdot \Delta v_i}{E_L} = b^{(m)} \times x_i, \quad b^{(m)} < 0$$

- Restoring angular momentum coupling

$$c_{L,i} = \frac{\Delta L_i}{E_L} \approx \frac{J_{ii} \cdot \Delta \omega_i}{E_L} = b^{(L)} \times \vartheta_i, \quad b^{(L)} < 0$$



Free flight experiment, stereoscopic view

Lateral^(m)-angular^(L) Coupling

$$\begin{pmatrix} b_i^{(m)} & b_{\vartheta,i}^{(m)} \\ b_i^{(L)} & b_{\vartheta,i}^{(L)} \end{pmatrix} \begin{pmatrix} r_i \\ \vartheta_i \end{pmatrix} \approx \begin{pmatrix} c_{m,i} \\ c_{L,i} \end{pmatrix} = \frac{1}{P_L} \begin{pmatrix} \bar{F}_i \\ \bar{M}_i \end{pmatrix} \approx \frac{1}{P_L} \begin{pmatrix} m \cdot \ddot{r}_i \\ J \cdot \ddot{\vartheta}_i \end{pmatrix}$$

- Linearization of momentum coupling: $b_i^{(j)}$: craft-specific constants
- Quasi-continuous approximation: Equations of motion

Requirements for Beam-riding

Necessary condition

$$\delta = \left[\frac{b_i^{(m)}}{m} - \frac{b_{\vartheta,i}^{(L)}}{J} \right]^2 + 4 \frac{b_{\vartheta,i}^{(m)}}{m} \frac{b_i^{(L)}}{J} \geq 0$$

Sufficient condition

$$\frac{b_i^{(m)}}{m} + \frac{b_{\vartheta,i}^{(L)}}{J} \leq - \sqrt{\left(\frac{b_i^{(m)}}{m} - \frac{b_{\vartheta,i}^{(L)}}{J} \right)^2 + \frac{b_{\vartheta,i}^{(m)}}{m} \frac{b_i^{(L)}}{J}}$$

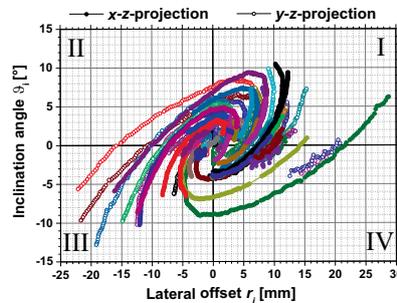
Restoring momenta exceed lat.-ang. coupling.

Implications

- Assumption of 2D approach
- Dependency on BEP mass, CMS position, momentum of inertia
- Independency on laser power

Example - Parabolic Lightcraft

Lateral-angular Motion



Trajectories from free flight experiments

Motion Characteristics

Spiral-formed trajectories

$$\begin{pmatrix} r(t) \\ \vartheta(t) \end{pmatrix} = \exp(\kappa t) \begin{pmatrix} \hat{r} \cos(\omega t + \varphi) \\ \hat{\vartheta} \cos(\omega t + \varphi + \Delta\varphi) \end{pmatrix}$$

Oscillation period $T = 0.78$ s

Damping constant $\kappa = 0.97$ s⁻¹ > 0

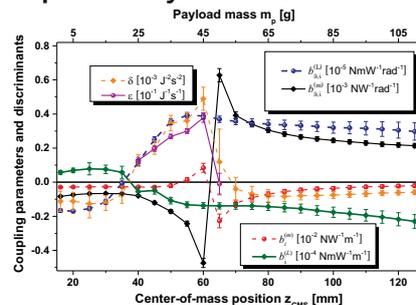
Specific Matrix of Flight Dynamics

$$\begin{pmatrix} b_i^{(m)} & b_{\vartheta,i}^{(m)} \\ b_i^{(L)} & b_{\vartheta,i}^{(L)} \end{pmatrix} = \begin{pmatrix} -0.4 \text{ N}/(\text{MW} \cdot \text{mm}) & -2 \text{ N}/(\text{MW} \cdot \text{deg}) \\ +20 \text{ mN} \cdot \text{m}/(\text{MW} \cdot \text{mm}) & -70 \text{ mN} \cdot \text{m}/(\text{MW} \cdot \text{deg}) \end{pmatrix}$$

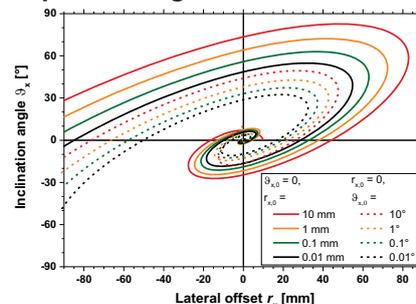
$$\delta = -1.27 \cdot 10^{-4} \text{ J}^{-2} \text{ s}^{-2} < 0$$

Failure of beam-riding

Impact of Payload Mass



Impact of Alignment at Launch



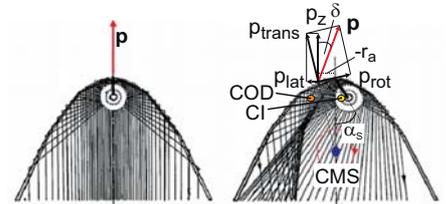
Solution strategies

Geometric Optimization



Cross-section of honeycomb-like thruster array with enhanced lateral coupling

Movable Detonation Center

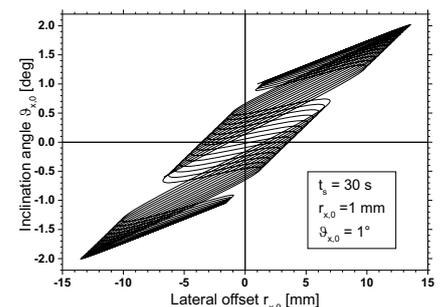


Shift of the detonation center (COD) by tilt of the ignition pin inside the lightcraft

Alternative Solutions

- Spin-stabilization (Myrabo)
- Decoupling of optics and nozzle (Rezunkov)
- Dynamic adjustment of laser beam position (Takahashi)

Theoretical Solution



Knowledge for Tomorrow

