On the Processing of Very High-Resolution Spaceborne SAR Data

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Abstract—This paper addresses several important aspects that need to be considered for the processing of spaceborne SAR data with resolutions in the decimeter range. In particular, it will be shown how the motion of the satellite during the transmission/reception of the chirp signal and the effect of the troposphere deteriorate the impulse response function if not properly considered. Further aspects that have been investigated include the curved orbit, the array pattern for electronically steered antennas, and several considerations within the processing itself. For each aspect a solution is proposed, and the complete focusing methodology is expounded and validated using simulated point targets and staring spotlight data acquired by TerraSAR-X with 16 cm azimuth resolution and 300 MHz range bandwidth.

Index Terms—Synthetic aperture radar (SAR), Spotlight SAR, SAR processing, stop-and-go approximation, troposphere.

I. INTRODUCTION

Spaceborne SAR processing is already an established topic. Many efficient solutions have been proposed over the last decades for every imaging mode, be it stripmap, spotlight, ScanSAR or TOPS (Terrain Observation by Progressive Scans). However, the assumptions of some of these algorithms start to be invalid depending on the acquisition geometry, especially in terms of the image resolution. While airborne SAR processors achieve nowadays resolutions in the decimeter range, the same approaches do not perform perfectly in a low Earth orbit (LEO) scenario, mainly due to the much greater sensor velocity and the larger distances involved. Furthermore, when getting close to decimeter resolutions several effects appear, which do not show up in an airborne scenario and must be taken into account to achieve a satisfactory focusing performance.

In order to design efficient processors that overcome these effects it is of great help to have real data available, which in the current case are provided by the TerraSAR-X (TSX) satellite. The TerraSAR-X mission represents one of the most successful high-resolution spaceborne SAR missions up to date, not only because of the impressive geometric and radiometric accuracy of the calibrated products [1], [2], but also because the TSX satellite has become the perfect test-bed for future SAR mission concepts thanks to its flexible commanding and operation. TSX has demonstrated for the first time in space several innovative modes like the TOPS mode [3]–[5], spaceborne bistatic imaging (together with its twin satellite, TanDEM-X) [6], bidirectional SAR imaging [7], or digital beamforming [8]. One of the last milestones achieved with the TSX satellite has been the acquisition of staring spotlight (ST) data. By exploiting the maximum azimuth steering capability of the sensor, it is possible to achieve a steering range of ±2.2 degrees, hence achieving a potential unweighted azimuth resolution of 16 cm [9]–[11]. Thanks to these data several effects could be precisely investigated and corrected, as expounded in the following sections.

The paper is divided as follows. Section II addresses the main aspects in the processing of very high resolution spotlight data, while Section III considers further secondary aspects. In all cases, a solution is proposed in order to achieve proper focusing. Section IV suggests a processing flow including the proposed corrections and finally Section V presents several results including simulations and high resolution spotlight data acquired by TSX.

<table>
<thead>
<tr>
<th>Mode</th>
<th>Az. resolution</th>
<th>Az. scene size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sliding spot. (SL)</td>
<td>1.7 m</td>
<td>10 km</td>
</tr>
<tr>
<td>High-res. spot. (HS)</td>
<td>1.1 m</td>
<td>5 km</td>
</tr>
<tr>
<td>Staring spot. (ST)</td>
<td>0.21 m</td>
<td>3 km-5 km</td>
</tr>
</tbody>
</table>

II. KEY ASPECTS OF HIGH RESOLUTION SPACEBORNE SAR PROCESSING

This section expounds the main effects that need to be considered when processing very high resolution spaceborne data. It is assumed that the high azimuth resolution is achieved by using the spotlight mode, be it staring or sliding [9]. The ST mode illuminates the same spot on ground during the whole integration time, while the sliding spotlight mode slides the beam to extend the azimuth coverage, which occurs at the expense of azimuth resolution. In both cases, the antenna is steered in the azimuth dimension, either mechanically or electronically. Table I summarizes the azimuth resolution and the azimuth scene extension for the three spotlight modes offered by the TSX satellite, where note that the ST mode has been recently implemented in the TSX ground segment.
TABLE II
TSX STARING SPOTLIGHT ACQUISITION OVER OBERPFaffenHOFEN, GERMANY

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Central frequency</td>
<td>9.65 GHz</td>
</tr>
<tr>
<td>Total azimuth processed bandwidth</td>
<td>38.5 kHz</td>
</tr>
<tr>
<td>Azimuth resolution</td>
<td>16 cm</td>
</tr>
<tr>
<td>Chirp bandwidth</td>
<td>300 MHz</td>
</tr>
<tr>
<td>Ground range scene size</td>
<td>8.8 km</td>
</tr>
<tr>
<td>Azimuth scene size</td>
<td>3.4 km</td>
</tr>
<tr>
<td>Incidence angle</td>
<td>35°</td>
</tr>
<tr>
<td>Central point (longitude/latitude)</td>
<td>11.264°, 48.088°</td>
</tr>
</tbody>
</table>

workflow and is available since October 2013. Due to the larger integration time of the ST mode, several effects appear, which can be neglected in the operational sliding spotlight (SL) and high resolution spotlight (HS) modes.

The first of these effects occurs due to the motion of the satellite during the transmission and reception of the chirp signal. This effect is well-known in the frame of frequency-modulated continuous-wave (FMCW) SAR radars mounted on airborne platforms [12], [13]. In Section II-A, the impact on high-resolution pulsed radars is analyzed.

The curved orbit and the validity of the hyperbolic approximation is also a topic that has been addressed before in the literature [14]–[16]. Section II-B suggests an innovative correction of the orbit curvature based on state-of-the-art airborne SAR motion compensation techniques [17]–[19]. Besides being very simple to implement, it can also accommodate to a large extent the azimuth variance of the geometry.

One last aspect is the delay introduced by the troposphere in the range history. This delay can change significantly due to the variation of the squint (or azimuth) angle during the formation of the synthetic aperture, hence resulting in azimuth defocusing if not considered, especially at higher frequency bands. Section II-C addresses this topic and suggests a model-based correction.

Through the different sections, ST data acquired by TSX are used. The particular data take was acquired over Oberpfaffenhofen, Germany, where five corner reflectors (CRs) were deployed in order to analyze their impulse response function (IRF) and validate the methodology. The main data take parameters appear in Table II.

A. Stop-and-Go Approximation

In the processing of spaceborne SAR raw data it is usually assumed that the platform does not move during the transmission of the pulse signal and the reception of the backscattered echoes. Such an assumption is usually called the stop-and-go or start-stop approximation and has mainly two effects. A “slow-time” one, which is linked to the fact that the satellite indeed moved between transmission and reception, e.g., about 30 m in the TSX case. This fact implies mainly a range-dependent azimuth shift of the focused signal, which can be efficiently considered with a linear azimuth phase ramp in the range-Doppler domain after the range cell migration correction (RCMC) given by [20]

\[ H_{\text{sinc}}(f_s, r) = \exp \left[ j \cdot 2\pi \cdot \frac{r}{c} \cdot f_s \right], \]  

where \( r \) is the range vector, \( f_s \) is the azimuth-frequency vector, and \( c \) is the speed of light. With this correction the targets have a constant azimuth time over range and are aligned with the annotated GPS instrument time. An additional effect occurs due to the slight bistatic operation, which becomes more evident the larger the integration time, i.e., the range history is the sum of two hyperbolas rather than just one. Although the effect is minor, it is properly accounted for in the correction suggested in the next section, where the accommodation of the curved orbit uses the position of the satellite at the transmission and reception events for the reference range.

A second effect deals with the motion of the satellite during the transmission and reception of the chirp signal itself, i.e., a “fast-time” effect or, in other words, a real Doppler effect. The TSX chirp signal has a length of about 50 \( \mu s \), during which the satellite moves about 40 cm in the azimuth direction. This effect is well-known in FMCW SAR systems [12], [13]. The phenomenon was also discussed in [21] for pulsed radars, where the analysis was done in terms of a mismatch during the matched filtering in range. As shown in [21], the difference in the instantaneous frequency between the nominal range variation and the one including the motion of the platform is given by

\[ \Delta f = -\frac{2}{\lambda} \frac{\partial R(t)}{\partial t} = f_{\text{DC}}, \]  

where \( \lambda \) is the wavelength, \( R(t) \) is the range history and \( f_{\text{DC}} \) is the Doppler centroid caused by the platform movement during transmission/reception. By assuming a large time-bandwidth product, the shift in the signal in the range-time dimension is then given by

\[ \Delta \tau = \frac{\Delta f}{K_r} = \frac{f_{\text{DC}}}{K_r}, \]  

where \( K_r \) is the chirp rate and \( \tau \) represents the fast time. This means that there is a range shift present in the signal as a function of the instantaneous azimuth frequency. In the case of large azimuth bandwidths, this effect will introduce different range shifts along the azimuth integration interval, hence deteriorating the impulse response function in both dimensions.

Another intuitive way to visualize this effect is by considering different azimuth phase ramps as a function of the range frequency, since, due to the large time-bandwidth product, there is a direct mapping between fast-time and range frequency. In other words, due to the motion of the satellite, the zero-Doppler time changes as a function of the range frequency, corresponding to a range-frequency dependent linear phase ramp in the azimuth dimension. The azimuth shift can then be expressed as

\[ \Delta t = \frac{\tau_p \cdot f_i}{B_{rg}} = \frac{f_i}{K_r}, \]  

where \( f_i \) is the range frequency, \( t \) is the slow time and \( \tau_p \) and \( B_{rg} \) are the chirp length and chirp bandwidth, respectively.

Fig. 1 shows the resulting phase error due to the stop-and-go approximation measured over a corner reflector of the TSX ST acquisition and the corresponding IRF. The first plot on the left is the phase of the 2D phase spectrum after removing the global linear ramps due to the target position. The error reaches
a chirp length of 50 μs, the bandwidth 300 MHz, and the azimuth processed bandwidth 38.5 kHz.

The chirp length is 50 μs at the edges of the spectrum. If not corrected, this error introduces resolution loss of up to 15% in both dimensions for an azimuth bandwidth of 38.5 kHz (16 cm resolution without weighting), a range bandwidth of 300 MHz and a chirp length of 50 μs. Please note that in order to generate the plots of Fig. 1 and properly appreciate the effect of the fast-time stop-and-go approximation, the suggested corrections for the other aspects, namely the consideration of the curved orbit and the troposphere, were applied (see Sections II-B and II-C, respectively).

Since the effect is space invariant, it can be easily corrected in the 2D frequency domain using the following phase function [12], [21]

\[ H^\text{fast} (f_a, f_r) = \exp \left[ j \cdot 2\pi f_a \cdot \frac{f_r}{K_r} \cdot f_r \right]. \]  

This phase correction shall be applied at the beginning of the processing before calling the focusing kernel. In the spotlight modes one needs to consider the azimuth aliasing at raw data level, which can be done either by using sub-apertures [4], [22], [23] or a deramping approach [24] (see Section IV).

### B. The Curved Orbit

A hyperbolic range history, i.e., a linear track, is assumed by most spaceborne SAR image formation algorithms, but this approximation becomes less accurate the larger the integration time. For example, the TSX ST mode has an integration time of about 7 seconds, which yields the error that can be observed in Fig. 2 for the Oberpfaffenhofen scene. Such an error degrades the azimuth resolution and introduces asymmetric side lobes.

Some solutions exist in the literature that use a numerical approach to circumvent this problem, e.g. [14], [15]. Also in the present case a numerical approach has been selected, which resembles the motion compensation approach in airborne SAR systems [17]–[19]. The line-of-sight (LOS) approximation error, \( \delta r_{\text{hyp}} \), shown in Fig. 2, can be computed for a reference target in the middle of the scene, yielding

\[
\delta r_{\text{hyp}}(t; r_{\text{ref}}) = \frac{1}{2} \left[ |p_{\text{sat}}(t) - p_{\text{ref}}(t; r_{\text{ref}})| + |p_{\text{sat}}(t) - p_{\text{ref}}(t; r_{\text{ref}})| \right] - \sqrt{r_{\text{ref}}^2 + v_{\text{ref}}^2(t; r_{\text{ref}}) \cdot (t - t_0)^2},
\]  

where \( t_0 \) and \( v_{\text{ref}} \) are the zero-Doppler time and the effective velocity for the reference point, respectively. \( p_{\text{sat}} \) is the satellite position vector in Earth-Centered Earth-Fixed (ECEF) coordinates and the superscripts Tx and Rx indicate the different positions at transmission and reception, respectively, i.e., the bistatic character of the survey is accounted for. The target at the center of the beam is indicated by the vector \( p_{\text{sat}} \), where the dependence with time indicates that the reference target might change in time, as for example occurs in the SL mode [9].

Two options are described in the following in order to correct for \( \delta r_{\text{hyp}} \): one perfectly matched to the point in the middle of the beam, which performs the correction in the azimuth-frequency domain; and a second one that approximates the compensation optimally to a line at mid-range by performing the correction in the azimuth-time domain. Their residual errors are analyzed quantitatively, thus allowing the choice of the most convenient approach for the final processing flow. The first, less attractive, possibility is to correct \( \delta r_{\text{hyp}} \) both in terms of envelope and phase in the azimuth-frequency domain by using the following phase filter

\[
H^\text{freq} \left( f_s, f_r; r_{\text{ref}} \right) = \exp \left[ j \cdot \frac{4\pi}{c} \cdot \left( f_0 + f_s \right) \cdot \delta r_{\text{hyp}}(f_s, f_r; r_{\text{ref}}) \right],
\]  

where \( r_{\text{ref}} \) is the reference range, \( f_0 \) is the central frequency, the subscript OC01 refers to the first-order orbit compensation and the superscript freq refers to the correction in the azimuth-frequency domain. \( \delta r_{\text{hyp}} \) is now the error given in (6) mapped into the 2D frequency domain by computing the azimuth time of stationary phase numerically.

The correction in the Doppler domain using (7) assumes azimuth invariance. However, the spaceborne SAR geometry is azimuth-variant due to the curved orbit and Earth’s rotation. Indeed, although the term \( \delta r_{\text{hyp}} \) varies mildly with the azimuth time, the effective velocity inside (6) shows a stronger variation. The azimuth-variant geometry can be evaluated by computing the effective velocity for a target separated only in the along-track dimension and then computing the mis-match during azimuth compression. Analytically, this is given by

\[
\phi^\text{az} \left( f_s; r_0 \right) = -\frac{4\pi}{\lambda} \cdot r_0 \cdot \left( \sqrt{1 - \left( \frac{\lambda f_s}{2v_e} \right)^2} - \sqrt{1 - \left( \frac{\lambda f_s}{2v_{e,\text{ref}}} \right)^2} \right),
\]  

where \( v_e \) is the effective velocity of the target under consideration. The phase error in (8) can result in defocusing
depending on the azimuth distance to the reference point and the azimuth processed bandwidth. A numerical simulation using a TSX-like orbit was performed in order to evaluate (8) for different incidence angles and latitudes. The selected Keplerian orbit parameters are shown in Table III. Fig. 3 shows the quadratic phase error (QPE) at the edge of the azimuth processed bandwidth, which in this case corresponds to 15 cm azimuth resolution without weighting. The analyzed target is located 2 km away from the reference target in the azimuth dimension, but at the same slant-range. Both points are located at 0 m altitude over the WGS-84 ellipsoid. Note that the plot analyzes the azimuth variance assuming the residual error has already been corrected in the azimuth-frequency domain using (7). Note also that the given values vary linearly with the distance to the scene center, quadratically with the azimuth processed bandwidth, and linearly with the wavelength, i.e., C-band has a larger error than X-band for the same processed bandwidth since it requires a larger integration time. The plot corresponds to an ascending orbit configuration and right-looking geometry, but similar plots are obtained for other configurations or orbits. In the configuration of the ST mode, the resulting values will degrade the azimuth resolution and introduce interferometric phase errors. As a final comment, note that due to the spotlight acquisition geometry, it does not introduce interferometric phase errors. As a final comment, note that due to the spotlight acquisition geometry, it does not help to process the raw data in azimuth blocks to accommodate the azimuth variance.

In order to efficiently handle the azimuth variance, the second possibility is to perform the correction with a phase multiplication in the azimuth-time domain using

$$H_{OCO1}(t, f; r_{ref}) = \exp \left[ j \cdot \frac{4\pi}{\lambda} \cdot (f_0 + f_c) \cdot \delta r_{hyp}(t; r_{ref}) \right],$$

(9)

which, again, shifts the signal both in terms of envelope and phase. Effectively, eq. (9) can accommodate the azimuth variance besides correcting the non-hyperbolic term due to the small beamwidth of the antenna. This correction makes the beam-center approximation [25], i.e., the correction is only valid for the target in the middle of the beam, but given the small beamwidth of current spaceborne sensors, e.g., 0.33° for TSX, the introduced error is very small. With the correction given by (9), a pure hyperbolic phase history is forced, so that a conventional frequency domain kernel assuming a hyperbolic phase history can still be used to process the data without modifications. Note that this correction is accurate in widebandwidth terms, but only for the reference target. Therefore, for other ranges or azimuth positions the correction becomes less accurate the larger the scene size.

Since the correction given by (9) is only valid for mid range, a range-dependent (second-order) OCO might be necessary, as it is usually the case with airborne SAR systems. Due to the small magnitude of the residual errors, a phase correction suffices, which is given by [17], [19]

$$H_{OCO2}(t, r) = \exp \left[ j \cdot \frac{4\pi}{\lambda} \cdot (\delta r_{hyp}(t; r) - \delta r_{hyp}(t; r_{ref})) \right].$$

(10)

For large errors, a range interpolation might be additionally needed in order to correct the range-dependent shift. In any case, note that due to the large separation between the sensor and the scene and the small swath width, the range-dependency can be neglected in most cases (the residual phase errors at the edge of the bandwidth are smaller than 1° for the TSX ST data taken in Section V). The accuracy of the orbit compensation depends mainly on the accuracy of the orbit product, which for the TSX science orbit is about 3 cm (1σ) in periods of low solar activity [26]. Since only the relative error given by (6) is of interest for the compensation, such an accuracy suffices.

Similar as in Fig. 3, the performance of the OCO approach can be evaluated numerically. In this case though, the residual
function. The operational TSX processor uses the latter model, which is given by

$$\Delta R_{\text{tropo}}(t; r_{\text{ref}}) = \frac{Z \cdot \exp[-h(r_{\text{ref}})/H]}{\cos \theta(r_{\text{ref}}) \cdot \cos \alpha_i(t; r_{\text{ref}})} = \frac{\Delta R_{\text{tropo}}(r_{\text{ref}})}{\cos \alpha_i(t; r_{\text{ref}})}$$

(11)

where Z is a constant zenith path delay in meters, H is a reference height, h is the altitude of the target, \(\theta\) is the look incidence angle, and \(\alpha_i\), which has been introduced here in addition, is the incident azimuth angle during the formation of the synthetic aperture. The rationale for the additional term, \(1/\cos \alpha_i\), in the mapping function is sketched in Fig. 5, where the tropospheric delay at zero Doppler is projected for each time instant during the formation of the synthetic aperture. The presented model is physically valid assuming a troposphere that is cylindrical symmetric around the reference point and time invariant during the synthetic aperture, which shall be the case at decimeter scales and suffices to achieve the nominal azimuth resolution, as commented later. Note that for increasing integration times the difference between \(\alpha\) and \(\alpha_i\) also increases (cf. Fig. 5). Furthermore, for large squints close to grazing angles, more sophisticated mapping functions shall be used [33], [34]. The model is validated experimentally in Section V for a squint angle variation of \(\pm 2.2^\circ\) corresponding to the ST mode, but further investigations would be required in order to validate the model for larger integration angles. Fig. 6 plots (11) after subtracting a constant offset, as a function of the azimuth angle \(\alpha_i\) assuming the following values: \(H = 6\) km, \(Z = 2.6\) m, \(h = 629\) m and \(\theta = 35^\circ\). As it can be induced from Fig. 6, for large integration times the dependence with \(\alpha_i\) is not negligible, hence introducing defocusing and phase errors if not considered. Furthermore, the delay in absolute terms, which in the TSX case shifts the image about 6 pixels in the slant-range dimension for the maximum sampling frequency, implies a mis-match of the azimuth compression filter, introducing additional defocusing and phase errors.

Fig. 7 shows this effect over the same CR as shown in Fig. 1, where the corrections mentioned in the previous sections have been already applied. For the configuration of this data take, the troposphere introduces a quadratic error of about 50\(^\circ\) at the edge of the processed bandwidth, and the further 50\(^\circ\) occur due to the azimuth filter mis-match, resulting in the total 100\(^\circ\) that can be observed in Fig. 7, which degrades the azimuth resolution by about 10\%. The correction of the troposphere using (11) can be applied together with the first order OCO, since a bulk correction for the middle of the scene suffices. Therefore, (9) becomes

$$H_{\text{OCO1}}(t, f_0 + f_i; r_{\text{ref}}) = \exp\left[\frac{4\pi}{c} \cdot (f_0 + f_i) \cdot \left(\delta r_{\text{hyp}}(t; r_{\text{ref}}) + \Delta R_{\text{tropo}}(t; r_{\text{ref}})\right)\right].$$

(12)

Note that the performance of the tropospheric correction will depend on the accuracy of the assumed model. In any case, the tropospheric component is space variant, with gradients of about 1 cm/km [35]. It is not the purpose of the suggested correction to achieve such an accuracy in absolute terms, but
rather to reduce the relative disturbance, i.e., the curvature, to a level where it does not affect the focusing quality. In this sense, the correction should be accurate at sub-pixel level in the range dimension, which is sufficient in order to obtain a proper curvature correction of the disturbance. On the other hand, strong topography variations within the imaged swath cannot be adapted with this simple correction. Since the topography also plays an important role within the focusing kernel itself, as later discussed in Section III-C, the tropospheric correction term due to topography variations can be compensated as well.

Concerning the ionosphere, the total delay is roughly 2 cm at X-band [20], and hence the dependence with \( \alpha_i \) can be neglected. On the other hand, the effect on wide-band systems is an issue not addressed in this paper due to its negligible effect in the TSX case.

### III. Further Considerations

The three aspects mentioned in the previous sections are the main ones in order to ensure a proper focusing, but not the only ones. This section addresses three further aspects, which are: special considerations when processing using sub-aperture approaches to avoid azimuth aliasing; the consideration of the array pattern to avoid resolution loss in the focused image; and the topography dependence of the focusing kernel.

#### A. Sub-Aperture Processing

The division of the raw data in sub-apertures is a well-known approach to accommodate the Doppler variation introduced in the signal by the antenna steering, which exploits the fact that the PRF is larger than the beam bandwidth [4], [22], [23]. The recombination is performed in the time domain after the range-variant processing has been performed. When using the azimuth scaling approach during the azimuth processing, a small margin is considered due to the stretching of the azimuth signal. Finally, the computed size is zero-padded to the next power of two for efficiency purposes. Nevertheless, a further fact needs to be considered: the RCMC filter stretches also the azimuth signal in time domain for range frequencies other than \( f_0 \). This happens especially for sub-apertures with large Doppler centroids. Hence, when going back to azimuth-time domain, where the sub-apertures are recombined, time-aliasing might appear, resulting in a considerable degradation of the focused image. The amount of this stretching can be computed using the RCMC filter, resulting in an additional extension that can be even larger than the effective sub-aperture size itself. Analytically, it suffices to take the RCMC filter used, e.g., by chirp scaling [36], so that the stretching can be computed for...
each sub-aperture as

\[ \Delta t_{\text{rec}(f_{DC,i})} = \frac{1}{2\pi} \cdot \frac{\partial \phi_{\text{rec}}(f_s, f_{DC})}{\partial f_s} \bigg|_{f_s=f_{DC,i}} \]

\[ = \frac{2r_{\text{ref}}}{c} \cdot \frac{f_{DC,i}}{c} \cdot \left( \frac{\lambda}{2v_e} \right)^2 \cdot \left( 1 - \left( \frac{f_{DC,i}}{2v_e} \right)^2 \right)^{3/2} \cdot B_{rg}, \] (13)

where \( \phi_{\text{rec}} \) is the phase function of the RCMC filter, and in practice \( f_s \) has been substituted by the Doppler centroid of the given sub-aperture, \( f_{DC,i} \), and the range frequency \( f_i \) by the range bandwidth, \( B_{rg} \), in order to compute the required time extension. After converting the extension into samples, the sub-aperture shall be zero-padded with half of this amount on each side.

A further aspect that needs to be considered is the Doppler centroid variation due to the wavelength dependence. The well-known Doppler formula is given by

\[ f_{DC} = \frac{2v_s}{\lambda} \cdot \sin \alpha, \] (14)

where \( v_s \) is the satellite velocity and \( \alpha \) is the squint angle. Therefore, for a given squint angle, the Doppler centroid changes as a function of the wavelength, i.e., within the range bandwidth, a fact that needs to be considered in order to avoid that parts of the spectrum cross the adjacent PRF band. A solution was proposed in [37] based on the azimuth spectral extension, which consists in replicating the two-dimensional spectrum in azimuth and filtering out the undesired parts. By doing so the azimuth sampling is increased according to the spectral extension. In the case of the TSX satellite and due to the small relative bandwidth, it suffices to increase the PRF in order to accommodate the Doppler-centroid variation, since the skew of the spectrum at the maximum squint angle is about \( B_{\text{skew}} = 600 \text{Hz} \). Note further, that the PRF must be increased anyway to reduce the impact of the azimuth ambiguities in the TSX case [9], [11]. The skew of the spectrum imposes an additional condition when computing the size of the sub-aperture [4], which now is given by

\[ T_{\text{sub}} = \frac{\text{PRF} - B_{\text{sw}} - B_{\text{skew}}}{2[K_{\text{rot}}]^2}, \] (15)

where \( B_{\text{sw}} \) is the azimuth processed bandwidth and \( K_{\text{rot}} \) is the Doppler centroid variation introduced by the steering of the antenna. If the processing is performed in the Fourier domain, the proper approach is to perform the spectral extension as proposed in [37].

B. Array Pattern

In electronically-steered antennas, a significant amplitude modulation is introduced by the single element antenna pattern when the steering angles become comparable to the single element pattern beamwidth. Furthermore, other aspects like, e.g., the feed network or the coupling between antenna elements, can influence the final signal amplitude. Fig. 8 shows the computed normalized modulation using the TSX antenna patterns for a given ST data take. This curve has been computed by integrating for each echo the transmit-receive antenna pattern within the main lobe, i.e.,

\[ A[n] = \left( \int_{\Omega_{\text{sub}}} G_{\text{Tx}}(\alpha; n) \cdot G_{\text{Rx}}(\alpha; n) \cdot \text{d}\alpha \right)^{1/2}, \] (16)

where \( G(\alpha; n) \) is the one-way azimuth antenna pattern as a function of the azimuth angle \( \alpha \) and the discrete echo line number \( n \). After normalization, the inverse of this curve can be applied directly at raw data level to correct for the undesired modulation, similar as the recently proposed approach for the scalloping correction of TOPS data [38]. Note that, in any case, a scaling of the noise at scene edges is unavoidable. Note also that the inter-element distance of the azimuth antenna tiles (0.4 m for TSX [39]) plays an important role, since, in combination with the element antenna pattern, it results in the so-called grating lobes. Precisely at the maximum steering angles of \( \pm 2.2^\circ \) the strongest grating lobe has exactly the same gain as the main lobe. Therefore, the element antenna pattern and the grating lobes have an important impact in terms of azimuth ambiguities and must be precisely considered for the commanding of the ST mode in the TSX case [9], [11]. On the other hand, the influence of noise scaling can be partially mitigated at detected image level by proper noise subtraction as proposed in [40], but note that this approach has not been applied to the TerraSAR-X images shown in Section V.

C. Topography Dependence

For a given zero-Doppler slant-range distance \( r_0 \), the range history in a spaceborne scenario depends on the topography due to the curved orbit [5], [41], [42]. Similar as with the hyperbolic range history approximation, this effect becomes more noticeable for larger integration times. This means that, if the processing is performed with an azimuth-invariant reference height, as is usually assumed within current spaceborne imaging algorithms, azimuth defocusing might occur. Fig. 9 shows the height error that results in a phase error of \( \pi/2 \) at the edge of the processed bandwidth as a function of the azimuth resolution for the TSX-like orbit of Table III. This corresponds to a resolution loss of approximately 10% without weighting function, since the phase error is mainly quadratic with frequency. In the ST mode the topography should be accommodated within 60 m to avoid defocusing greater than
10%. For a more detailed analysis concerning the topography dependency in SAR focusing please refer to [41].

Due to the space variance of the effect, it is not trivial to include the compensation within the kernel of a Fourier-based processor. Therefore, one straightforward approach is to perform a block-wise post-focusing using an external DEM as suggested in [42], an approach based on existing topography-dependent motion compensation approaches for airborne SAR systems [43], [44]. Please note that for the results shown in Section V no post-focusing was performed, and instead the reference height was matched to that of the reference points to be analyzed.

At this point it is interesting to note that the troposphere correction also depends on the height of the target [see (11)]. Hence, the block-wise approach could also handle a residual tropospheric correction. When no external information concerning the topography is available, then autofocus approaches can be used instead to improve the focusing of the image.

IV. PROPOSED PROCESSING FLOW

Fig. 10 shows the suggested processing chain for the focusing of very high resolution spotlight SAR data, which includes the corrections mentioned in the previous sections. The block diagram reflects the generality of these corrections and hence it is not specified for any particular focusing kernel. Without loss of generality, the consideration of the higher signal bandwidth w.r.t. the PRF is presented either by using sub-apertures or with the deramping solution expounded in [24], where in the latter case no assembly of sub-apertures is needed, but the kernel must account for the changing of the azimuth sampling after the deramping operation.

The blocks highlighted in gray are the new ones proposed in this paper. First, the array pattern correction is performed at raw data level if required, i.e., in case an electronically-steered array is used. After handling the large azimuth signal bandwidth either with sub-apertures (in which case each sub-aperture needs to be zero-padded considering the stretching due to the RCMC filter, see Section III-A) or with the deramping approach presented in [24], a 2D fast Fourier transform (FFT) together with, whenever required, the azimuth spectral extension, follows. The stop-and-go correction defined in (5) can then be applied. After an inverse azimuth FFT, the first order OCO and the tropospheric correction are applied together through the azimuth-dependent phase function given by (12) to correct both the phase and the envelope of the signal for mid-range. An inverse range FFT brings the signal back to the range- and azimuth-time domain, where any Fourier-based processing kernel can now be used in order to perform the range-variant processing. This includes monochromatic kernels, like chirp scaling (CS) approaches [18], [36], the range-Doppler (RD) algorithm with secondary range compression (SRC) in the 2D frequency domain [16], [45], or algorithms based on the chirp-Z transform (CZT) [24], [46], as well as polychromatic ones, which basically leads to the \( \omega-k \) algorithm [47] and its extensions to handle the spaceborne geometry, especially in terms of the separation of the azimuth compression step from the Stolt mapping in order to ease the implementation of the Stolt interpolation itself [48] or to facilitate the motion compensation in airborne systems (extended \( \omega-k \), EOK [29]), or by computing numerically the Stolt kernel in order to accommodate more precisely the orbit curvature and the variation of the effective velocity with range, an approach named singular value decomposition (SVD)-Stolt [15]. The range-variant processing shall include a residual correction of the RCM in the range-Doppler domain via interpolation due to the range dependence of the effective velocity, a step implicitly included in the range-Doppler algorithm. The selection of the range-variant processing kernel will depend on the sensor capabilities and image quality requirements. For the most demanding scenarios it is suggested to use the OCO together with a modified SVD-Stolt [15] where the azimuth compression is removed from the Stolt mapping as in EOK [29], [48]. This approach can account for the residual SRC due to the curved orbit for targets located at ranges other than \( r_{\text{ref}} \), since the OCO is only accurate for this range, while still being able to handle the azimuth-variant geometry.

After the range-variant processing, the second order orbit compensation can take place in terms of a residual phase correction as given by (10) in order to accommodate the range variance. Again, this correction can include a delta tropospheric delay correction. The azimuth processing can take place afterwards, which can be solved with a SPECAN approach in case of using sub-apertures [18], [23] or with a conventional matched filtering, and in both cases considering the range-dependence of the effective velocity.

As a last comment, the higher the resolution, the larger the sensitivity to the topography, as shown in Fig. 9. For very high resolution spaceborne SAR imaging, this will be the limiting factor, which, as already commented, requires a space-variant correction. Such a correction could deal with other residual errors not considered by the focusing kernel, e.g., azimuth variance not corrected by the OCO, residual SRC, residual RCM, etc. However, the better the performance of the Fourier-based kernel, the simpler the post-processing will be.

V. EXPERIMENTAL RESULTS

A simulation with point targets was performed using the parameters shown in Table IV and a TSX-like orbit (see Table III). Note that the parameters have been chosen based on

Fig. 9. Maximum allowed topographic height error as a function of the azimuth resolution by allowing a maximum phase error of \( \pi/2 \) at the edge of the azimuth processed bandwidth. A TSX-like orbit has been simulated (see Table III).
Fig. 10. Proposed processing chain (new steps in gray) to process high resolution spotlight data. CS stands for chirp scaling, RD for range-Doppler, CZT for chirp-Z transform, EOK for extended ω-k, and SVD for singular value decomposition.

TABLE IV
SIMULATION PARAMETERS

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Central frequency</td>
<td>9.65 GHz</td>
</tr>
<tr>
<td>Total azimuth processed bandwidth</td>
<td>33 kHz</td>
</tr>
<tr>
<td>Azimuth resolution</td>
<td>19 cm</td>
</tr>
<tr>
<td>Chirp bandwidth</td>
<td>1.2 GHz</td>
</tr>
<tr>
<td>Ground range scene size</td>
<td>5 km</td>
</tr>
<tr>
<td>Azimuth scene size</td>
<td>5 km</td>
</tr>
<tr>
<td>Incidence angle</td>
<td>55°</td>
</tr>
<tr>
<td>Central point (longitude/latitude)</td>
<td>11.264°, 48.088°</td>
</tr>
</tbody>
</table>

A possible configuration for a next generation X-band satellite [49]. The motion of the satellite was simulated between and during transmission and reception, while the troposphere was not included. Due to the large relative bandwidth, monochromatic algorithms do not perform properly, so the EOK approach was selected, further including a residual RCMC in the form of an interpolation in the range-Doppler domain after the Stolt mapping to adapt for the variation of the effective velocity. The second order OCO is not really needed in this case and hence was not applied. Fig. 11 shows the IRFs of the nine point targets, which are located at the edges and the center of the 5 km × 5 km scene. The measured resolutions are within 0.5% accuracy while the IPEs are smaller than 1°.

Real data acquired by TSX in the staring spotlight mode have been further used to validate the proposed methodology.

Fig. 11. Contour plots of the interpolated IRFs by using the proposed processing chain with the extended ω-k (EOK). The simulation parameters appear in Table IV.

Fig. 12. Contour plots of the interpolated IRFs of five CRs of the TerraSAR-X staring spotlight image acquired over Oberpfaffenhofen, Germany. The last CR on the lower row is located at the right edge of the scene in near range. No sidelobe suppression was performed, so that the obtained resolutions are 16 cm in azimuth and 44 cm in slant-range, hence matching the theoretical values. The data were processed with the proposed processing chain and the range-Doppler (RD) algorithm.
where in this case the influence of the troposphere needs to be considered. Table II shows the main acquisition parameters, while Fig. 12 depicts the IRFs of the five CRs located in the scene acquired over Oberpfaffenhofen, Germany. During the processing all the anomalies were considered and corrected. The data were processed following the flow diagram of Fig. 10 using the RD algorithm in sub-apertures. The second order OCO was not performed and the reference point for both the first order OCO and the tropospheric correction is in the middle of the scene. Without spectral weighting, the measured values are 44.9 cm and 16.4 cm in range and azimuth, respectively, hence matching the theoretical ones with 2% accuracy. The reflectivity image is shown in Fig. 13, while Fig. 14 shows a zoom of it and compares it with the standard high-resolution spotlight (HS) mode. In the latter case, both images have been multilooked to a resolution of 1 m × 1 m, and the radiometric resolution improvement of the ST image is evident. Note also that there is a gain in the detectability of point targets (about 7 dB) in the full resolution ST data due to the increased compression gain.

Finally, in order to remark the importance of the suggested corrections, Fig. 15 shows the interpolated IRF of one of the CRs of Fig. 12 with and without the main corrections expounded in Section II, namely, the “fast-time” stop-and-go effect, the tropospheric correction, and the orbit compensation. Without these corrections the IRF is severely degraded, especially in terms of resolution, with a loss of more than 50% in both range and azimuth dimensions.

VI. CONCLUSION

Spaceborne SAR systems are unique in providing high-resolution, weather independent images of the Earth surface on a global scale. In order to increase the reliability and robustness of the information retrieval in SAR images, more stringent requirements for each specific application are defined by the users in terms of observables (e.g., time series), space diversity (e.g., interferometry, tomography), multi-channel acquisition (e.g., polarimetry, multi-frequency) and last but not least improved geometric resolution. State-of-the-art satellites like TerraSAR-X, TanDEM-X, COSMO-SkyMed as well as Radarsat-2 are providing images with a resolution in the meter regime. The next generation of SAR satellites in X-band will provide a geometric resolution in the decimeter regime.

In order to cope with the demanding requirements for improved geometric resolution, this paper has presented several critical aspects for the processing of very high resolution spaceborne data, of which the motion of the platform during the transmission/reception of the chirp signals and the troposphere are the most relevant. The correction of the former can be efficiently performed in the 2D frequency domain, while the troposphere can be corrected using a simple model for a reference target inside the scene, partly accommodating its azimuth variance. The non-hyperbolic phase history, which becomes more significant at larger integration times, has been also addressed, and a simple solution based on the motion compensation of airborne SAR systems has been proposed. This orbit compensation can also accommodate to a large extent the azimuth variance of the geometry without introducing undesired interferometric phase errors. A numerical evaluation of this approach has been presented, which confirms its validity for the processing of relatively large scenes in terms of spotlight imaging.

Further practical aspects to be considered have been also addressed, namely, the array pattern of the electronically steered antenna as well as the handling of the sub-apertures in the presence of large range bandwidths or large Dopplers. Finally, the dependence of the focusing kernel with the topography of the scene has been mentioned. Indeed, the accommodation of the topography with Fourier-based processors is challenging due to its inherent space-variant property. This issue has not been directly addressed in this paper, but ongoing work can be found in [42]. Similarly, the coupling between troposphere and topography is currently being investigated [50].

Finally, a generic processing flow has been suggested. Without entering into implementation details, the proposed focusing chain can be used with any processing kernel. The large azimuth bandwidth w.r.t. system PRF can be handled by using different strategies, be it sub-apertures or a deramping approach. The separation of the azimuth compression step allows, among other things, for a residual RCMC in the range-Doppler domain in order to accommodate the variation of the effective velocity with range, a necessary step for very high resolution spaceborne SAR imaging.

Simulated data using point targets as well as TSX ST data have been used to validate the methodology. In the latter case, the theoretical azimuth resolution of 16 cm without spectral weighting, 21 cm with the usual TSX weighting function, has been achieved after performing all the suggested corrections.

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