

A Fresh Look On Liquid-Electrolyte-Li/S-Batteries: Non-Equilibrium Thermodynamics Based, Detailed Modeling of Transport and Reactions

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Introduction: Li/S batteries

PRO:

- High energy density
- Cost-effective

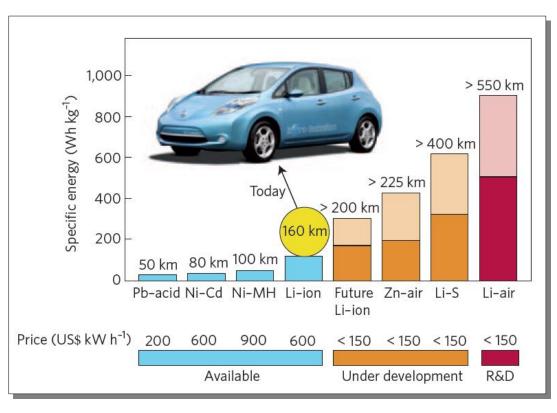
CON:

- Poor cycleability (capacity fading)
- Low cycling efficiency (voltage plateau: "infinite" charging)
- High self-discharge

"shuttle effect": transport and interface phenomena are involved

ONE WAY FORWARD:

More understanding and fundamental inside obtained via *modeling*.



(Figure from: Bruce et al., Nature Materials, 11, p. 19-29, 2012)





Motivation: "standard" 1D Li/S modeling

 Transport description: dilute solution theory expressing diffusion and migration with the Nernst-Planck equation:

$$\left. \frac{\partial C_i}{\partial t} \right|_{tr} = \left. \frac{\partial}{\partial y} \left(D_i^{eff} \left(\frac{\partial C_i}{\partial y} + \frac{zFC_i}{RT} \frac{\partial \Phi}{\partial y} \right) \right) \right.$$

(transport of chemical species only depends on the concentration of this species and the potential; transport of unshielded ions is considered)

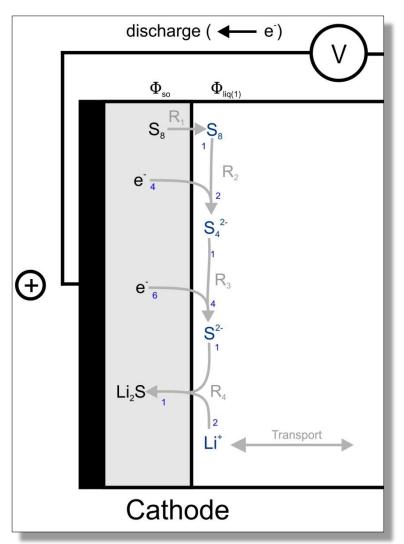
 The potential step between electrode and electrolyte is often treated as one single step, different potentials along the reaction coordinate are only crudely taken into account (via the symmetry factor alpha)

$$k_{\rm f} = k_0^{\rm f} T^{\beta} \exp \left(-\frac{E_{\rm f}^{\rm act}}{RT}\right) \exp \left(-\frac{\alpha z F}{RT} \Delta \phi\right)$$





Motivation: "standard" Li/S modeling



- Desolvation, adsorption, and electron transfer reaction are usually lumped together into one single reaction expressed by one single kinetic description:
- Here, e.g. the dissolved Li⁺, which is transported through the electrolyte, directly takes part in the precipitation reaction of Li₂S.
- Also, reactants and products "see" either the potential of the electrode, or the potential of the electrolyte.





Fresh look on 1D Li/S modelling: transport

 Transport theory based on non-equilibrium thermodynamics, following Latz & Zausch (2011):

$$\begin{vmatrix} \frac{\partial C_{Li^+}}{\partial t} \end{vmatrix}^{tr} & = & -\overrightarrow{\nabla} \left(-a \left(\frac{\partial \mu_{Li^+}}{\partial C_{Li^+}} \right) \overrightarrow{\nabla} C_{Li^+} - b \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - c \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - d \left(\frac{\partial \mu_{S_8}}{\partial C_{88}} \right) \overrightarrow{\nabla} C_{S_8} - \frac{\kappa t_{Li^+}}{Fz_{Li^+}} \overrightarrow{\nabla} \widetilde{\Phi} \right)$$

$$\frac{\partial C_{S^2-}}{\partial t} \Big|^{tr} & = & -\overrightarrow{\nabla} \left(-b \left(\frac{\partial \mu_{Li^+}}{\partial C_{Li^+}} \right) \overrightarrow{\nabla} C_{Li^+} - e \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - f \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - g \left(\frac{\partial \mu_{S_8}}{\partial C_{88}} \right) \overrightarrow{\nabla} C_{S_8} - \frac{\kappa t_{S^2-}}{Fz_{S^2-}} \overrightarrow{\nabla} \widetilde{\Phi} \right)$$

$$\frac{\partial C_{S^2-}}{\partial t} \Big|^{tr} & = & -\overrightarrow{\nabla} \left(-c \left(\frac{\partial \mu_{Li^+}}{\partial C_{Li^+}} \right) \overrightarrow{\nabla} C_{Li^+} - f \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - h \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - i \left(\frac{\partial \mu_{S_8}}{\partial C_{S_8}} \right) \overrightarrow{\nabla} C_{S_8} - \frac{\kappa t_{S^2-}}{Fz_{S^2-}} \overrightarrow{\nabla} \widetilde{\Phi} \right)$$

$$\frac{\partial C_{S_8}}{\partial t} \Big|^{tr} & = & -\overrightarrow{\nabla} \left(-d \left(\frac{\partial \mu_{Li^+}}{\partial C_{Li^+}} \right) \overrightarrow{\nabla} C_{Li^+} - g \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - i \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - z \left(\frac{\partial \mu_{S_8}}{\partial C_{S_8}} \right) \overrightarrow{\nabla} C_{S_8} \right)$$

$$\frac{\partial G_{S_8}}{\partial t} \Big|^{tr} & = & -\overrightarrow{\nabla} \left(-d \left(\frac{\partial \mu_{Li^+}}{\partial C_{Li^+}} \right) \overrightarrow{\nabla} C_{Li^+} - g \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - i \left(\frac{\partial \mu_{S^2-}}{\partial C_{S^2-}} \right) \overrightarrow{\nabla} C_{S^2-} - z \left(\frac{\partial \mu_{S_8}}{\partial C_{S_8}} \right) \overrightarrow{\nabla} C_{S_8} \right)$$

- ⇒ transport of a dissolved chemical species depends on the concentrations of all other dissolved chemical species (important for Li/S systems with potentially high polysulfide-concentrations)
- ⇒ the approach takes the shielding effects of both solvent and counterions into account (also especially important for Li/S systems)

Latz, A., Zausch, J.; "Thermodynamic consistent transport theory on Li-ion batteries", Journal of Power Sources, 196, 3296-3302, 2011





Fresh look on 1D Li/S modelling: kinetics I

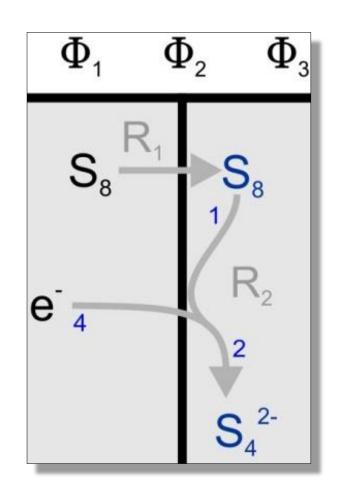
 Kinetic theory based on the law of mass action (e.g. Baird, 1999) including effects of the electric potential via the electrochemical potential, following Rubi & Kjelstrup (2003) and Latz & Zausch (2012)

Baird, J. K.; "A Generalized Statement of the Law of Mass Action", Journal of Chemical Education, 76 (8), 1146-1150, 1999

Rubi, J. M., Kjelstrup, S.; "Mesoscopic Nonequilibrium Thermodynamics Gives the Same Thermodynamic Basis to Butler-Volmer and Nernst Equations", Journal of Physical Chemistry B, 107, 13471-13477, 2003

Latz, A., Zausch, J.; "Thermodynamically derived model and simulation of intercalation for a microscopic transport model of Li-ion batteries", submitted to Electrochimica Acta, 2012

⇒ Reactants, products and intermediates "see" different potentials along the potential gradient from the electrode to the electrolyte.







Fresh look on 1D Li/S modelling: kinetics II

Using thermodynamic consistency:

from
$$K = e^{-\frac{\Delta G^0}{RT}}$$
 and $K = \frac{k_f}{k_b}$ follows $k_b = \frac{k_f}{K} = \frac{k_f}{e^{-\frac{\Delta G^0}{RT}}} = k_f e^{\frac{\Delta G^0}{RT}}$

An expression for the electrochemical potential of $\bar{\mu} = \mu^0 + \text{RT} \ln \left(\gamma e^{\frac{zF\Phi}{RT}} \frac{c}{c^0} \right)$

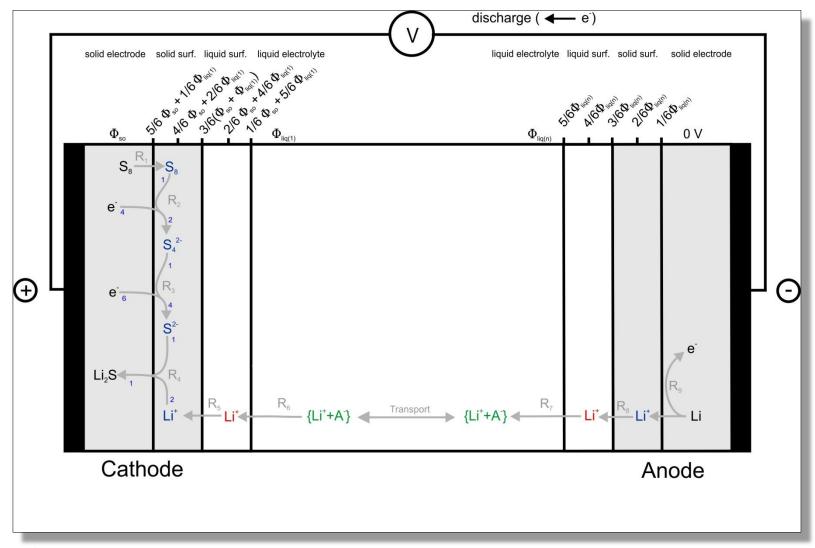
- · An expression for the electrochemical potential of
- And a six-point linear interpolation of the potential step between the electrode and the bulk electrolyte
- One can write a kinetic expression for, e.g., reaction 2 (previous slide):

$$\begin{array}{lll} R_{2} & = & \frac{k_{f}}{\gamma^{*'}} \frac{k_{f}}{e^{\frac{-4F}{RT}} \left(\frac{5}{6}\Phi_{so} + \frac{1}{6}\Phi_{liq}\right)} \left(a\left(\frac{so}{sr}S_{8}\right) \left(a_{e}^{c}\right)^{4} e^{\frac{-1\cdot4F}{RT}\Phi_{so}} - e^{\frac{\Delta G_{2}^{0}}{RT}} a\left(\frac{so}{sr}S_{4}^{2-}\right)^{2} e^{\frac{-2\cdot2F}{RT} \left(\frac{4}{6}\Phi_{so} + \frac{2}{6}\Phi_{liq}\right)}\right) \\ & = & \frac{k_{f}}{\gamma^{*'}} \left(a\left(\frac{so}{sr}S_{8}\right) \left(a_{e}^{c}\right)^{4} e^{\frac{4F}{RT} \left(\frac{1}{6}(\Phi_{liq} - \Phi_{so})\right)} - e^{\frac{\Delta G_{2}^{0}}{RT}} a\left(\frac{so}{sr}S_{4}^{2-}\right)^{2} e^{\frac{4F}{RT} \left(\frac{1}{6}(\Phi_{so} - \Phi_{liq})\right)}\right) \\ & = & \frac{k_{f}}{\gamma^{*'}} \left(a\left(\frac{so}{sr}S_{8}\right) \left(a_{e}^{c}\right)^{4} e^{\frac{4}{6}\frac{F}{RT} (\Phi_{liq} - \Phi_{so})} - e^{\frac{\Delta G_{2}^{0}}{RT}} a\left(\frac{so}{sr}S_{4}^{2-}\right)^{2} e^{\frac{4F}{RT} (\Phi_{so} - \Phi_{liq})}\right) \end{array}$$





Fresh look on Li/S modelling: Xplicit procs.







Fresh look on Li/S modelling: eq. system I

$$\begin{array}{lll} R_{1} & = & \left(\frac{k_{f}}{\gamma^{*}}\right)_{R_{1}} \left(\left(1-\frac{1}{1+e^{z_{1}^{*}\cdot\left(\left[\frac{los}{sr}S_{8}\right]-z_{1}^{b}\right)}}\right) - \frac{\left[\frac{so}{ss}S_{8}\right]}{\left[\frac{so}{sr}S_{8}\right]eq}\right) \\ R_{2} & = & \left(\frac{k_{f}}{\gamma^{*'}}\right)_{R_{2}} \left(a\left(\frac{so}{sr}S_{8}\right)\left(a_{e}^{c}\right)^{4} e^{\frac{4}{6}\frac{F}{RT}\left(\Phi_{liq}-\Phi_{so}\right)} - e^{\frac{\Delta G_{2}^{0}}{RT}}a\left(\frac{so}{sr}S_{4}^{2-}\right)^{2} e^{\frac{4}{6}\frac{F}{RT}\left(\Phi_{so}-\Phi_{liq}\right)}\right) \\ R_{3} & = & \left(\frac{k_{f}}{\gamma^{*'}}\right)_{R_{3}} \left(a\left(\frac{so}{sr}S_{4}^{2-}\right)\left(a_{e}^{c}\right)^{6} e^{\frac{4}{6}\frac{F}{RT}\left(\Phi_{liq}-\Phi_{so}\right)} - e^{\frac{\Delta G_{3}^{0}}{RT}}a\left(\frac{so}{sr}S_{2}^{2-}\right)^{4} e^{\frac{8}{6}\frac{F}{RT}\left(\Phi_{so}-\Phi_{liq}\right)}\right) \\ R_{4} & = & \left(\frac{k_{f}}{\gamma^{*}}\right)_{R_{3}} \left(a\left(\frac{so}{sr}S_{2}^{2-}\right)a\left(\frac{so}{sr}Li^{+}\right)^{2} - e^{\frac{\Delta G_{3}^{0}}{RT}}\left(1-\frac{1}{1+e^{z_{1}^{*}\cdot\left(\left[\frac{los}{sr}Li_{2}S\right]-z_{1}^{b}\right)}\right)\right) \\ R_{5} & = & \left(\frac{k_{f}}{\gamma^{*'}}\right)_{R_{5}} \left(a\left(\frac{liq}{sr}Li^{+}\right)e^{-\alpha_{R_{5}}\frac{2}{6}\frac{F}{RT}\left(\Phi_{so}-\Phi_{liq}\right)} - e^{\frac{\Delta G_{3}^{0}}{RT}}a\left(\frac{so}{sr}Li^{+}\right)e^{\left(1-\alpha_{R_{5}}\right)\frac{2}{6}\frac{F}{RT}\left(\Phi_{so}-\Phi_{liq}\right)}\right) \\ R_{6} & = & \left(\frac{k_{f}}{\gamma^{*}}\right)_{R_{5}} \left(a\left(\frac{liq}{sr}Li^{+}+A^{-}\right)\right) - e^{\frac{\Delta G_{3}^{0}}{RT}}a\left(\frac{liq}{sr}Li^{+}\right)\right) \\ R_{7} & = & \left(\frac{k_{f}}{\gamma^{*}}\right)_{R_{7}} \left(a\left(\frac{liq}{sr}Li^{+}\right) - e^{\frac{\Delta G_{7}^{0}}{RT}}a\left(\frac{liq}{sr}Li^{+} + A^{-}\right)\right)\right) \\ R_{8} & = & \left(\frac{k_{f}}{\gamma^{*'}}\right)_{R_{8}} \left(a\left(\frac{so}{sr}Li^{+}\right)e^{\alpha_{R_{8}}\frac{F}{RT}\frac{2}{6}\Phi_{liq}} - e^{\frac{\Delta G_{3}^{0}}{RT}}a\left(\frac{liq}{sr}Li^{+}\right)e^{-\left(1-\alpha_{R_{8}}\right)\frac{F}{RT}\frac{2}{6}\Phi_{liq}}\right) \\ R_{9} & = & \left(\frac{k_{f}}{\gamma^{*}}\right)_{R_{8}} \left(1-e^{\frac{\Delta G_{3}^{0}}{RT}}\left(a_{e}^{c}\right)a\left(\frac{so}{sr}Li^{+}\right)\right) \end{array}$$





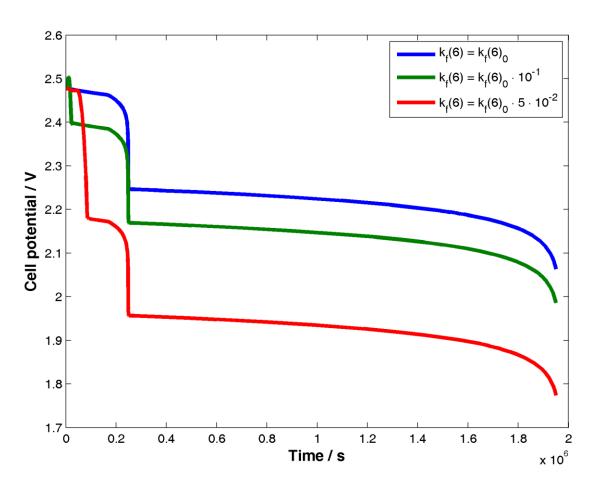
Fresh look on Li/S modelling: eq. system II

$$\begin{array}{llll} \text{electrolyte:} & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right] \right]}{\partial t} \Big|_{i} & = & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right] \right]}{\partial t} \Big|_{i}^{\text{tr}} \\ \text{cathode:} & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right] \right]}{\partial t} \Big|_{1} & = & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right] \right]}{\partial t} \Big|_{1}^{\text{tr}} - \text{R}_{6} \frac{\text{A}_{1}^{\text{reac}}}{\text{V}_{1}} \\ \text{anode:} & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{n} & = & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{n}^{\text{tr}} + \text{R}_{7} \frac{\text{A}_{1}^{\text{reac}}}{\text{V}_{n}} \\ \\ \text{cathode:} & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{ca} & = & \text{R}_{6} - \text{R}_{5} \\ & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{ca} & = & \text{R}_{6} - \text{R}_{5} \\ & \frac{\partial \left[^{\text{liq}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{ca} & = & \text{R}_{5} - 2\text{R}_{4} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{ca} & = & \text{R}_{7} + 4\text{R}_{3} \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{ca} & = & \text{R}_{8} + 2\text{R}_{2} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{2} + 2\text{R}_{4} \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{2} + 2\text{R}_{4} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{2} + 2\text{R}_{4} \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{2} + 2\text{R}_{4} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{2} + 2\text{R}_{4} \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{2} + 2\text{R}_{4} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{4} + 2\text{R}_{3} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{4} + 2\text{R}_{3} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{4} + 2\text{R}_{3} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{4} + 2\text{R}_{3} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{-} \right\} \right]}{\partial t} \Big|_{a} & = & -\text{R}_{4} + 2\text{R}_{3} \\ \\ & \frac{\partial \left[^{\text{lig}}\left\{ \text{Li}^{+} + \text{A}^{$$

- 1D continuum type model: discretized in 1D
- Resulting DAE solved with MATLAB solver ode15i



First qualitative results: dependency on k_f(6)

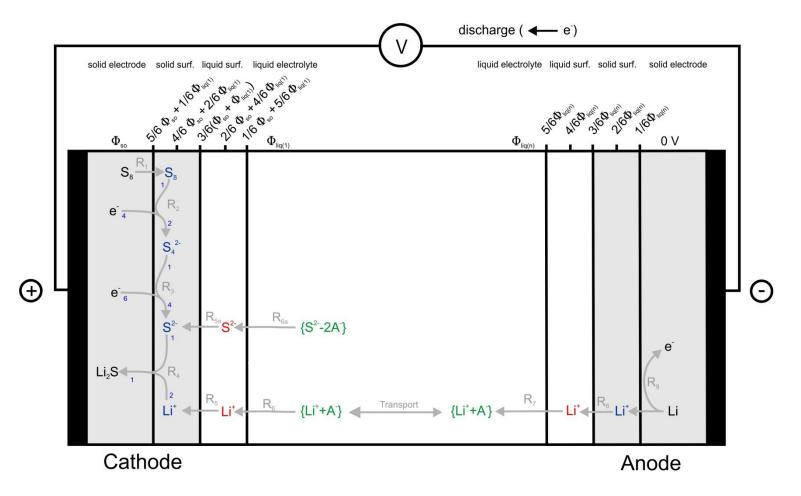


It is important to explicitly describe desolvation kinetics in the model, as desolvation kinetics are most likely more influenced by, e.g., low temperatures than charge-transfer reaction kinetics.





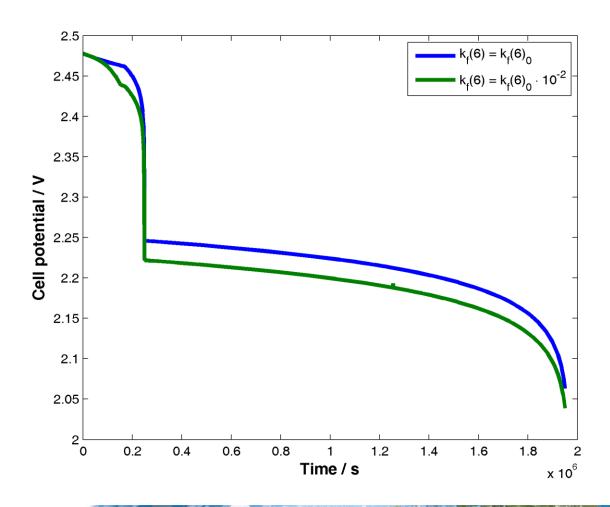
First qualitative results: dissolution of polysulfides I







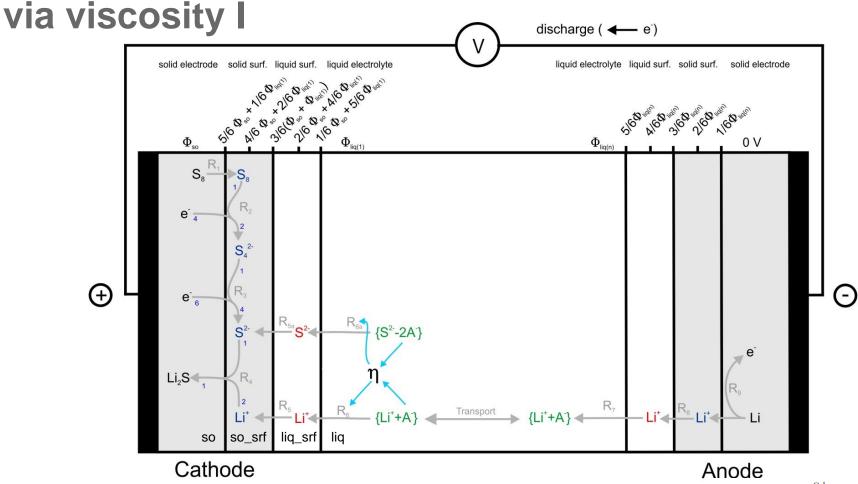
First qualitative results: dissolution of polysulfides II







First qualitative results: feedback on k_f(6)



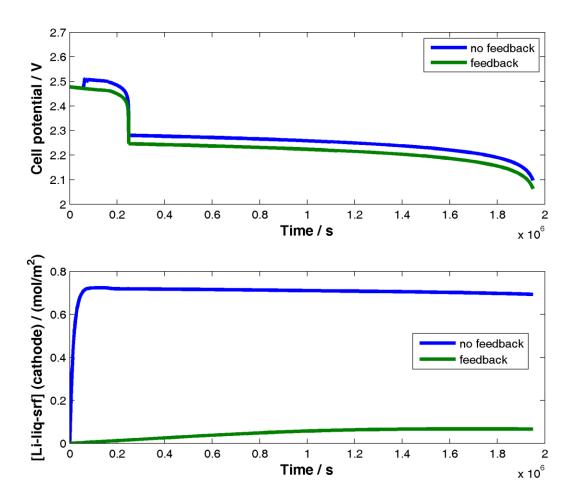
Roughly following Mahiuddin & Ismail (1982): $_{\eta} \approx _{\mathrm{A}} \mathrm{e}^{\left(\mathrm{B} \sum_{\mathrm{C_{i}}} + \mathrm{C} \left(\sum_{\mathrm{C_{i}}}\right)^{2}\right)}$ and $_{\mathrm{k_{f}}}|_{\mathrm{R}_{6}} \approx \frac{\mathrm{k_{f}^{0}}|_{\mathrm{R}_{6}}}{\eta}$

Mahiuddin, S., Ismail, K.; "Temperature and concentration dependence of viscosity of Mg(N0₃),-H₂0 systems", Canadian Journal of Chemistry 60(23), 2883-2888, 1982

60(23), 2883-2888, 1982



First qualitative results: feedback on k_f(6) via viscosity II





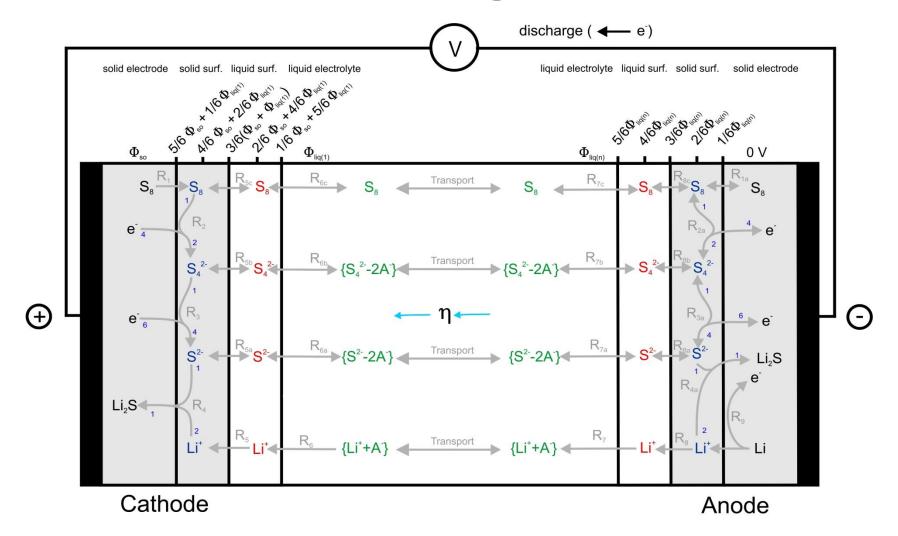


Summary:

- This is WORK IN PROGRESS!
- Three main differences to "standard" Li/S modeling:
 - 1. Transport (allowing for interactions between species, taking shielding effects into account explicitly)
 - 2. Explicit treatment of desolvation and adsorption (allowing for various explicit feedback loops)
 - 3. More detailed treatment of potential step between electrode and electrolyte
- As first results, we qualitatively showed the "effect" of point 2, but all of them bring the model closer to reality and allow for a more detailed analysis of important processes
- Adaptation and comparison of the model to experimental data and ab-initio calculations is planned, but we are always looking for additional cooperation with experimental groups!



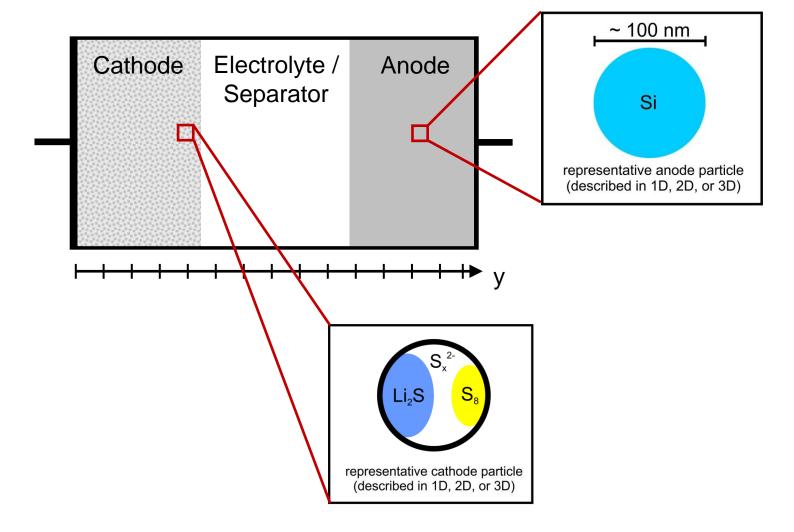
Outlook I: Shuttle effect & degradation







Outlook II: Micro- & Nanostructures











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Thank you very much for your attention

