

1           Rotation Period of Venus estimated from Venus Express  
2                           VIRTIS images and Magellan altimetry

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9   **Abstract**

The 1.02  $\mu\text{m}$  wavelength thermal emission of the night side of Venus is strongly anti-correlated to the elevation of the surface. The VIRTIS instrument on Venus Express has mapped this emission and therefore gives evidence for the orientation of Venus between 2006 and 2008. The Magellan mission provided a global altimetry data set recorded between 1990 and 1992. Comparison of these two data sets reveals a deviation in longitude indicating that the rotation of the planet is not fully described by the orientation model recommended by the IAU. This deviation is sufficiently large to affect estimates of surface emissivity from infrared imaging. A revised period of rotation of Venus of  $243.023 \pm 0.002$  days aligns the two data sets. This period of rotation agrees with pre-Magellan estimates but is significantly different from the commonly accepted value of  $243.0185 \pm 0.0001$  days estimated from Magellan radar images. It is possible that this discrepancy stems from a length of day variation with the value of  $243.023 \pm 0.002$  days representing the average of the rotation period over 16 years.

10 *Keywords:* Venus, Rotational dynamics, Infrared observations

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11 **1. Introduction**

12 Venus Express is the first spacecraft orbiting Venus since the end of the Magellan  
13 Mission in 1994. By comparing the appropriate data sets from these mission, we can

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14 estimate the rotation of the planet accumulated over 16 years and thus the mean rotation  
15 period.

16 The atmosphere of Venus is optically thick in visible and infrared wavelengths and  
17 the first tenable estimates of the slow retrograde rotation of the surface were derived  
18 from Earth based radar observations (e.g. Victor and Stevens, 1961; Pettengill et al.,  
19 1962; Goldstein and Carpenter, 1963). The early estimates were based on the spectral  
20 width of the reflected radar signal and therefore gave evidence of the apparent spin rate  
21 at the time of observation. Improved analysis of time delay and doppler shift of the  
22 radar echo soon allowed surface features to be mapped (e.g. Goldstein, 1964; Dyce et al.,  
23 1967; Shapiro, 1967). Tracking the location of such features allows a measurement of  
24 the rotation period that increases in accuracy with the time baseline, provided that the  
25 period of rotation is constant.

26 Data from several observatories gathered between 1964 and 1977 were analyzed by  
27 Shapiro et al. (1979) and the resulting rotational elements, including the rotation period  
28 of  $243.01 \pm 0.03$  d, were recommended in the first report of the IAU working group on  
29 cartographic coordinates and rotational elements of the planets and satellites (Davies  
30 et al., 1980). This recommendation for coordinate referencing was adopted for the Venera  
31 15/16 radar imaging (Barsukov et al., 1986). Updated IAU recommendations with a  
32 rotation period of 243.025 d (Davies et al., 1987) were used for all Magellan data products  
33 (Pettengill et al., 1991), including the global topographic data record GTDR version 3.2  
34 (Rappaport et al., 1999) used in this work.

35 Two later studies of Earth based radar data from the Goldstone observatory between  
36 1972 and 1982 (Slade et al., 1990) and of all available Earth based data including 1988  
37 Arecibo observations agree on a period of rotation of  $243.022 \pm 0.003$  d (Davies et al., 1992).  
38 However, the tracking of features seen repeatedly in Magellan images acquired between  
39 between August 1990 and September 1992 results in a significantly different rotation  
40 period of  $243.0185 \pm 0.0001$  d (Davies et al., 1992). The comparison of Venera 15/16  
41 images from 1983 and Magellan images in the same work again results in a longer period  
42 of rotation of  $243.023 \pm 0.001$  d. The analysis of Magellan gravity data acquired between  
43 September 1992 and September 1994 results in another value of of  $243.0200 \pm 0.0002$  d  
44 (Konopliv et al., 1999).

45 The cited rotation period determinations from surface feature tracking are based on  
46 imaging of radar surface reflectivity. By contrast, several instruments on Venus Express  
47 can track surface features by observing near infrared atmospheric windows that transmit  
48 some of the thermal emission from the surface. The observations of thermal emission used  
49 here are from the first band of the infrared channel of the visible and thermal imaging  
50 spectrometer (VIRTIS), approximately at 1.02  $\mu\text{m}$  wavelength (Coradini et al., 1998;  
51 Drossart et al., 2007). Due to the extreme greenhouse climate and thick atmosphere  
52 the surface temperature can assumed to be a function of surface elevation. Accordingly,  
53 thermal emission is strongly anticorrelated to radar altimetry (Lecacheux et al., 1993).

54 Thermal emission is also influenced by the surface emissivity, which is of geological  
55 interest as it yields information about the chemistry and mineralogy of the surface (Hel-  
56 bert et al., 2008; Hashimoto et al., 2008; Arnold et al., 2008; Mueller et al., 2008; Smrekar  
57 et al., 2010; Haus and Arnold, 2010). The surface emissivity can be derived, when ther-  
58 mal emission imaging data can be combined with sufficiently accurate radar altimetry  
59 (Hashimoto and Sugita, 2003), e.g. the Magellan global topography data record (GTDR)  
60 (Ford and Pettengill, 1992; Rappaport et al., 1999).

61 The VIRTIS data in combination with GTDR altimetry have revealed increased emis-  
62 sivity at several volcanoes (Mueller et al., 2008), which is interpreted as resulting from  
63 fresh, relatively unweathered lava flows Smrekar et al. (2010). In areas with less obvious  
64 emissivity anomalies, closer inspection shows that westward slopes have a tendency to  
65 appear brighter than predicted by GTDR altimetry. A misalignment between the coordi-  
66 nate system used and the actual orientation of the planet qualitatively fits the observed  
67 bias. Smrekar et al. (2010) applied a shift of  $-0.15^\circ$  in longitude to improve the emissivity  
68 maps from the work of Mueller et al. (2008). This shift minimizes the derived emissivity  
69 variation, however it does not strongly affect the most obvious emissivity anomalies.

70 The retrieval of surface emissivity is based on the prediction of thermal emission  
71 from altimetry. Alternatively, the VIRTIS thermal emission data can be used to estimate  
72 surface topography, but this estimate is locally biased by the unknown surface emissivity.  
73 This study is conducted using the topography derived from VIRTIS because it involves  
74 the more intuitive physical unit meter. The altimetry derived from near infrared imaging  
75 can be compared to the Magellan GTDR to test whether an orientation model with a

76 certain period of rotation aligns the two data sets.

## 77 **2. Observations**

### 78 *2.1. Venus Express VIRTIS*

79 During the acquisition of the VIRTIS data set the spacecraft Venus Express was in  
80 an elliptical orbit around Venus with the apoapsis roughly 60000 km above the southern  
81 pole and periapsis roughly at 100 to 200 km altitude (Svedhem et al., 2007). VIRTIS is  
82 a line scanning spectrometer, the image of a slit is dispersed across a rectangular array  
83 of detectors to create a line of adjacent spectra in the range between 0.2 and 5  $\mu\text{m}$ . A  
84 scanning mirror allows repeated acquisition of spectra with varying angles perpendicular  
85 to the slit to ultimately construct a three dimensional image cube with two spatial and  
86 one spectral dimension (Coradini et al., 1998). The field of view of VIRTIS corresponds  
87 to roughly one third of the Venus disc at apoapsis (Drossart et al., 2007) and extensive  
88 imaging of the surface is restricted to the southern hemisphere. Two types of observations  
89 are used for this study: mosaics of the disc of the planet from apoapsis, and images from  
90 the ascending or descending branch of the orbit with spacecraft altitudes greater than  
91 10000 km (Titov et al., 2006).

92 The thermal emission from the surface at 1.02  $\mu\text{m}$  wavelength is measured on the  
93 dark side of the planet. To reduce the impact of stray light from the bright side of  
94 Venus, the slit of the instrument is generally oriented parallel to the terminator for  
95 the apoapsis mosaics, which results in a correlation of VIRTIS image alignment with  
96 referenced longitude, i.e. longitude on average increases from the left side of the images  
97 to the right.

98 The observed angle of emission varies but its influence on radiance is virtually in-  
99 dependent from any property of the surface. The surface thermal emission radiation is  
100 intensely scattered at air molecules and cloud particles and as a result the anisotropy of  
101 the radiation field at the top of the atmosphere is dominated by the upper cloud structure  
102 (Grinspoon et al., 1993). This has additional implications for coordinate referencing, as  
103 the image of the surface thermal emission appears projected on the cloud layer between  
104 50 and 74 km altitude (Ignatiev et al., 2009). To account for this, the VIRTIS data set  
105 contains two sets of coordinates: one at the intersection of the line of sight with the

106 surface reference sphere at the mean planetary radius and one at a reference sphere 60  
 107 km higher, representing the cloud layer. VIRTIS data coordinates are referenced in ac-  
 108 cordance with the orientation model recommended by the IAU (Seidelmann et al., 2002)  
 109 which includes a period of rotation of 243.0185 d estimated from Magellan radar images  
 110 (Davies et al., 1992).

111 The VIRTIS data processing for surface imaging is described in more detail in the  
 112 work of Mueller et al. (2008). It includes corrections for stray sunlight, viewing geometry  
 113 and cloud opacity retrieved from VIRTIS band 30 at approximately 1.31  $\mu\text{m}$  wavelength.  
 114 The notable difference is that here the polynomial fit to the average relation of thermal  
 115 emission brightness temperature to Magellan topography is not used to predict local ra-  
 116 diance from topography, but instead to estimate local topography from VIRTIS radiance.

117 This estimate of surface topography from top of atmosphere thermal emission ra-  
 118 diance is somewhat facilitated by the highly reflective atmosphere, which reduces the  
 119 influence of emissivity on the radiation measured on the dark side of the planet (Mo-  
 120 roz, 2002). The hemispherically integrated reflectance  $R$  of the cloud layer is modeled  
 121 to be on average 0.82 (Hashimoto and Imamura, 2001). Thermal emission radiation is  
 122 the product of black body radiation at surface temperature  $B(T)$  and emissivity  $\varepsilon$ . The  
 123 radiation originating from the surface is reflected between atmosphere with reflectivity  $R$   
 124 and surface with albedo  $a = 1 - \varepsilon$  and the outbound hemispherically integrated radiation  
 125 flux at the top of the atmosphere  $F_{\text{toa}}$  can be approximated by

$$F_{\text{toa}} = \frac{1 - R}{1 - R(1 - \varepsilon)} \varepsilon \pi B(T) \quad (1)$$

126 (Hashimoto and Sugita, 2003). From this equation follows that a deviation of 10 %  
 127 from an emissivity of 0.85 -typical for basalt- results only in a variation in outbound  
 128 radiation of 2 to 3 % (Hashimoto and Sugita, 2003). If the surface of Venus typically has  
 129 a lower emissivity of about 0.6 owing to chemical weathering as proposed by Smrekar  
 130 et al. (2010), this effect is less pronounced. 10 % emissivity variation then corresponds  
 131 to about 5 % radiance variation.

132 A modification of Eq. 1 is used to correct for the variable cloud opacity, yielding  
 133 for each spectrum a brightness temperature which differs from the surface temperature  
 134 because of the unknown surface emissivity and extinction in the lowest part of the atmo-  
 135 sphere. This brightness temperature monotonically decreases with surface topography.

136 A second degree polynomial of all brightness temperature measurements is fitted to the  
137 corresponding GTDR altimetry values. This polynomial then allows to estimate the  
138 topography for each VIRTIS data point.

139 The connection between VIRTIS data and Magellan altimetry data is made according  
140 to the orientation model recommended by the IAU. In the following other orientation  
141 models are evaluated, but the fit is not repeated for each model. A small horizontal  
142 misalignment between the two data sets most likely only increases the scatter of Magellan  
143 data with respect to the fit but introduces no significant bias.

144 The data points are extracted from VIRTIS nightside images with an exposure du-  
145 ration of at least 3 sec. Data frames -corresponding to one exposure of the slit- with  
146 minimum angle between surface normal and direction towards the sun of less than  $95^\circ$   
147 are excluded from analysis to avoid the sunlight scattered for several degrees beyond  
148 the terminator. Spectra with emission angles of more than  $85^\circ$  have insufficient signal  
149 to noise ratio and spatial resolution and are likewise excluded. The images used were  
150 acquired between May 2006 and August 2008 with a median date of 9 January 2007.

151 Fig. 1 a) shows a map representation of the median over time of VIRTIS derived  
152 topography data. In general, the data at more equatorial latitudes and in the eastern  
153 hemisphere are more sparse due to mission constraints, here the median is less effective  
154 in removing noise (Mueller et al., 2008). For the following calculations, the individual  
155 VIRTIS measurements are used and not the projected and averaged map representation.

## 156 *2.2. Magellan GTDR*

157 The Magellan GTDR (Version 2.3) used here was reprocessed by Rappaport et al.  
158 (1999) to correct for Magellan ephemeris errors. The ephemeris corrections were ap-  
159 plied to single orbit altimeter footprints from the Magellan Altimetric and Radiometric  
160 Composite Data Record (ARCDR), which is coordinate referenced following the IAU  
161 recommendations from 1985 (Davies et al., 1987). The altimeter readings were acquired  
162 between August 1990 and August 1992 over three mapping cycles each covering approx-  
163 imately the whole surface though with data gaps. For the creation of the gridded GTDR  
164 map the readings were averaged over time and thus the median acquisition time Jan. 8  
165 1991 is taken as representative for all of the GTDR data.

166 The Magellan GTDR data has a sampling distance of about 5 km but the actual  
167 spatial resolution varies with latitude between 8 and 27 km (Ford and Pettengill, 1992).  
168 This spatial resolution is however in any case better than the spatial resolution of the  
169 VIRTIS data. Near infrared radiation transmitted through the clouds of Venus is dif-  
170 fusely scattered and mixing of radiation from different surface areas reduces the spatial  
171 resolution to  $\sim 90$  km (Hashimoto and Imamura, 2001). The GTDR data is here used  
172 in comparison with VIRTIS data, which requires that the GTDR spatial resolution be  
173 reduced to that of VIRTIS. To this end the GTDR is smoothed with a moving weighted  
174 average following the algorithm described in Mueller et al. (2008). A projection of this  
175 smoothed GTDR data set is presented in Fig. 1 b).

### 176 3. Comparison of the two data sets

177 We have visually compared the two maps in Fig. 1 and conclude that the Magellan  
178 altimetry appears systematically offset to the west relative to the Venus Express map  
179 when following the IAU recommendations. This offset is present at all longitudes and  
180 becomes much less obvious towards the south pole. The offset therefore has the general  
181 characteristics of a rotation around the planetary spin axis.

182 The method of least squares provides a straightforward way to estimate both the offset  
183 in longitude and error of the offset from the  $\chi^2$  statistic described in section 3.1 (e.g.  
184 Press et al., 1992). This approach, however, does not easily account for systematic errors,  
185 e.g. in the VIRTIS coordinate referencing, or non-random errors that are correlated with  
186 location such as those arising from the unknown surface emissivity.

187 Nevertheless, we first proceed with the least squares method to find the offset and to  
188 investigate whether the vertical error of VIRTIS derived altimetry allows for a significant  
189 estimate of the offset between the data sets. Then the error of the offset is again estimated  
190 by using a 'bootstrap' approach (e.g. Press et al., 1992) and by dividing the VIRTIS data  
191 set into subsets and finding the offset for each. The latter two methods are more likely  
192 to provide an more realistic estimate of the certainty of the result but systematic errors  
193 can also additionally impact the accuracy of the result.

194 The problem of accuracy is approached from another direction by testing the effects of  
195 the most probable sources of systematic errors, i.e. surface emissivity variation, VIRTIS

196 coordinate referencing and an error in the spin axis direction. We note that these sys-  
 197 tematic errors not only can impact the accuracy, but also likely increase the uncertainty  
 198 estimated through the subset and 'bootstrap' methods.

### 199 3.1. Differences between VIRTIS and GTDR

200 To estimate the offset, the minimum of the  $\chi^2$  statistic of the  $n \sim 10^7$  VIRTIS derived  
 201 altimetry values  $Z_i(x_i)$  with respect to the corresponding Magellan altimetry  $Z_{\text{MGN}}(x'_i)$   
 202 is found:

$$\chi^2 = \sum_{i=1}^n \left[ \frac{Z_i(x_i) - Z_{\text{MGN}}(x'_i)}{\sigma_{\text{VEX}}} \right]^2 \quad (2)$$

203 where  $x_i$  are the coordinates of VIRTIS data,  $x'_i$  are coordinate transformation of  $x_i$   
 204 including the variable offset, and  $\sigma_{\text{VEX}}$  is the error of VIRTIS derived altimetry. The  
 205 error is expected to vary with pixel position on the detector, instrumental temperature,  
 206 acquisition exposure duration, observation geometry, cloud opacity and space weather.  
 207 For convenience we adopt a constant value for all data points.

208 The minimum is found by calculating  $\chi^2$  for various offsets corresponding to rotations  
 209 of the planetary surface. For models with one parameter, the limits of confidence around  
 210 this minimum are equivalent to an increase in  $\chi^2$  by one (Press et al., 1992), provided that  
 211 the VIRTIS deviates from the Magellan data with a normal distribution with variance  
 212  $\sigma_{\text{VEX}}^2$  and has no error in  $x_i$ . When following the IAU recommendations, i.e. assuming  
 213 no offset  $x_i = x'_i$ , and further assuming  $\chi^2 = n - 1$ , Eq. 2 leads to  $\sigma_{\text{VEX}} \simeq 2500\text{m}$ , which  
 214 can be adopted as data error for the calculation of limits of confidence (Press et al.,  
 215 1992).

216 Fig. 2 shows a histogram of the differences between VIRTIS and GTDR altimetry  
 217 with  $x_i = x'_i$ . The median of the distribution is at  $\sim 60$  m and the 16th and 84th  
 218 percentile are found 500 and 530 m difference from this value. This is not consistent  
 219 with the above assumption of a normal distribution with a standard deviation of 2500  
 220 m. An overlay of a fitted gaussian with center at 58 m and standard deviation of 494  
 221 m shows that outlying differences are systematically more frequent than expected in a  
 222 normal distribution that describes the central 95 percentiles well. This may be due to  
 223 a non-gaussian distribution or a varying error  $\sigma_{\text{VEX}}$ . The formal limits of confidence  
 224 derived from the assumption of normally distributed error described by a constant  $\sigma_{\text{VEX}}$



225 might therefore be spurious, which is exacerbated by the possibility of errors in the  
226 coordinate referencing of VIRTIS.

227     Aside from the possible errors in the referencing, a local bias in the derived altimetry  
228 can also influence the  $\chi^2$  statistic. If the bias is correlated with the slope, i.e. the partial  
229 derivative of the topography with the coordinate shift, it may appear similar to the bias  
230 introduced by an horizontal offset between the two data sets and thus may introduce a  
231 bias in the position of the minimum  $\chi^2$ . The map in Fig. 1 a) represents the median over  
232 time and therefore gives evidence of any local biases. Various systematic differences are  
233 obvious between the map representations of the data sets, which can not be explained  
234 by random errors or offsets in coordinates. Some of these correspond to a bias in derived  
235 topography of up to 600 m and have been interpreted to be caused by surface emissivity  
236 variation (Helbert et al., 2008; Mueller et al., 2008; Smrekar et al., 2010).

237     This leads to the question, whether such surface emissivity variations are more influ-  
238 ential than the biases introduced by coordinate offsets. For a qualitative evaluation of  
239 this problem, two subsets of the VIRTIS data set are selected by the criterion, that the  
240 data are acquired at locations where the median over time deviates from the Magellan  
241 topography for more than 300 m. The frequency distribution of deviations from the  
242 GTDR are also plotted in Fig. 2 a), where the red graphs corresponds to the locations  
243 with a bias at least 300 m lower than Magellan and the blue graphs correspond to a bias  
244 of at least 300 m above the GTDR. The data within subsets exceed the criterion due to  
245 random noise plus any combination of a bias in VIRTIS altimetry and horizontal offset  
246 to the GTDR.

247     In Fig. 2 b) the relative frequency distributions of the partial derivatives of topogra-  
248 phy with respect to longitude are plotted for the whole data set and the two subsets. The  
249 subset with a bias towards too low values is offset towards higher frequencies at positive  
250 topography derivatives -i.e. western slopes- while the subset with a bias to higher values  
251 is offset towards eastern slopes, when compared to the total data set. If assuming an  
252 offset of -0.3 deg in longitude and then reselecting the subsets, the offsets are reduced  
253 (Fig. 2). This is consistent with the effect of a coordinate offset in longitude between 0  
254 and -0.3°.

255     This may also be due to a correlation of both high emissivity with western slopes

256 and low emissivity with eastern slopes, however it seems unlikely that any coincidental  
 257 emissivity correlation with slope would produce such a symmetrical effect both in high  
 258 and low emissivity values. The subset with bias to too high values is now more frequent  
 259 on the steep western slopes, which indicates that the offset of -0.3 deg may be to extreme.  
 260 To find the best offset, the minimum of  $\chi^2$  is found with respect to the transformation  
 261  $x \rightarrow x'$  that aligns the two data sets.

### 262 3.2. *Aligning VIRTIS and GTDR*

263 To connect the two data sets separated in time by 16 years, the coordinates of VIRTIS  
 264 data are traced back through time using the to be tested set of rotational parameters  
 265 prescribing the orientation of Venus. The transformation is

$$x' = M^T A R A^T V x \quad (3)$$

266 where  $x'$  and  $x$  are VIRTIS data barycentric cartesian coordinates in the frame of  
 267 GTDR and VIRTIS coordinate referencing.  $V$  and  $M$  are the transformation matrices  
 268 from Venus coordinates to Earth mean equatorial coordinates at the epoch of J2000  
 269 according to coordinate systems used by VIRTIS (Seidelmann et al., 2002) and the GTDR  
 270 (Davies et al., 1987), respectively.  $A$  is constructed in the same way as  $V$  and  $M$  but  
 271 represents the set of rotational parameters to be evaluated.  $V$  and  $A$  are calculated for the  
 272 Julian day of VIRTIS observations and  $M$  for 8 January 1991, the median data acquisition  
 273 time of the GTDR.  $R$  is a rotation around the pole axis with an angle determined by the  
 274 number of Julian days between the VIRTIS data acquisition time and 8 January 1991 and  
 275 the angular velocity of the orientation model under evaluation. The smoothed GTDR  
 276 topography data corresponding to the VIRTIS data at  $x$  are then found through cubic  
 277 spline interpolation of 16 GTDR points neighboring  $x'$ . To ensure that all estimates  
 278 are based on the same subset of VIRTIS and GTDR data, only those VIRTIS data are  
 279 used, which are not within 100 km distance of missing GTDR data for all the orientation  
 280 models directly compared with each other.

### 281 3.3. *Offset in Longitude*

282 The first test aims to estimate the offset in longitude between the GTDR and VIR-  
 283 TIS data with the orientation model currently recommended by the IAU (Davies et al.,

1992; Seidelmann et al., 2002) and used for VIRTIS coordinate referencing. Offsets in longitude ranging from  $-0.3^\circ$  to  $0.08^\circ$  are added to the VIRTIS data coordinates. The minimum of  $\chi^2$  is located at a longitude offset of  $-0.165^\circ$ . Visual comparison of the map representations of the data sets confirms that this offsets appears to align VIRTIS and GTDR data.

The sum of the squares of all altimetry deviations between GTDR and VIRTIS at the minimum of  $\chi^2$  is  $\sim 1.1 \cdot 10^{14} \text{m}^2$ , with  $n=17\,381\,826$  this corresponds to a root mean square deviation (RMSD) of 2506 m. If no independent error estimate is available, the minimum of  $\sigma_{\text{VEX}} = \sqrt{\chi^2/(n-1)}$  -approximately equal to the RMSD- can be used to normalize  $\chi^2$  for an estimate of the limits of confidence of the fit (Press et al., 1992). The error estimated from the RMSD appears exaggerated in comparison with the central 95 percentiles of the deviations (Fig. 2). Adopting the value of 2506 m as error,  $\chi^2$  increases by one at a distance of  $0.005^\circ$  longitude from the minimum. This is a measure of the  $1\sigma$  confidence interval, which however is only then valid if there are only vertical and normally distributed errors in the VIRTIS data.

The large difference between the deviations in the central 95 percentiles (Fig. 2) and the RMSD hints towards the existence of extreme outliers. In order to estimate the robustness of the longitude offset estimate, additional data processing steps are introduced to reduce extreme errors. VIRTIS data calibration by default searches for single pixel spikes and saturated pixels and these are not included in this analysis. In addition to this, VIRTIS derived altimetry deviating more than 7500 m from the GTDR is not considered for the new data processing. Instrumental stray light and changes in the instrumental spectral transfer function from thermal stresses can introduce a bias that is approximately constant for each VIRTIS image. This bias is approximated by the average of the difference between VIRTIS and GTDR and subtracted from the measurements. The bias is typically around 300 m, but exceeds 2500 m in two images. No adjustments are made to the coordinates and therefore the subtraction of these biases will partly remove differences introduced by any deviation in the coordinates. The resulting  $\chi^2$  is therefore biased towards confirming the IAU coordinate referencing recommendations. The resulting minimum  $\chi^2$  is found at  $-0.1541 \pm 0.0010^\circ$  longitude relative to the IAU recommendations. The smaller formal confidence interval follows from the smaller RMSD

Orbits	Offset /°
25 - 93	-0.143
94 - 141	-0.170
141 - 316	-0.269
317 - 334	-0.113
334 - 358	-0.305
359 - 370	-0.127
370 - 388	-0.091
388 - 588	-0.150
588 - 603	-0.189

Table 1: Longitude offsets derived from each of nine subsets. VIRTIS images are assigned to subsets according to data acquisition time so that each subset contains nearly the same amount of data. Venus Express orbital period is 24 h. Orbit insertion was on 4 April 2006

315 of 569 m achieved with the additional data processing steps.

316 For the formal confidence interval it is assumed that the error of every data point is  
317 independent. For VIRTIS referencing errors, the error is not independent for all data  
318 points in the same image. In this case, an adaption of the "bootstrap" Monte Carlo  
319 simulation of the confidence interval described by Press et al. (1992) may give a better  
320 estimate. Sample sets of images are drawn randomly with replacement to create a number  
321 of sample data sets with the same number of images as the whole data set. Each sample  
322 set therefore omits some images and contains images twice or more often. The standard  
323 deviation of the position of the minimum  $\chi^2$  over roughly 1000 of these sample sets is  
324  $0.01^\circ$ , a magnitude larger than the formal confidence interval of the  $\chi^2$  statistic but still  
325 an order of magnitude smaller than the observed offset.

326 Dividing the data set into similarly sized subsets based on time of data acquisition  
327 may provide insight into the certainty of the observed offset and additionally allows to  
328 determine if the offset varies significantly with time. The resulting fitted offsets for nine  
329 subsets are plotted in Fig. 3 with confidence intervals derived through the 'bootstrap'  
330 method. The offsets are not consistent with each other but can not be very plausibly  
331 attributed to a real movement of the planet. A more likely explanation for the variance

332 of the fitted offset are systematic errors. For the certainty of the observed offset the  
333 standard deviation of the offset in the nine subsets of  $0.071^\circ$  is adopted. This confidence  
334 interval corresponds to an increase of the  $\chi^2$  statistic by 2836.

335 This high  $\chi^2$  increase over the confidence interval estimated from the subset method  
336 indicates that the vertical random error of the VIRTIS derived altimetry only plays a  
337 very minor role for the uncertainty of the offset. This means the  $\chi^2$  statistic is not  
338 meaningful for the significance of our result. In the following we will evaluate models on  
339 their RMSD, which may be more intuitive. The error of  $0.071^\circ$  longitude derived from  
340 the subset method corresponds to an increase of the RMSD ( $\Delta$ RMSD) of 0.046 m.

341 While the offset is supported by all of the the subsets, the question remains whether  
342 any systematic error affects all of the data to consistently produce a similar offset. In  
343 the following several possible systematic errors are investigated.

#### 344 *3.4. Influence of surface emissivity*

345 Surface thermal emission anomalies thought to be unweathered lava flows at the flanks  
346 of volcanic structures (Helbert et al., 2008; Mueller et al., 2008; Smrekar et al., 2010)  
347 introduce a bias of up to 600 m in the derived altimetry. The three strongest anomalies  
348 are at Juturna and Cakilaca fluctūs on the southern flank of the Lada Terra rise (Helbert  
349 et al., 2008), at the summit and northeastern flank of Idunn mons in Imdr regio and at  
350 the western flank of Shiwanokia corona (Smrekar et al., 2010).

351 As these anomalies are on the flanks of topographic features the position of the  
352 topographic feature may appear offset in the near infrared altimetry. The anomalies are  
353 found in various directions relative to the topographic features but overall the  $\chi^2$  statistic  
354 might be biased if the distribution of emissivity anomalies with respect to slope direction  
355 is by coincidence not symmetrical (Fig. 2 b and c).

356 To better understand the possible influence of surface emissivity variation, data within  
357 four areas containing the strongest anomalies with excess thermal emission are removed  
358 from the data set. The areas are Imdr regio (bounded by  $50^\circ$ S,  $40^\circ$ S,  $210^\circ$ E and  $220^\circ$ E),  
359 Themis regio ( $50^\circ$ S,  $30^\circ$ S,  $270^\circ$ E,  $300^\circ$ W), Dione regio ( $40^\circ$ S,  $30^\circ$ S,  $320^\circ$ E,  $330^\circ$ E) and  
360 Lada Terra together with the south-eastern rim of the Lavinia basin ( $80^\circ$ S,  $40^\circ$ S,  $340^\circ$ E,  
361  $20^\circ$ E). These areas encompass all of the volcanic hotspot centers identified in Magellan

362 gravity data of the southern hemisphere (Smrekar, 1994; Stofan et al., 1995), and are  
363 thus areas with a high likelihood of ongoing active volcanism.

364 The data set excluding these areas has approximately 20 % less data points. The  
365 minimum of the  $\chi^2$  statistic is at  $-0.1291^\circ$  longitude relative to IAU recommendations  
366 with a formal confidence interval of  $0.0012^\circ$ . The 20 % wider confidence interval compared  
367 to the full data set may be due to fewer data and much less topographic features (see  
368 Fig. 1). The standard deviation of the fitted longitude offset in nine subsets is  $0.066^\circ$ .  
369 Compared to the  $0.071^\circ$  of the full data set, this indicates that the systematic errors are  
370 not efficiently removed with the exclusion of the four areas.

371 We are not aware of any effects possibly causing a systematic bias of surface thermal  
372 emission on the eastern or western slope of topographic highs. Orographic effects of  
373 surface temperature or weathering might play a role but aeolian features indicate that  
374 the prevailing surface winds are in North South direction (Greeley et al., 1995).

375 The Magellan radiothermal emission measurements at 12.9 cm wavelength have re-  
376 vealed anomalous emissivity at high altitudes above 4 to 5 km (Pettengill et al., 1992).  
377 This anomaly is thought to be caused by a highly dielectric mineral that is only stable  
378 below a certain temperature, possibly influenced by atmospheric composition (e.g. Fegley  
379 et al., 1997; Wood, 1997). The altitude of this 'snowline' varies with latitude but no bias  
380 with direction of topographic slope is reported, even when the 'snowline' was used as  
381 control on stereo image digital elevation models (Arvidson et al., 1994; Howington-Kraus  
382 et al., 2002). These radiothermal emissivity anomalies are however not relevant for the  
383 VIRTIS derived infrared emissivity data. VIRTIS coverage is restricted to parts of the  
384 southern hemisphere with negligible surface area above 4 km altitude.

385 In conclusion, the most strongest thermal emission anomalies influence the fit of the  
386 offset only by  $0.025^\circ$ . Less obvious thermal emission anomalies can further influence the  
387 fit, however it is unlikely that such more subtle anomalies could influence the fit more  
388 by coincidence. The existence of a systematic emissivity difference between eastern and  
389 western flanks of topographic highs appears unlikely.

### 390 3.5. *VIRTIS coordinate referencing*

391 A simple explanation for the observed offset in longitude would be a systematic error  
392 in the coordinate referencing of the data sets such as from misalignment of the instrument

393 or refraction in the atmosphere. The typical viewing geometry of VIRTIS nightside  
394 observations from above the south pole with the slit oriented parallel to the terminator  
395 means that the planetary coordinates are correlated with the instrument and spacecraft  
396 reference frame. The average difference of referenced longitude between neighboring  
397 pixels is  $0.24^\circ/\text{pixel}$  in the direction of the slit (i.e. the spacecraft y-axis as defined in  
398 (Titov et al., 2006)) and  $0.01^\circ/\text{pixel}$  perpendicular to the slit (i.e. the spacecraft x-axis  
399 as defined in (Titov et al., 2006)). Star and limb observations with VIRTIS exclude a  
400 misalignment greater than 0.4 pixel in the slit direction and 1.3 pixel perpendicular to  
401 the slit, corresponding to an error in longitude referencing of  $0.1^\circ$  in the worst case.

402 A misalignment of 0.1 pixel, i.e. 0.25 mrad, in either direction is simulated by in-  
403 terpolating between the referenced coordinates of neighboring pixels. The fitted offset  
404 increases with misalignment of the instrument along the y-axis of the spacecraft, and  
405 decreases with misalignment along the x-axis. The modeled misalignment of 0.1 pixel  
406 along the y-axis results in a fitted longitude offset of  $0.0164^\circ$ , and along the x-axis in an  
407 offset of  $0.0007^\circ$ .

408 This offset from modeled misalignment is smaller than expected from the average  
409 differences of longitude between neighboring pixels. This might be due to the weighting  
410 introduced by the distribution of topographical features. Topographical features are  
411 scarce at lower latitudes where the effect of a misalignment for longitude referencing is  
412 greater. The maximally possible longitude bias of  $4 \cdot 0.0164^\circ + 13 \cdot 0.0007^\circ = 0.075^\circ$  from a  
413 biased instrument misalignment is similar to the observed variation of the longitude offset  
414 over nine data subsets with a standard deviation of  $0.071^\circ$ . The possible misalignment  
415 may therefore have a significant effect on the observed offset, although it can not explain  
416 the full offset of  $0.154^\circ$ .

417 To account for the light scattering atmosphere, VIRTIS data is referenced to a sphere  
418 with radius 6112 km representing the cloud layer of Venus, equivalent to 60 km altitude  
419 above the mean planetary radius. The altitude of optical depth of one is  $74 \pm 1$  km  
420 at low latitudes on the dayside, and decreases below  $-50^\circ$  latitude to a variable altitude  
421 with an observed minimum of 63 km at the south pole (Ignatiev et al., 2009). The cloud  
422 base was found by nephelometer and particle counter experiments on descent probes and  
423 is expected between 45 and 50 km altitude (Ragent et al., 1985). The reference altitude

424 therefore lies roughly in the middle of the clouds. Nevertheless, a different altitude may  
 425 lead to a more appropriate referencing of the surface image projected on the clouds.

426 The difference  $h$  of this best reference sphere to the altitude of 60 km then causes a  
 427 local distortion in the coordinate referencing of VIRTIS data. The referenced and the  
 428 most appropriate coordinates are both on a line perpendicular to the limb and the angle  
 429  $\alpha$  between them as seen from the instrument is approximately

$$\alpha = \frac{h}{s} \sin \theta \quad (4)$$

430 where  $s$  is the slant distance between spacecraft and reference sphere and  $\theta$  is the  
 431 emission angle. This allows us to calculate the bias in longitude referencing introduced  
 432 by an inappropriate cloud altitude by linear interpolation of the longitudes of VIRTIS  
 433 geometry data to the lines of sight with correct coordinates. Assuming a cloud altitude  
 434 error  $h$  of 14 km, the average bias in longitude referencing is  $-0.004^\circ$ . Assuming  $h=-10$   
 435 km the average deviation is  $0.004^\circ$ , with minimum value of  $-0.49^\circ$ , maximum value of  
 436  $0.46^\circ$  and a standard deviation of  $0.04^\circ$ . The bias in latitude corresponding to  $h$  of 14 km  
 437 is  $0.09^\circ$ . This small dependence of longitude referencing on the reference sphere radius  
 438 is due to the typical viewing geometry from above the south pole.

439 This estimate of coordinate bias is verified by referencing the data to a spheres with  
 440 6102 km and 6122 km radius, corresponding to the lower cloud and upper cloud at 50  
 441 km and 70 km altitude. The resulting fitted offsets are  $-0.157^\circ$  and  $-0.152^\circ$ , respectively,  
 442 both within  $0.003^\circ$  of the longitude offset of  $-0.154^\circ$  at 60 km altitude. The altitude of  
 443 the reference sphere within the cloud layer does therefore not significantly affect the fit  
 444 of the longitude offset.

### 445 3.6. Rotation axis direction

446 A deviation in the parameters describing the direction of the rotation axis can appear  
 447 similar to an offset in longitude. To investigate this effect for the VIRTIS data set, the  
 448 rotation axis parameters derived by Davies et al. (1992) and recommended by the IAU  
 449 (Seidelmann et al., 2002) are varied by  $2\sigma$  and the best fitting longitude offset aligning  
 450 the VIRTIS and Magellan altimetry data sets is found by minimizing the RMSD. The  
 451 results are presented in Tab. 2. The fitted longitude offset is sensitive to right ascension,



Declination	Fit at right ascension:		
	272.72°	272.76°	272.80°
67.14°	-0.168°	-0.156°	-0.145°
	0.183 m	0.189 m	0.212 m
67.16°	-0.166°	-0.154°	-0.142°
	-0.003 m	0.000 m	0.020 m
67.18°	-0.164°	-0.152°	-0.140°
	-0.132 m	-0.132 m	-0.114 m

Table 2: Influence of variation of rotation axis on fitted offset in longitude and the corresponding change of the minimum root mean square deviation between the data sets, relative to the value of 569.263m for the IAU orientation model with longitude offset. The rotation axis right ascension (RA) and declination (DE) is varied around the values recommended by the IAU (RA = 272.76°, DE = 67.16°) for  $2\sigma$  of the stated error in the work of Davies et al. (1992).

452 however a deviation of more than  $2\sigma$  from the values recommended by the IAU is  
453 required to explain the offset in longitude. Assuming that the trend is linear, a deviation  
454 of about  $20\sigma$  could explain the offset in longitude.

455 The minimum  $\chi^2$  hint towards a higher spin axis declination than recommended by  
456 the IAU. It is desirable to find the minimum RMSD in the parameter space of pole right  
457 ascension, declination and longitude offset. However, the possibly large systematic errors  
458 in VIRTIS latitude referencing and the uneven distribution of data over the planet reduce  
459 confidence in the accuracy of the fit for all parameters. We did not attempt this fit due  
460 to the large computational cost compared to the doubtful outcome.

461 The fit of the longitude offset is not significantly affected by plausible errors in the  
462 position of the pole recommended by the IAU. This spin axis direction is confirmed by  
463 independent estimates based on Earth based radar observations and Magellan gravity  
464 observations, which however led to significantly different periods of rotation (Davies  
465 et al., 1992; Konopliv et al., 1999).

### 466 3.7. Rotation period

467 If this offset in longitude is due to a deviation in rotation period, the sign indicates a  
468 slower retrograde rotation than recommended by the IAU. The difference of median data

469 acquisition times is 5845 Julian days. The difference of angular velocity corresponding  
470 to an offset in longitude of  $-0.154 \pm 0.071^\circ$  is  $-2.6 \cdot 10^{-5} \pm 1.2 \cdot 10^{-5}$  °/day. The angular  
471 velocity of the orientation model is  $1.4813688$  °/day, adding the offset leads to a period  
472 of rotation of  $243.0228 \pm 0.0020$  days.

473 We can not confirm or reject this period of rotation from observation of the evolution  
474 of the longitude offset. If the true period of rotation of Venus is 243.023 days, the offset  
475 in longitude occurring over the 600 days of VIRTIS observations is approximately  $0.02^\circ$ ,  
476 which is small compared to the scatter of the longitude offsets of the 9 subsets of  $0.071^\circ$ .  
477 The offsets of the subsets do not appear to have a significant trend (Fig. 3).

478 The RMSD of the orientation model with a revised period of rotation of 243.023 days  
479 is 0.001 m higher than the orientation model with a constant offset of  $-0.154^\circ$  longitude  
480 (see table 3). This indicates a worse fit, which is however not significant compared to the  
481  $\Delta$ RMSD adopted as limit of confidence. In other words, the observed offset is consistent  
482 with a revised period of rotation of 243.0228 days, but we can not show that the offset  
483 changes accordingly over the 2 years of VIRTIS observations. There is however a reason  
484 why the revised period of rotation is more plausible than the constant offset as detailed  
485 in the next section.

### 486 *3.8. Other sets of rotational parameters*

487 The period of rotation of  $243.0228 \pm 0.0020$ d is consistent with the estimates from  
488 ground based observations by Slade et al. (1990), Shapiro et al. (1990) and reported  
489 by Davies et al. (1992), as well as to the value derived from comparison of Venera  
490 15/16 and Magellan radar images by Davies et al. (1992). It is not consistent with the  
491 estimates based on Magellan SAR data alone (Davies et al., 1992) or Magellan gravity  
492 data Konopliv et al. (1999).

493 The  $\chi^2$  values for several models are listed in table 3 in order of increasing  $\chi^2$ .  
494 Appended to the table are two hybrid models based the previous tests, derived from  
495 the orientation model recommended by the IAU (Davies et al., 1992; Seidelmann et al.,  
496 2002). The first hybrid model adds a constant longitude offset of  $-0.154^\circ$  and the second  
497 uses a revised period of rotation of 243.023d, matched to introduce an similar offset at  
498 the median VIRTIS data acquisition time.

499 The model with the constant offset provides the reference RMSD of 569.262 m at  
500 the offset of  $-0.154^\circ$  longitude. A measure of the significance of  $\Delta$ RMSD can be derived  
501 from the deviation of the fitted shifts of nine subsets of  $0.071^\circ$ , which corresponds to an  
502 increase in RMSD of 0.046. This confidence limit estimate however assumes that the  
503 spin axis is well known. If the spin axis direction is varied by  $2\sigma$  in both right ascension  
504 and declination the minimum RMSD changes by as much as 0.212 m.

505 The best fit is achieved with the set derived from Goldstone ground based radar  
506 observations (Slade et al., 1990). Comparison with table 2 indicates that much of the  
507  $\Delta$ RMSD can be attributed spin axis declination, which deviates significantly from other  
508 estimates. The second best fit comes from the orientation model based on all available  
509 Earth based data from 1972 to 1988 credited to G.H. Pettengill in the work of Davies  
510 et al. (1992). This model is within its stated error consistent with IAU recommendations  
511 for the spin axis (Seidelmann et al., 2002) and a revised rotation period of 243.023 days,  
512 as derived from the fitted offset in longitude between VIRTIS and Magellan data. The  
513 spin axis is furthermore consistent with the Magellan gravity model (Konopliv et al.,  
514 1999).

515 Although the VIRTIS Magellan comparison RMSD may suggest otherwise, the model  
516 based on the Earth based 1972 to 1988 observations is probably preferable to the Gold-  
517 stone 1972 to 1982 model. As stated above, the VIRTIS referencing may contain system-  
518 atic errors in latitude that have the potential to affect the fit when varying the position  
519 of the pole.

#### 520 4. Discussion and Conclusions

521 Over the 16 years between the Magellan and Venus Express missions, an offset in  
522 longitude of  $0.154 \pm 0.071^\circ$  between the two topography data sets is observed when the  
523 orientation model following IAU recommendations (Davies et al., 1992; Seidelmann et al.,  
524 2002) is used. This deviation is relevant for the retrieval of surface emissivity from orbiter  
525 near-infrared imaging (Helbert et al., 2008; Hashimoto et al., 2008; Arnold et al., 2008;  
526 Mueller et al., 2008; Smrekar et al., 2010; Haus and Arnold, 2010).

527 The orientation model recommended by the IAU (Davies et al., 1992) is based on  
528 Magellan synthetic aperture radar (SAR) images and there could conceivably be an offset

Observations and Reference	Period of rotation /days	Right ascension /deg	Declination /deg	$\Delta$ RMSD /m
Goldstone 1972 to 1982 (Slade et al., 1990)	243.022(3)	272.79(14)	67.23(5)	-0.198
Earth based 1972 to 1988 (Davies et al., 1992)	243.022(2)	272.74(2)	67.17(2)	-0.060
Earth based <sup>(1)</sup> (Davies et al., 1987, 1992)	243.025(2)	272.69(9)	67.17(6)	-0.007
Magellan gravimetry (Konopliv et al., 1999)	243.0200(2)	272.743(2)	67.156(1)	0.199
Magellan SAR <sup>(2)</sup> (Davies et al., 1992)	243.0185(1)	272.76(2)	67.16(1)	0.364
Venera & Magellan SAR (Davies et al., 1992)	243.023(1)	272.43(5)	67.16(2)	0.599
Earth based 1975 to 1983 (Shapiro et al., 1990)	243.026(6)	272.73(9)	67.11(9)	0.681
-0.154° longitude offset	243.0185	272.76	67.16	0
Revised period of rotation	243.0230	272.76	67.16	0.001

Table 3: Sets of Venus rotational parameters in the epoch of J2000 and their difference in root mean square deviation  $\Delta$ RMSD, relative to RMSD = 568.262 m. The numbers in brackets give error estimates for the last digit or digits. (1) Values recommended by the IAU (Davies et al., 1987) and used for Magellan altimetry referencing (Rappaport et al., 1999). (2) Values recommended by the IAU (Seidelmann et al., 2002) and used for VIRTIS referencing.

529 in referencing of the Magellan altimetry relative to the images. Howington-Kraus et al.  
530 (2002) test the Magellan sensor model including corrections for refraction and ephemeris  
531 errors by fitting radar image stereo pairs and minimizing the residuals between the stereo  
532 elevation models and Magellan GTDR altimetry. They report an error in the refraction  
533 correction corresponding to 0.15 km on ground - equivalent to less than  $0.01^\circ$  longitude  
534 at latitudes lower than  $80^\circ$ - but no systematic deviation between Magellan altimetry and  
535 radar imagery.

536 The offset in longitude could also be due to systematic or random errors in the  
537 VIRTIS data set. Excluding some areas which are thought to contain surface emissivity  
538 anomalies at recent lava flows (Smrekar et al., 2010) reduces the fitted offset by  $0.025^\circ$  to  
539  $-0.129^\circ$ . The coordinate referencing error in longitude from instrument alignment may  
540 be as large as  $0.075^\circ$  while the error from uncertainty in the correction for atmospheric  
541 refraction is less than  $0.003^\circ$ . The observation of an offset is reproducible with subsets  
542 of the VIRTIS data, which additionally allows to an estimate of the error of the offset.  
543 After the division into nine subsets the standard deviation of the fitted offsets is  $0.071^\circ$ ,  
544 which is comparable to the error estimate from VIRTIS referencing. Added together the  
545 systematic errors can nearly match the observed offset and if there are yet unidentified  
546 systematic errors this might explain the whole offset.

547 However, the offset can also be introduced if the period of rotation of Venus is 243.0228  
548 days as opposed to the value of 243.0185 days assumed for coordinate referencing based  
549 on IAU recommendations. This matches the period of rotation of  $243.022 \pm 0.002$  days  
550 derived from all available Earth based observations from 1972 to 1988 (Davies et al., 1992)  
551 and the period of rotation of  $243.022 \pm 0.003$  days derived from Goldstone observations  
552 (Slade et al., 1990). The latter orientation model appears to fit VIRTIS and Magellan  
553 data better but this is possibly caused by an error in the spin axis direction of the model  
554 and a bias in latitude in the VIRTIS data.

555 The spin axis direction of the former, from the Earth observations with the longest  
556 time baseline from 1972 to 1988, agrees with that from Magellan SAR (Davies et al.,  
557 1992) and gravity observations (Konopliv et al., 1999). Therefore the three independent  
558 spin axis estimates with the smallest formal errors are consistent with each other (Table  
559 3). The rotation periods of these models are however inconsistent or nearly inconsistent

560 with each other.

561 The inconsistency between the estimates of the period of rotation is puzzling, however  
562 the estimates are based on data from different times and over different timescales (see Fig.  
563 4). A change in spin rate of this magnitude is not inconsistent with Earth-based radar  
564 measurements of the instantaneous spin rate of Venus (Margot et al., 2006) obtained  
565 between 2004 and 2009 [Margot, personal communication, 2010].

566 Therefore it might be possible that the long time baseline estimates represent the  
567 average spin rate while the Magellan radar and gravity observations were made during  
568 a time when the spin rate deviated from its average. All discussed estimates that do not  
569 exclusively use Magellan data have a time baseline of at least 8 years and are formally  
570 consistent with a period of rotation of  $243.023 \pm 0.002$  days. The Magellan radar (Davies  
571 et al., 1992) and gravity (Konopliv et al., 1999) estimates are not consistent with this  
572 value, but observe each a 2 year period between 1990 and 1994. Thus a short, singular or  
573 periodic length of day excursion could explain why the Magellan radar period of rotation  
574 estimate differs by  $\sim 5$  min from the estimates with longer time baselines.

575 A possible explanation for such spin period variations is angular momentum exchange  
576 between the solid body of Venus and its thick, superrotating atmosphere (e.g. Schubert,  
577 1983). Assuming relative atmospheric angular momentum exchanges similar to Earth  
578 (Hide et al., 1980), length of day variations about one hour are possible (Golitsyn, 1982;  
579 Schubert, 1983). Parish et al. (2011) find in a Venus atmosphere general circulation  
580 model an angular momentum oscillation with an amplitude of 5 % with a periodicity of  
581  $\sim 10$  years. This corresponds to a length of day variation amplitude on the order of  $\sim 15$   
582 min (Schubert, 1983).

583 If the periods of rotation in table 3 are taken as average over each time baseline it  
584 is possible to fit the data with corresponding time averages of a sinusoid representing  
585 deviations from a period of rotation of 243.022d. The sinusoid with a period of 10 years  
586 and length of day variation amplitude of 15 min does not result in a good fit for any  
587 phase. For sinusoids with a period of 10 years there is a local minimum of the  $\chi^2$  statistic  
588 at an amplitude of 5.4 min and phase of 3.33 radian relative to the year 0. This minimum  
589  $\chi^2$  is 3.17 which is consistent with the data errors from table 3 and an appropriate model  
590 fitted with five degrees of freedom (Press et al., 1992).

591 There are however many formally better fits with sinusoid periods of less than 10  
592 years. Some of these have improbably low  $\chi^2$  which either hints towards exaggerated  
593 error estimates (Press et al., 1992) or towards a problem that is underconstrained due  
594 to the data representing averages over time. The deviation of the rotation period when  
595 averaged over a time interval greater than the period of the angular momentum oscillation  
596 is less than  $1/(2\pi)$  of the sinusoid amplitude. The errors of the rotation period estimates  
597 with baselines greater 8 years are only one order of magnitude smaller than a length of  
598 day variation amplitude of 15 min. Thus, for the long baseline estimates, any plausible  
599 deviation is therefore very close to or even less than the error. If only the two Magellan  
600 estimates with baselines of 2 years contribute significantly to the fit, it is difficult to  
601 constrain a sinusoid with three parameters.

602 While the period and amplitude of length of day variation observed in the global circula-  
603 tion model by Parish et al. (2011) is not consistent with the observations, it is possible  
604 that the model does not perfectly represent the atmosphere of Venus and that there is  
605 actually a different periodic length of day variation consistent with the observations.

606 The atmosphere is however not the the only possible source of angular momentum  
607 variation. Cottureau et al. (2011) compare various possible contributions to the Venus  
608 length of day variation. They conclude that torque exerted by the Sun on Venus repre-  
609 sented as a triaxial ellipsoid is the dominating contribution with a length of day variation  
610 of 120 s with a dominant periodicity of 58 d. From global circulation numerical models  
611 they derive an atmospheric contribution to the length of day variation of less than a  
612 minute with dominant frequencies corresponding to periods of less than 266 days. The  
613 numerical models are stated to be similar to the model presented by Lebonnois et al.  
614 (2010), which however does not show decadal variations similar to the model of Parish  
615 et al. (2011). In total the peak to peak length of day variations modeled by Cottureau  
616 et al. (2011) are approximately 3 min and thus additional sources of length of day vari-  
617 ation may be required.

618 Another aspect of the rotation dynamics of Venus is the proximity of rotation period  
619 to a resonance with Earth conjunctions at 243.16 days (e.g. Shapiro et al., 1979, 1990).  
620 The value of 243.023 days is outside of the interval of rotation periods that can be attained  
621 by libration (Shapiro et al., 1990). On the other hand, Caudal (2010) puts forward the

622 hypothesis of a differentially rotating solid inner core in resonance with Earth, which  
623 again leads to the question of angular momentum exchange.

624 Investigation of the possible periodicity of the Venus length of day variation is not  
625 possible with the data used here. A reinvestigation of the radar feature tracking data  
626 with detailed consideration of the times when individual features were observed while  
627 allowing for length of day variation may yield better results but is beyond the scope  
628 of this manuscript. Additional measurements of the instantaneous spin rate of Venus  
629 (Margot et al., 2006) would be very helpful.

630 Regardless of the large uncertainties of the VIRTIS Magellan comparison, measure-  
631 ments with a shorter time baseline such as the work of Davies et al. (1992) may be less  
632 well suited to create a model of planetary rotation for the purpose of coordinate referenc-  
633 ing. If we construct a new orientation model using the IAU pole position (Seidelmann  
634 et al., 2002) and the Magellan-VIRTIS rotation period obtained here, we find that this  
635 model is consistent with the with the model from Earth based observations between 1972  
636 to 1988 as cited in the work of Davies et al. (1992). Both have relatively long time base-  
637 lines of 16 years and therefore likely provide a more accurate long term description of  
638 the orientation of Venus than the model recommended by the IAU (Seidelmann et al.,  
639 2002), which is based on radar observations over a period of 2 years (Davies et al., 1992).

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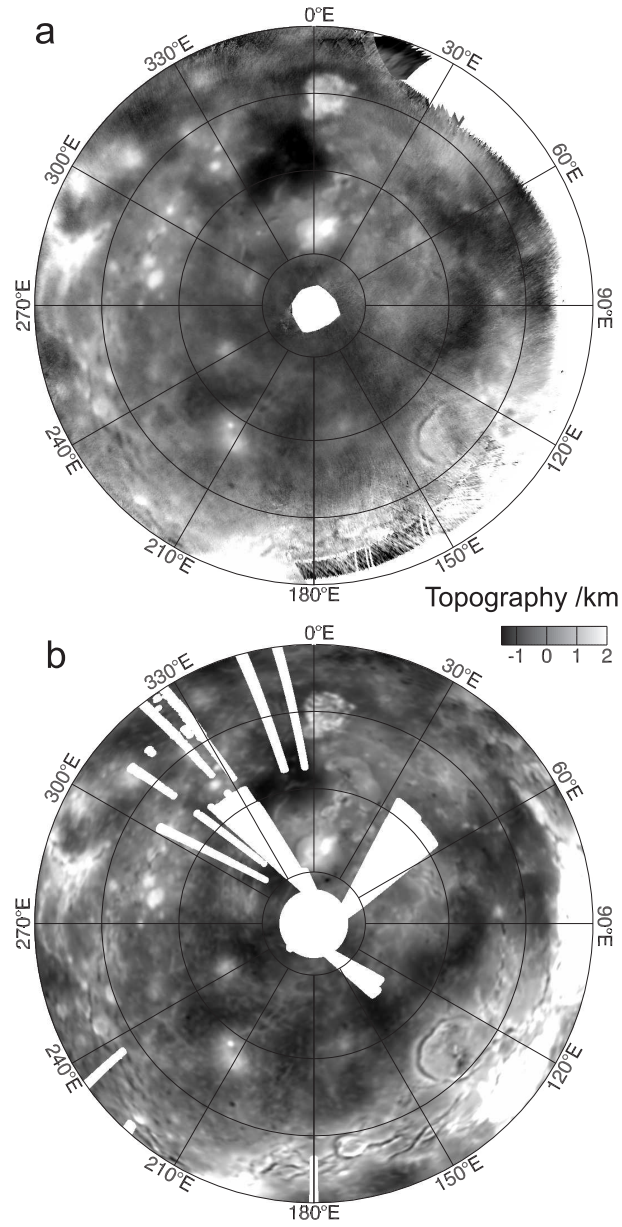


Figure 1: Topography maps of the southern hemisphere of Venus in Lambert's azimuthal equal area projection. a) derived from VIRTIS near infrared thermal emission data. b) Magellan altimetry (Rappaport et al., 1999) smoothed to resemble thermal emission resolution. Areas within 100 km distance of missing data are left blank.

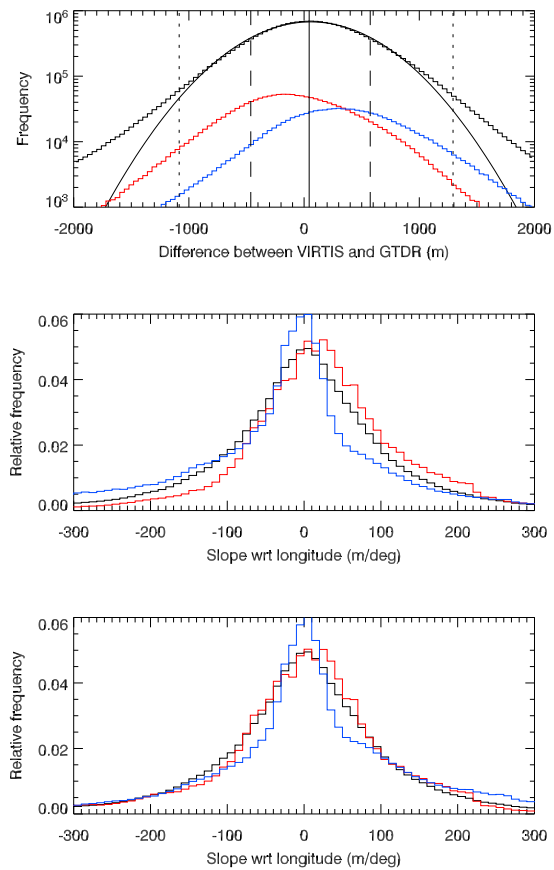


Figure 2: a) Frequency distribution of differences between VIRTIS data and GTDR. The black histogram represents the whole data set, the solid graph is a fit of a gaussian with center at 58 m and standard deviation of 494 m. The solid vertical line represents the median deviation at 44 m while the long-dashed represent the 16th and 84th percentile -i.e.  $1\sigma$  in a normal distribution- and the short dashed the 2.3th and 97.7th percentile. The red and blue histograms represent subsets of the data with a local bias of less than -300 m and more than 300 m, respectively. b) The relative frequency distributions of slopes with respect to longitude for the whole set and the two subsets. c) A reselection of the outlying subsets correcting for an assumed offset in longitude of -0.3 deg.

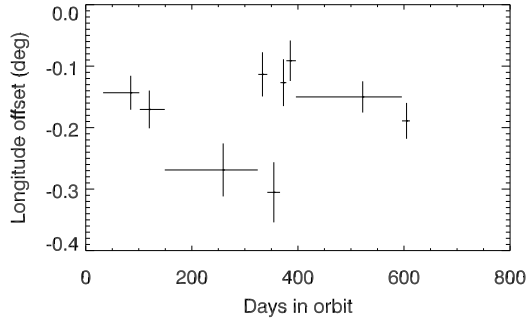


Figure 3: Offset derived from similarly sized subsets created by assigning images in order of data acquisition time. Horizontal bars denote period of data acquisition for each subset. The varying data acquisition duration of subsets is due to the varying rate of data produced by VIRTIS. Venus Express (VEX) orbit insertion was on 4 April 2006, 5577 Julian days after the median Magellan data acquisition time. The  $\chi^2$  error estimates are too small for the scale of this plot. The vertical error bars correspond to the confidence interval derived from the 'bootstrap' method.

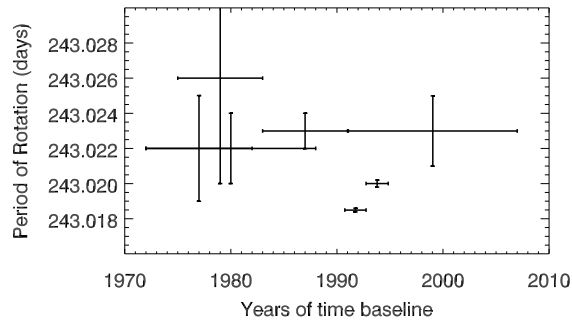


Figure 4: The most recent estimates of the period of rotation and the time baseline of measurements. The full models and their sources are given in table 3. The horizontal bars show the period over which the data for each estimate was acquired.