



# Modeling the next battery generation: Lithium-sulfur and lithium-air cells

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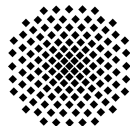
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in der Helmholtz-Gemeinschaft



HIU



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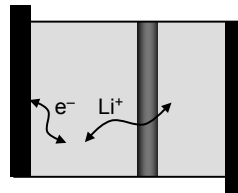


Bundesministerium  
für Bildung  
und Forschung

# Research profile: Computational battery technology

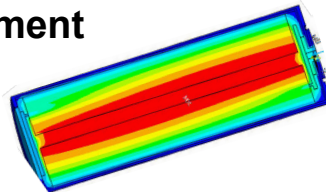
## ➤ Lithium-ion technology

**LiFePO<sub>4</sub> batteries:  
Electrochemistry  
and impedance**



Understanding and optimization of physicochemical behavior

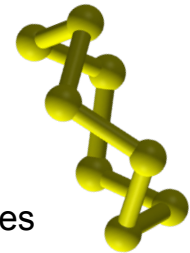
**Thermal management  
and runaway risk**



Understanding and optimization of thermal and safety behavior

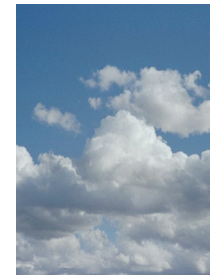
## ➤ Post-lithium-ion cells

**Lithium-sulfur cells:  
Redox chemistry and  
transport**



Analysis of cycling properties and chemical reversibility

**Lithium-air cells:  
Multi-phase chemistry  
and reversibility**



Improvement of porous air electrode

## ➤ Multi-scale and multi-physics modeling and numerical simulation



Motivation and approach

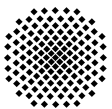
Lithium-sulfur

Lithium-air (organic)

Lithium-air (aqueous)

Conclusions

DLR





## Motivation and approach

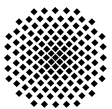
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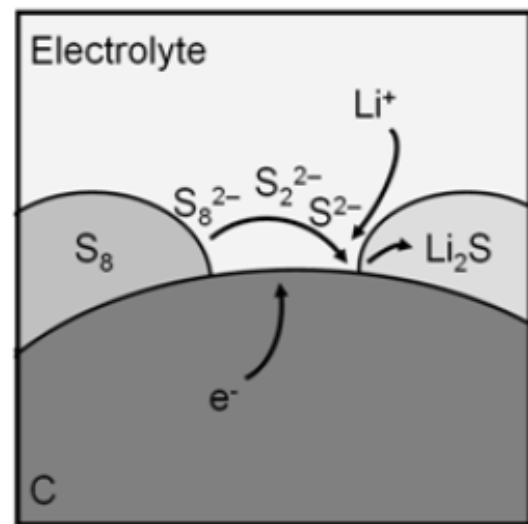


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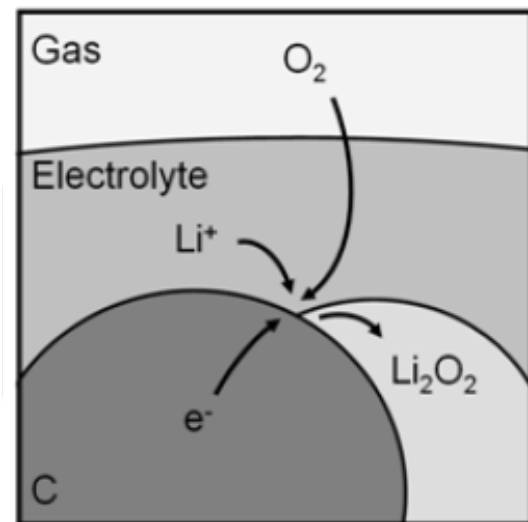
# Li-S and Li-O: Challenges

- Complex multi-phase management
  - Li-S: Solid reactant  $S_8$  and product  $Li_2S$ , solid precipitates
  - Li-O: Solid, liquid and gas phase involved
- Complex chemistry
  - Li-S: Polysulfide ion intermediates
  - Li-O: Oxygen reduction as traditional problem of electrochemistry
- Low cycleability, low efficiency
- **Computational modeling for understanding and optimization**

Li-S cathode



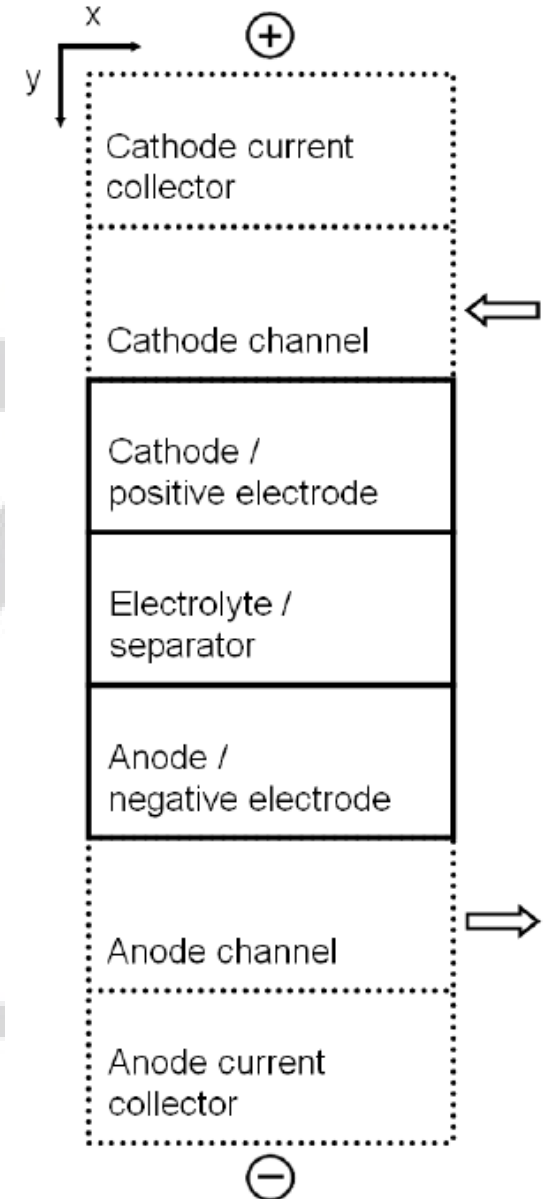
Li-O cathode



# 1D/2D generic modeling framework

- Electrochemical cell of up to seven **layers**
- Each layer consists of arbitrary number of solid, liquid and/or gaseous **bulk phases**
- Each layer can contain an arbitrary number of **interfaces** (phase boundaries)
- Each bulk phase consists of arbitrary number of **chemical species**
- **Chemistry** takes place at interfaces
- **Transport** mechanisms (liquid, solid, gas)
- **Continuum** (homogenization) approach

J. P. Neidhardt, D. N. Fronczek, T. Jahnke, T. Danner, B. Horstmann and W. G. Bessler, J. Electrochem. Soc., submitted (2012).





# Chemical reactions at interfaces

- Mass-action kinetics describes chemical source terms  $\dot{s}_i$

$$\dot{s}_i = \nu_i \left( k_f \prod_{j \in R_f} c_j^{\nu_j'} - k_r \prod_{j \in R_r} c_j^{\nu_j''} \right)$$

$\nu$  stoichiometric coefficient  
 $k$  reaction rate constant  
 $c$  concentration of reactants

- Rate constants described by modified Arrhenius expression. Reverse rate follows from thermodynamic consistency.

$$k_f = A^f T^\beta \underbrace{\exp\left(-\frac{E^{\text{act}}}{RT}\right)}_{\text{Temperature dependence}} \underbrace{\exp\left(-\frac{\alpha z F}{RT} \Delta\phi\right)}_{\text{Potential dependence}}$$

$$\frac{k_f}{k_r} = \exp\left(-\frac{\Delta G^0}{RT}\right)$$

Preexponen-  
tial factor

Temperature dependence  
(Activation energy  $E^{\text{act}}$ )

Potential dependence  
(Half-cell potential  $\Delta\phi$ )

# Multi-phase management

- The volume fraction  $\varepsilon_i$  of each phase  $i$  depends on time

$$\frac{\partial(\varepsilon_i \rho_i)}{\partial t} = R_i M_i$$

$\varepsilon$  volume fraction

$\rho$  density

$R$  chemical formation rate

$M$  molar mass

- Volume fractions sum up to one. Def. of compressible phase necessary.

$$\sum \varepsilon_i = 1$$

- Microstructural effects enter via interfacial area and transport coefficients

$$A_{m,n}^V = A_0^V \cdot f(\varepsilon_m, \varepsilon_n)$$

$A^V$  volume-specific surface area /  $\text{m}^2/\text{m}^3$

$$D_i^{\text{eff}} = \frac{\varepsilon_i}{\tau_i^2} D_i \quad \sigma_i^{\text{eff}} = \frac{\varepsilon_i}{\tau_i^2} \sigma_i$$

$D$  diffusion coefficient

$\sigma$  Conductivity



# Mass and charge transport in liquid electrolyte

- Species conservation  
(Nernst-Planck equation)

$$\frac{\partial(\varepsilon c_i)}{\partial t} = -\frac{\partial J_i}{\partial y} + \sum_m A_m^V \dot{s}_{i,m}$$

$$J_i = -D_i^{\text{eff}} \frac{\partial c_i}{\partial y} - D_i^{\text{migr,eff}} \frac{\partial \phi_{\text{elyt}}}{\partial y}$$

- Charge neutrality

$$0 = -\sum_i z_i F \frac{\partial J_i}{\partial y} + \sum_m z_i F A_m^V \dot{s}_{i,m}$$

- Diluted solution theory  
(Li-S)

$$D_i^{\text{migr}} = \frac{z_i F}{RT} c_i D_i$$

- Concentrated solution theory  
(Li-O)

$$D_{\pm} = D^0 + \frac{t_{\pm}}{z_{\pm} F} \frac{\sigma_D}{c_{\pm}}$$

$$D_{\pm}^{\text{migr}} = \frac{t_{\pm}}{z_{\pm} F} \sigma$$

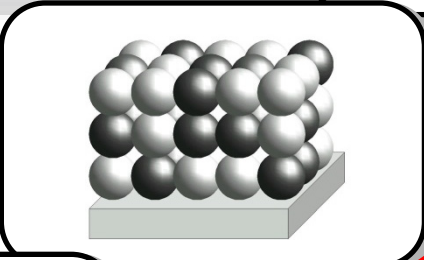
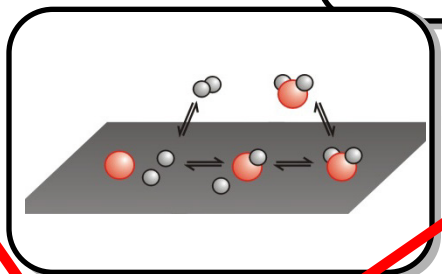
m

nm

# Multi-scale simulation framework

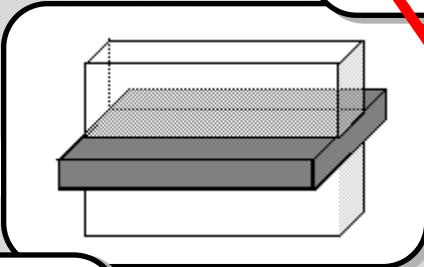
- DENIS: Detailed Electro-chemistry and Numerical Impedance Simulation
- In-house C/C++ software
- Workhorse of the group

Interfaces

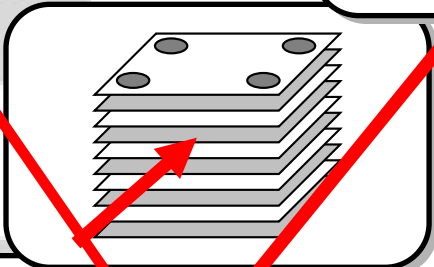


Electrode

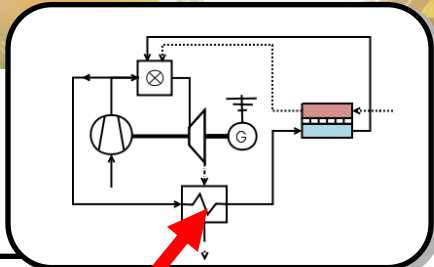
DENIS



Cell



Stack



System

MATLAB

Coupling DENIS-SIMULINK

ANSYS/COMSOL

Coupling DENIS-ANSYS/COMSOL for CFD simulations

LIMEX

Implicit DAE solver (Deuflhard, Berlin)

CANTERA

Coupling with CANTERA (Goodwin, Caltech) for chemistry source terms and transport coefficients



Motivation and approach

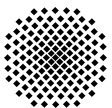
## **Lithium-sulfur**

Lithium-air (organic)

Lithium-air (aqueous)

Conclusions

DLR



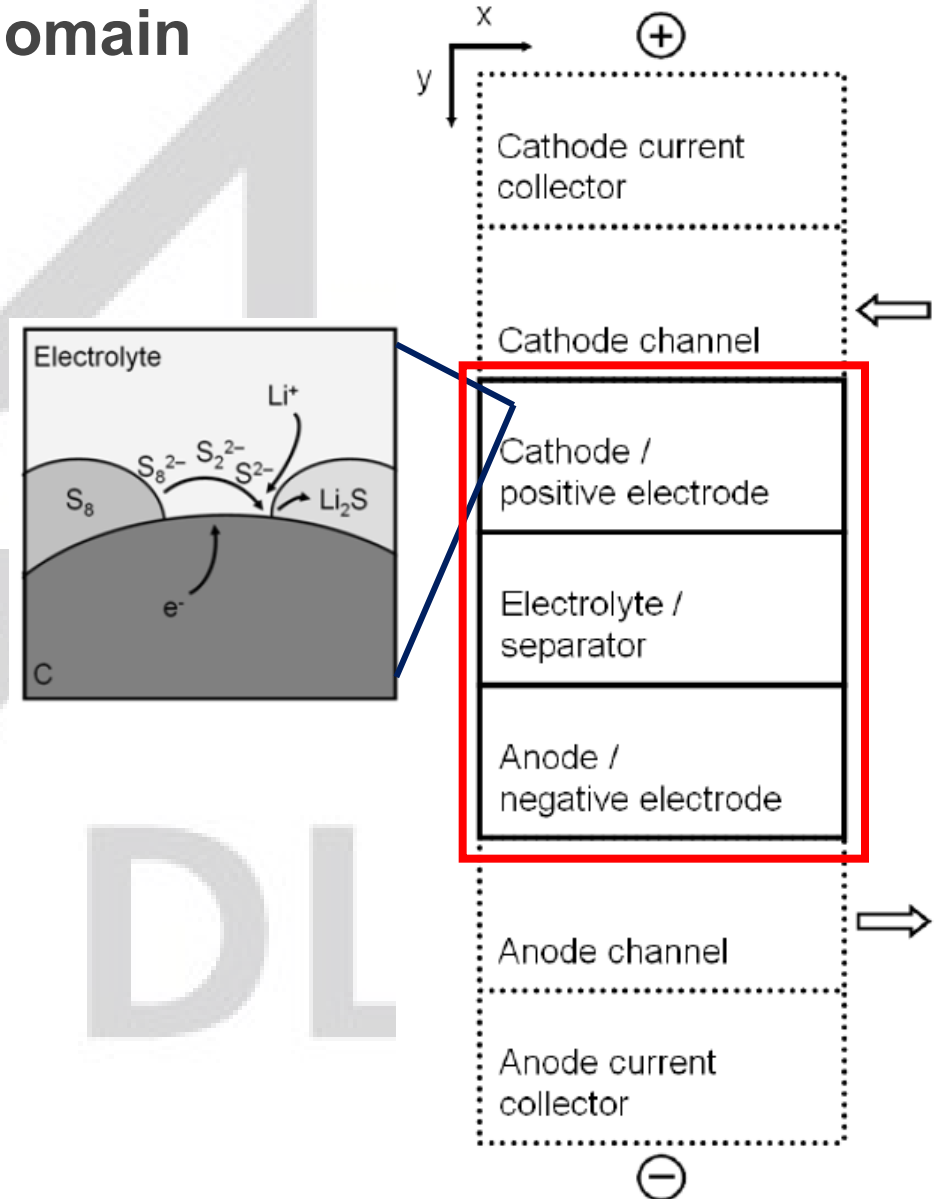
HIU (C)

# Li-S battery modeling domain

Cathode properties:

- Thickness: 41  $\mu\text{m}$
- Phases (charged state):
  - Sulfur  $\epsilon = 0.16$
  - Carbon  $\epsilon = 0.06$
  - Electrolyte  $\epsilon = 0.78$
  - $\text{Li}_2\text{S}$   $\epsilon = 10^{-7}$
- Interfaces:
  - Sulfur-Electrolyte
  - Carbon-Electrolyte
  - $\text{Li}_2\text{S}$ -Electrolyte

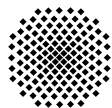
Anode: Lithium metal



# Li-S battery model: Thermodynamics and transport

Species	Molar Gibbs energy / $\text{kJ}\cdot\text{mol}^{-1}$	Density / Initial concentration	Diffusion coefficient / $\text{m}^2\cdot\text{s}^{-1}$
Li	0	$5.34\cdot 10^2 \text{ kg}\cdot\text{m}^{-3}$	
C	0	$2.26\cdot 10^3 \text{ kg}\cdot\text{m}^{-3}$	
$\text{S}_8^{(\text{solid})}$	0	$2.07\cdot 10^3 \text{ kg}\cdot\text{m}^{-3}$	
$\text{Li}_2\text{S}$	-441.4		
$\text{C}_4\text{H}_6\text{O}_3$	0	$9.831\cdot 10^3 \text{ mol}\cdot\text{m}^{-3}$	
$\text{Li}^+$	0	$9.841\cdot 10^2 \text{ mol}\cdot\text{m}^{-3}$	$1\cdot 10^{-10}$
$\text{PF}_6^-$	0	$9.830\cdot 10^2 \text{ mol}\cdot\text{m}^{-3}$	$4\cdot 10^{-10}$
$\text{S}^{2-}$	-405.08	$8.127\cdot 10^{-10} \text{ mol}\cdot\text{m}^{-3}$	$1\cdot 10^{-10}$
$\text{S}_2^{2-}$	-422.29	$5.141\cdot 10^{-7} \text{ mol}\cdot\text{m}^{-3}$	$1\cdot 10^{-10}$
$\text{S}_4^{2-}$	-450.91	$1.966\cdot 10^{-2} \text{ mol}\cdot\text{m}^{-3}$	$1\cdot 10^{-10}$
$\text{S}_6^{2-}$	-460.23	$3.185\cdot 10^{-1} \text{ mol}\cdot\text{m}^{-3}$	$6\cdot 10^{-10}$
$\text{S}_8^{2-}$	-461.20	$1.750\cdot 10^{-1} \text{ mol}\cdot\text{m}^{-3}$	$6\cdot 10^{-10}$
$\text{S}_8^{(\text{liquid})}$	-48	$1.868 \text{ mol}\cdot\text{m}^{-3}$	$1\cdot 10^{-9}$

➤ Parameters converted from Kumaresan et al., J. Electrochem. Soc. 155, A576 (2008)



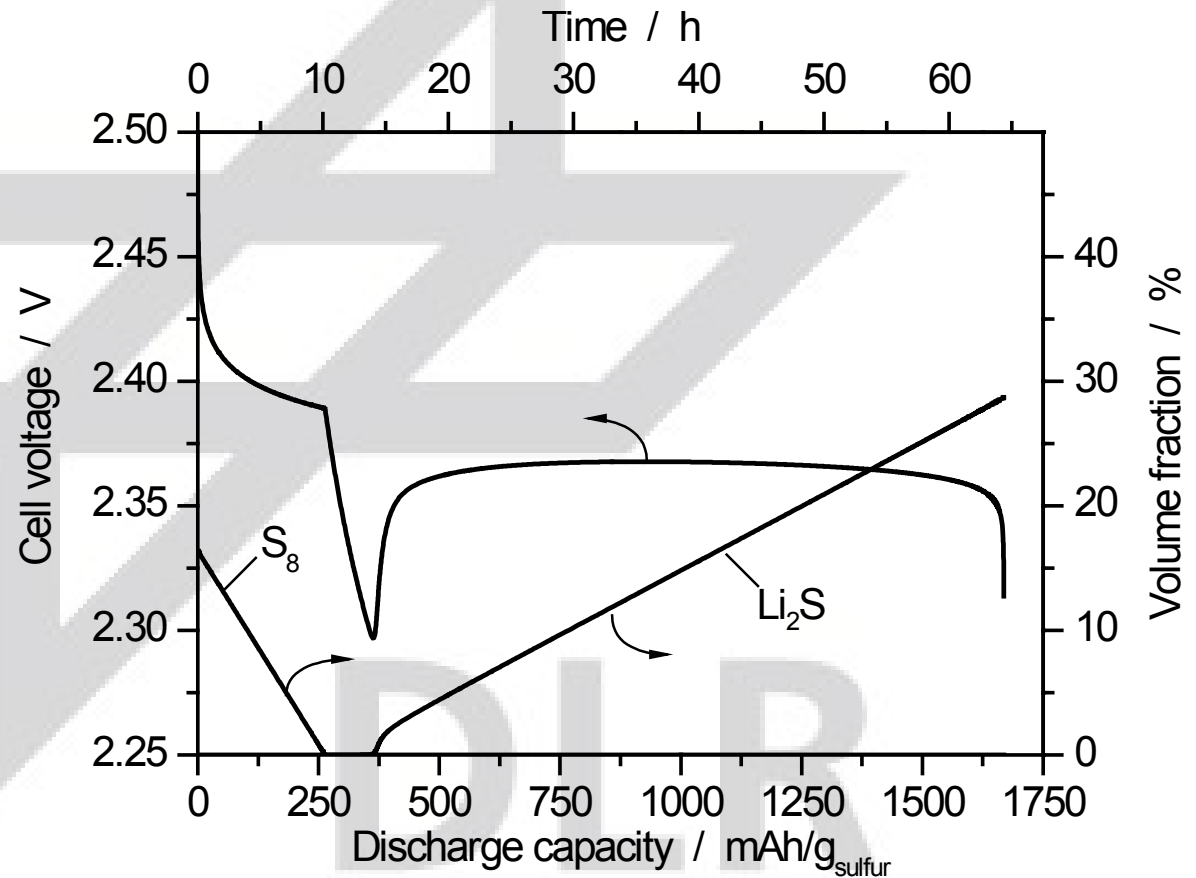
# Li-S battery model: Reactions and kinetics

Reaction	Preexponential factor, forward reaction	Preexponential factor, reverse reaction
$\text{Li} \rightleftharpoons \text{Li}^+ + \text{e}^-$	$4.086 \cdot 10^{-9} \text{ m}^{-5} \cdot \text{mol}^2 \cdot \text{s}^{-1}$	$1 \text{ m}^{-2} \cdot \text{mol} \cdot \text{s}^{-1}$
$\text{S}_8^{(\text{solid})} \rightleftharpoons \text{S}_8^{(\text{liquid})}$	$1.900 \cdot 10^{-2} \text{ m}^{-0.5} \cdot \text{mol}^{0.5} \cdot \text{s}^{-1}$	$1 \text{ s}^{-1}$
$\frac{1}{2} \text{S}_8^{(\text{solid})} + \text{e}^- \rightleftharpoons \frac{1}{2} \text{S}_8^{2-}$	$7.725 \cdot 10^{13} \text{ m}^{-0.5} \cdot \text{mol}^{0.5} \cdot \text{s}^{-1}$	$2.940 \cdot 10^{-27} \text{ m}^{-0.5} \cdot \text{mol}^{0.5} \cdot \text{s}^{-1}$
$\frac{3}{2} \text{S}_8^{2-} + \text{e}^- \rightleftharpoons 2 \text{S}_6^{2-}$	$4.331 \cdot 10^{16} \text{ m} \cdot \text{mol}^{-0.5} \cdot \text{s}^{-1}$	$1.190 \cdot 10^{-23} \text{ m}^4 \cdot \text{mol}^{-1} \cdot \text{s}^{-1}$
$\text{S}_6^{2-} + \text{e}^- \rightleftharpoons \frac{3}{2} \text{S}_4^{2-}$	$3.193 \cdot 10^{14} \text{ s}^{-1}$	$4.191 \cdot 10^{-24} \text{ m} \cdot \text{mol}^{-0.5} \cdot \text{s}^{-1}$
$\frac{1}{2} \text{S}_4^{2-} + \text{e}^- \rightleftharpoons \text{S}_2^{2-}$	$2.375 \cdot 10^{11} \text{ m}^{-0.5} \cdot \text{mol}^{0.5} \cdot \text{s}^{-1}$	$7.505 \cdot 10^{-24} \text{ s}^{-1}$
$\frac{1}{2} \text{S}_2^{2-} + \text{e}^- \rightleftharpoons \text{S}^{2-}$	$4.655 \cdot 10^{12} \text{ m}^{-0.5} \cdot \text{mol}^{0.5} \cdot \text{s}^{-1}$	$4.738 \cdot 10^{-22} \text{ s}^{-1}$
$2 \text{Li}^+ + \text{S}^{2-} \rightleftharpoons \text{Li}_2\text{S}^{(\text{solid})}$	$2.750 \cdot 10^{-5} \text{ m}^6 \cdot \text{mol}^2 \cdot \text{s}^{-1}$	$8.250 \cdot 10^{-19} \text{ s}^{-1}$

➤ Parameters converted from Kumaresan et al., J. Electrochem. Soc. 155, A576 (2008)

# Li-S: Simulated discharge curve and phase change

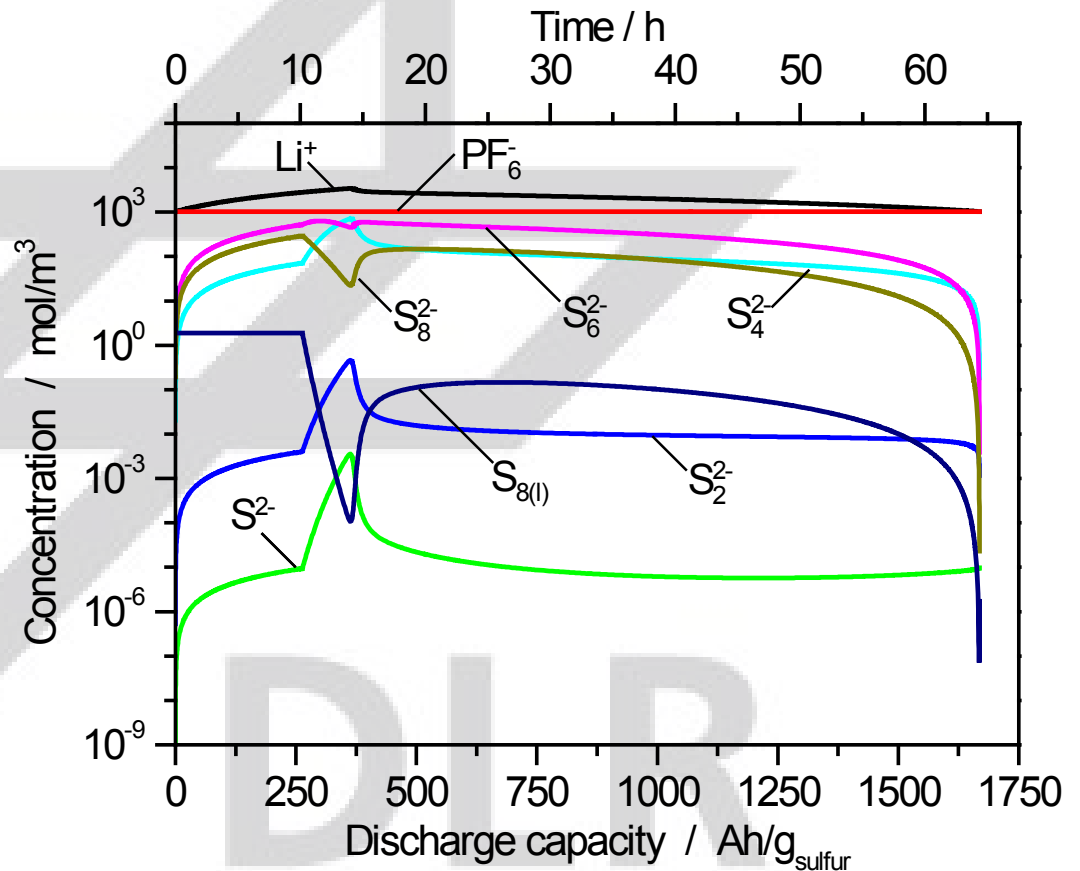
- Discharge shows typical two-stage behavior
- Solid  $S_8$  is fully consumed before solid  $Li_2S$  is formed





# Li-S: Simulated ionic species concentrations

- First stage: Sulfur polyanions are formed
- Second stage: Sulfur polyanions are reduced
- End of discharge: No more sulfur polyanions





Motivation and approach

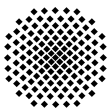
Lithium-sulfur

**Lithium-air (organic)**

Lithium-air (aqueous)

Conclusions

DLR



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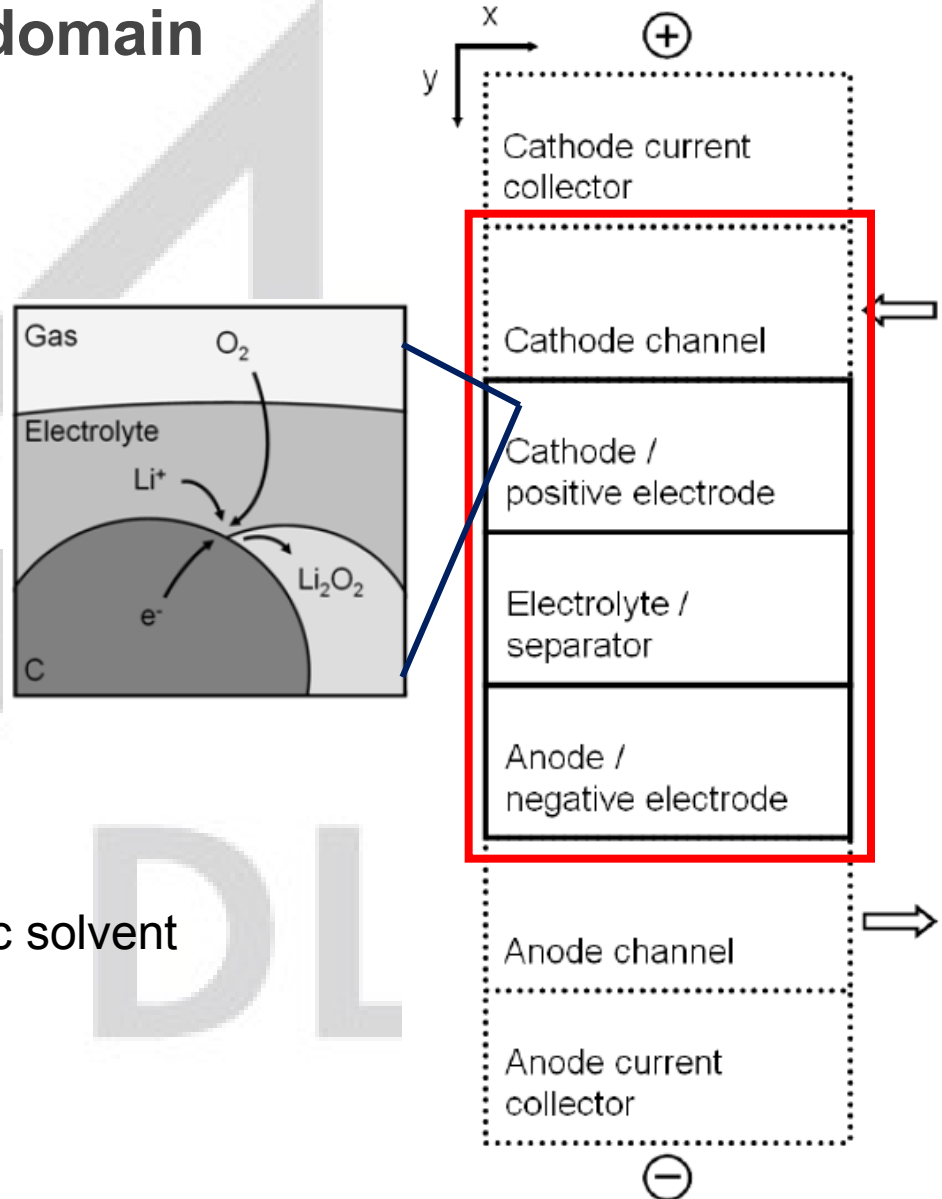
# Li-O battery modeling domain

Cathode properties:

- Thickness: 750  $\mu\text{m}$
- Phases:
  - Carbon  $\epsilon = 0.25$
  - Electrolyte  $\epsilon = 0.75$
  - $\text{Li}_2\text{O}_2$   $\epsilon = 10^{-7}$
- Interfaces:
  - Carbon-Electrolyte- $\text{Li}_2\text{O}_2$

Electrolyte:  $\text{LiPF}_6$  / Stable organic solvent

Anode: Metallic lithium



# Li-O battery model: Thermodynamics and kinetics

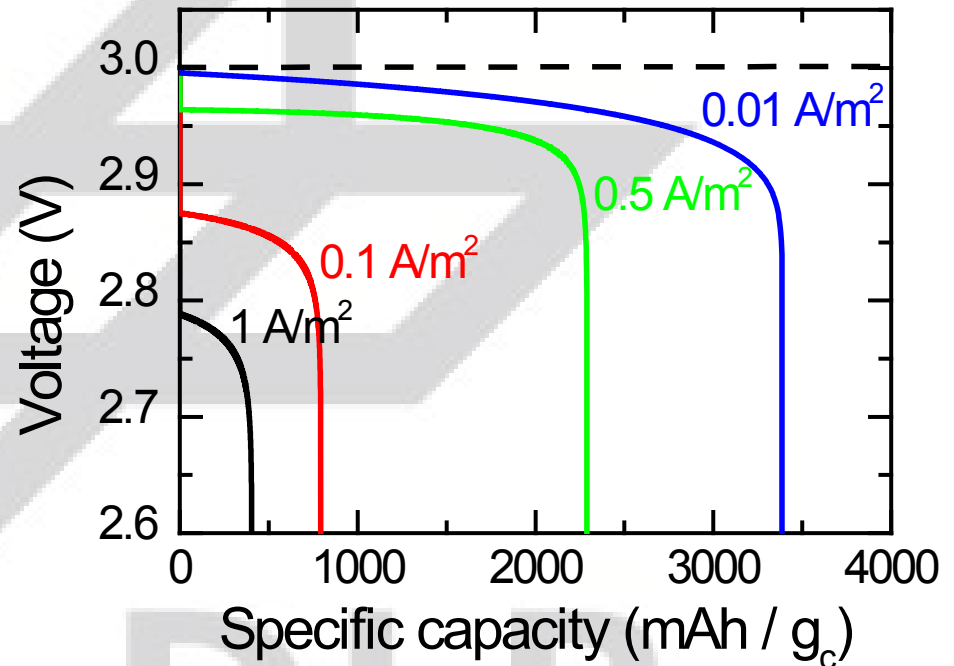
Species	Molar Gibbs energy / $\text{kJ}\cdot\text{mol}^{-1}$	Density / Initial concentration
Li	0	$5.34\cdot 10^2 \text{ kg}\cdot\text{m}^{-3}$
$\text{Li}^+$	0	$1.0\cdot 10^3 \text{ mol}\cdot\text{m}^{-3}$
$\text{PF}_6^-$	-	$1.0\cdot 10^3 \text{ mol}\cdot\text{m}^{-3}$
$\text{O}_2^{(\text{gas})}$	-61	21 %
$\text{O}_2^{(\text{dissolved})}$	-43	$1.62 \text{ mol}\cdot\text{m}^{-3}$
$\text{Li}_2\text{O}_2$	-644	$2.14\cdot 10^3 \text{ kg}\cdot\text{m}^{-3}$
EC-EMC	-	$1.07\cdot 10^4 \text{ mol}\cdot\text{m}^{-3}$

Reaction	Preexponential factor, forward reaction	Activation energy
$\text{Li} \rightleftharpoons \text{Li}^+ + \text{e}^-$	$1.31\cdot 10^{-1} \text{ m}\cdot\text{s}^{-1}$	0
$\text{O}_2^{(\text{gas})} \rightleftharpoons \text{O}_2^{(\text{dissolved})}$	Assumed in equilibrium	-
$2 \text{Li}^+ + \text{O}_2^{(\text{dissolved})} + 2 \text{e}^- \rightleftharpoons \text{Li}_2\text{O}_2$	$9.23\cdot 10^{31} \text{ m}^7\cdot\text{mol}^{-2}\cdot\text{s}^{-1}$	0

- Parameters converted from: P. Andrei, J. P. Zheng, M. Hendrickson and E. J. Plichta, J. Electrochem. Soc., 157, A1287 (2010); A. Nyman, M. Behm and G. Lindbergh, Electrochim. Acta, 53, 6356 (2008); R. C. Weast, Handbook of chemistry and physics, CRC Press (1982).

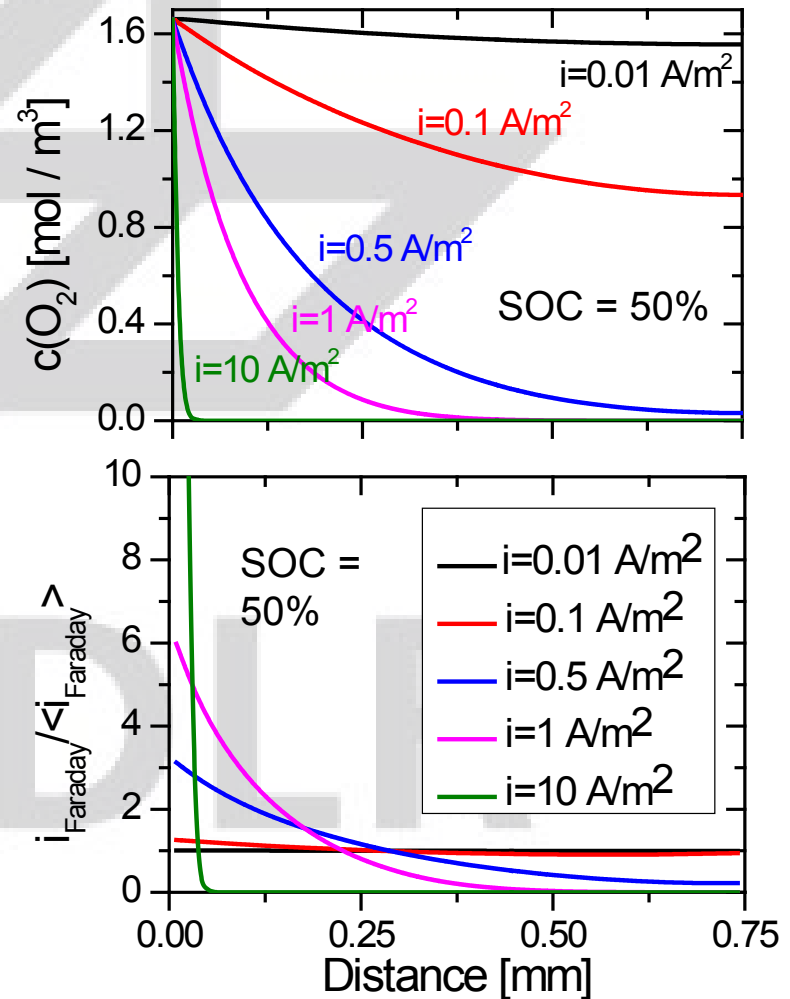
## Li-O: Simulated discharge behavior

- Discharge curves simulated for different current densities
- Polarization losses increase with increasing current density
- Capacity strongly depends on current density



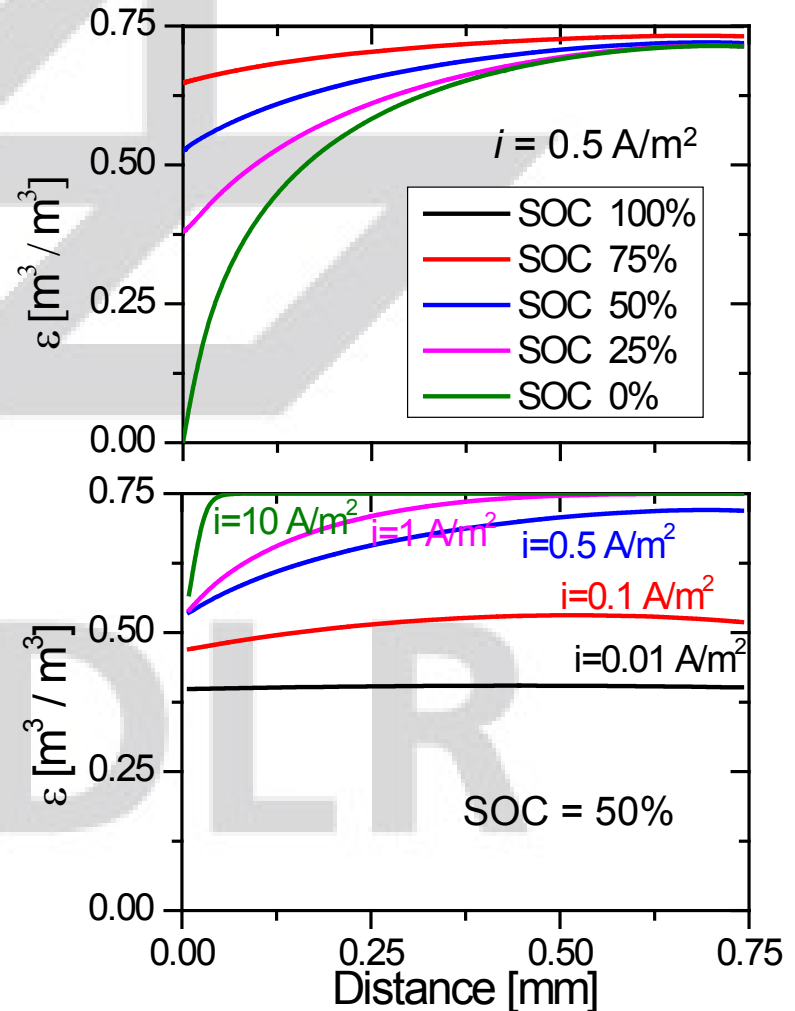
# Li-O: Spatial distribution

- Strong gradients of dissolved  $O_2$  in organic electrolyte
- At high currents, reactions are confined to regions close to channel
- **Rate-limiting  $O_2$  diffusion is origin of polarization losses**



# Li-O: Pore clogging

- Free porosity decreases upon discharge
- Pore clogging by product  $\text{Li}_2\text{O}_2$
- Clogging stronger close to channel
- Strong gradients for high currents
- **Pore clogging is origin of current-dependent capacity loss**







Motivation and approach

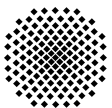
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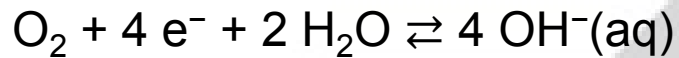


HIU (C)



## Aqueous Li-O: LiOH as soluble intermediate

➤ Oxygen reduction:



➤ Precipitation:



DLR

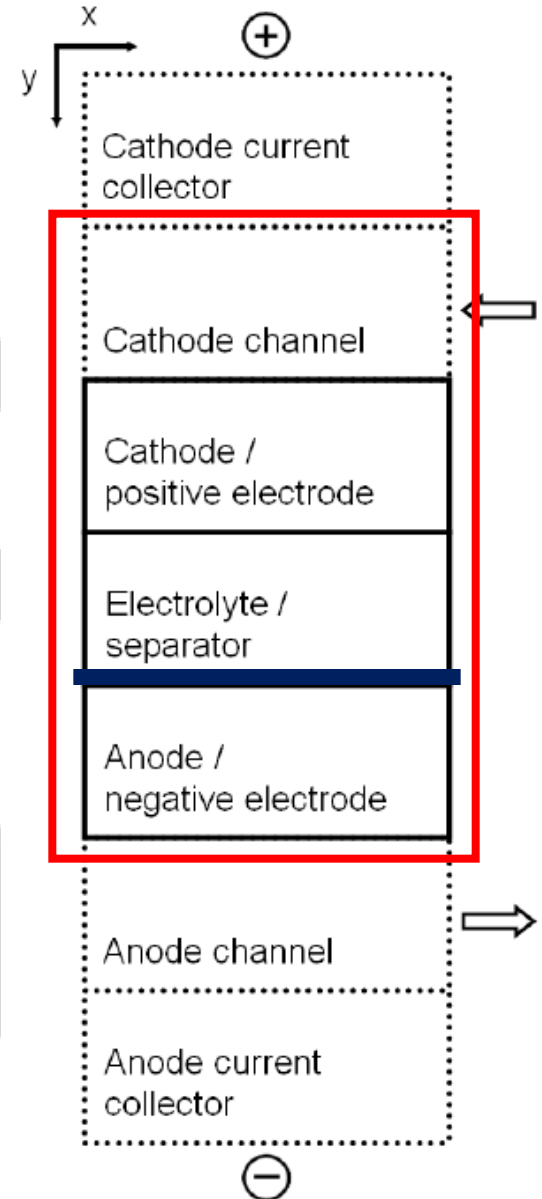
# Aqueous Li-O modeling domain

## Cathode properties:

- Thickness: 500  $\mu\text{m}$
- Phases (start composition):
  - Carbon  $\varepsilon = 0.25$
  - Water  $\varepsilon = 0.75$
  - $\text{LiOH}\cdot\text{H}_2\text{O}$   $\varepsilon = 10^{-7}$
- Interfaces:
  - Carbon-Electrolyte- $\text{LiOH}\cdot\text{H}_2\text{O}$

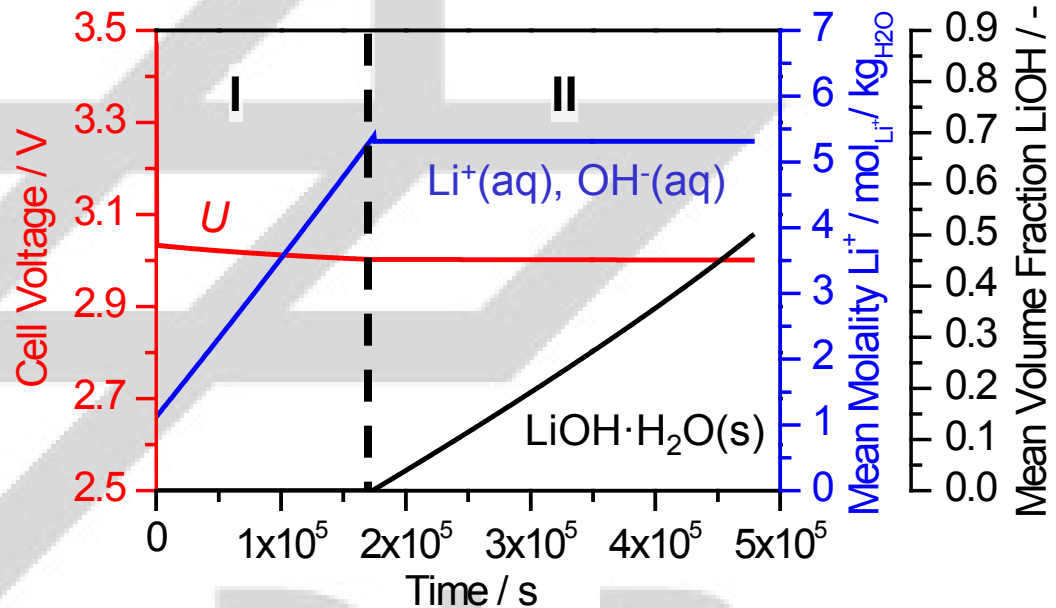
## Separator properties:

- Porous thickness: 100  $\mu\text{m}$
- Ideal separation from anode assumed (e.g.,  $\text{Li}^+$ -conducting glass)



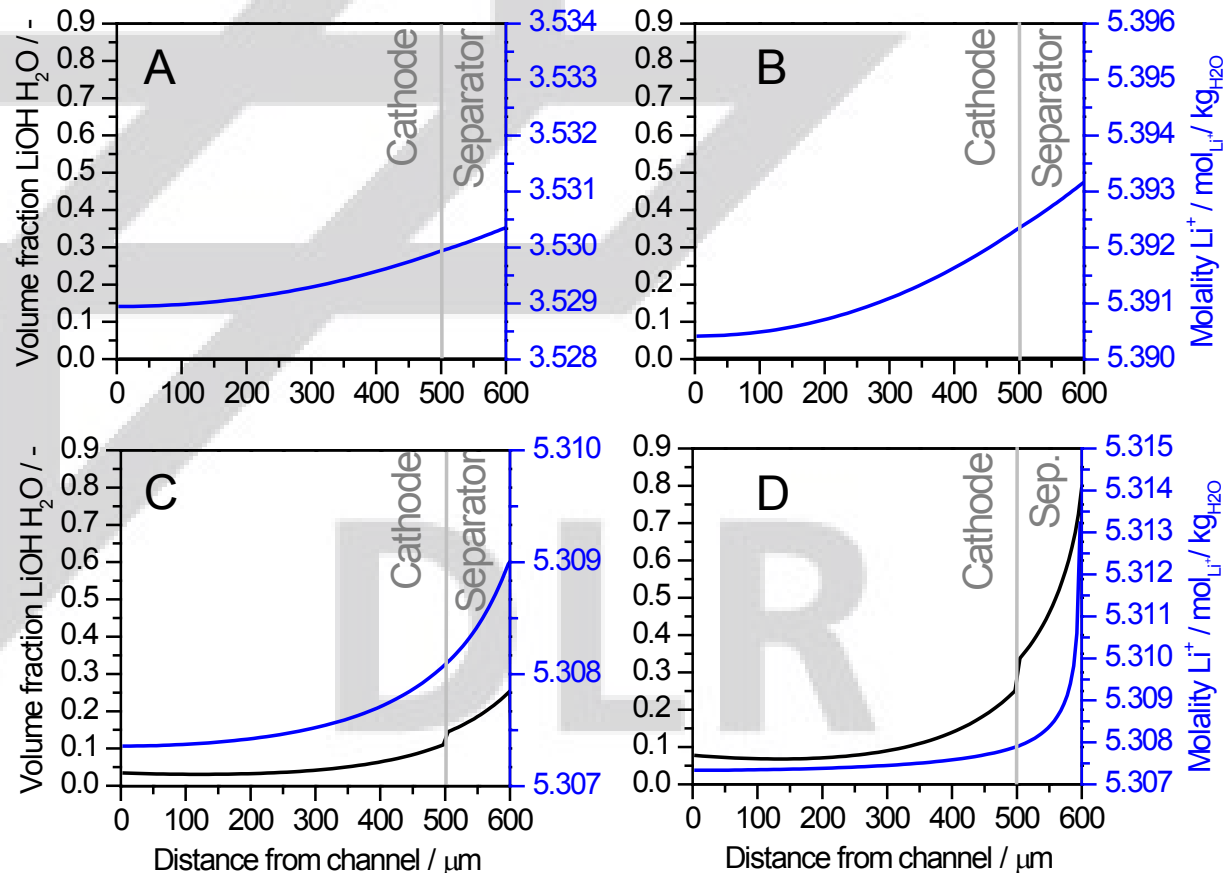
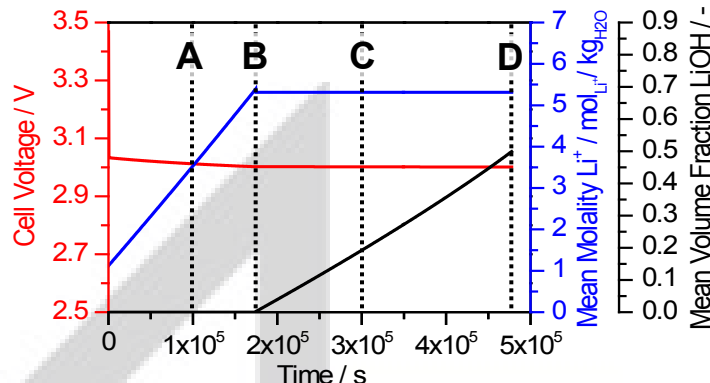
# Results: Aqueous Li-O battery

- Two-stage discharge
- I: Dissolved LiOH  
Small voltage variation
- II: Precipitation of  $\text{LiOH}\cdot\text{H}_2\text{O}$   
Constant voltage
- End of discharge:  
Capacity limited by LiOH precipitation



# Concentration distribution

- A  $\text{Li}^+/\text{OH}^-$  concentration gradient, peak at anode
  - B Increasing  $\text{Li}^+/\text{OH}^-$  concentration
  - C Beginning  $\text{LiOH}$  precipitation within separator close to anode
  - D  $\text{LiOH}$  precipitation at oxygen inlet and anode surface
- **End of discharge due to  $\text{LiOH}$  film on anode surface**





Motivation and approach

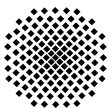
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Lithium-air (organic)

Lithium-air (aqueous)

**Conclusions**

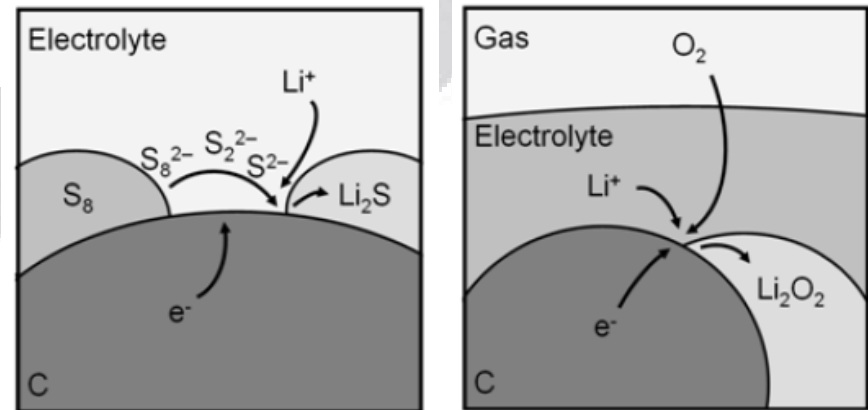
DLR



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## Summary: Next-generation battery modeling

- Li-S and Li-O batteries: High energy density, low cycleability
- Challenges: Complex chemistry and complex multi-phase behavior
- Chemistry, phases and transport included into modeling framework
- Li-S: Two-stage behavior: Dissolution, charge transfer, precipitation mechanism
- Li-O organic: Low oxygen diffusivity and pore clogging at channel
- Li-O aqueous: Low oxygen diffusivity and pore clogging at anode



**Thank you for your attention!**

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