Wind loads on heliostats and photovoltaic trackers at various Reynolds numbers

A. Pfahl\textsuperscript{a,*}, H. Uhlemann\textsuperscript{b}

\textsuperscript{a}German Aerospace Center (DLR) 
Solar Research  
Pfaffenwaldring 38-40  
D – 70569 Stuttgart 
Germany  
Andreas.Pfahl@dlr.de

\textsuperscript{b}German Dutch Wind Tunnels (DNW)  
Bunsenstrasse 10  
D – 37073 Göttingen  
Germany  
Heiko.Uhlemann@dnw-germany.aero

Available online at http://www.sciencedirect.com/science/article/pii/S0167610511001231 
© 2011 The Authors. Published by Elsevier Ltd.  
doi:10.1016/j.jweia.2011.06.009

Abstract
Wind loads on heliostats are usually determined at boundary layer, low-speed wind tunnels at which the design full-scale Reynolds number cannot be reached. In doing so, it is supposed the wind load coefficients are Reynolds number independent, which is known to be the case for sharp edged bodies. But for the stow position the usually round torque tube is directly exposed to the wind and could influence the wind loads.

By measurements in a high-pressure wind tunnel, it can be demonstrated that the design-relevant wind load coefficients are not Reynolds number dependent. However, the inclination of the mirror plane in stow position, due to the deflection of the heliostats structure at high Reynolds number, leads to increased wind loads and must be considered. The results are also valid for photovoltaic trackers of similar shape.

Keywords
heliostat, PV tracker, wind load, Reynolds number, high pressure wind tunnel, central receiver, solar tower, concentrated solar power, solar thermal

1 Introduction

* Corresponding author: Tel.: ++49 711 6862 479, Fax: ++49 711 6862 8032
Solar thermal power plants are a promising option to cover significant parts of increasing energy demand. At solar tower plants (Figure 1), sun-light is concentrated by mirrors that track the sun in two axes, the so-called heliostats. To reduce the blocking of each other, the heliostats reflect the sun rays to the top of a tower. There a receiver absorbs the radiation and supplies thermal energy to a power cycle; alternatively, the energy is used by chemical thermal processes or concentrated photovoltaic generation.

![Figure 1: Solar tower plant (BSE, 2011)](image)

The heliostat field is the main cost factor of solar tower plants. For a cost efficient dimensioning of the heliostats, the wind loads must be known. Wind tunnel measurements that have been published so far have all performed at Reynolds numbers ($Re$) considerably below the maximum values that can occur in reality.

While the drag force coefficient of sharp-edged bodies does not depend on $Re$ because the separation is determined by the edges, for structures with round edges it may significantly vary beyond a certain critical $Re$ depending on the surface roughness ($k/d = \text{grain size of sand} / \text{diameter of cylinder}$), see Figure 2.
The usually horizontally aligned, circular torque tube of heliostats might be a source of such Re-dependent wind load coefficients. In regular operation, this torque tube is not directly exposed to the wind (Figure 3) and thus is of minor importance for the wind loads.

For storm protection, the heliostats are horizontally aligned to minimize the surface of wind attack. In this stow position the torque tube is exposed directly to the wind so the separation at the torque tube and the following recirculation could depend on $Re$. The recirculation area influences the pressure distribution on the back side of the mirror plane (Figure 4) and thus the hinge moment $M_{H_y}$ about the torque tube center line (elevation axis). $M_{H_y}$ at this position can be maximized and therefore this configuration is relevant to design. The main objective of the investigations is to determine whether a significant dependency of the wind load coefficient of $M_{H_y}$ on $Re$ exists.
2 Specifications

The Re-numbers are highest for big heliostats. Therefore, a typical, big heliostat with 120m² mirror area (Figure 3) was investigated. The main specifications are:

\[
\begin{align*}
h & \quad \text{height of mirror plane} \quad 9.6 \text{ m} \\
b & \quad \text{width of mirror plane} \quad 12.9 \text{ m} \\
H & \quad \text{height of elevation axis} \quad 5.4 \text{ m} \\
d & \quad \text{diameter of torque tube} \quad 0.6 \text{ m} \\
V_{\text{max}} & \quad \text{design wind speed at height } H \quad 40 \text{ m/s} \\
Re_{d, \text{max}} & \quad \text{full-scale Re based on } d \text{ at height } H \quad 1.7 \cdot 10^6
\end{align*}
\]

The investigated wind loads are:

\[
\begin{align*}
F_x & \quad \text{horizontal wind force perpendicular to el. axis} \quad [\text{N}] \\
F_z & \quad \text{vertical wind force} \quad [\text{N}] \\
M_y & \quad \text{wind moment at foundation} \quad [\text{Nm}] \\
M_{Hy} & \quad \text{wind moment about elevation axis} \quad [\text{Nm}]
\end{align*}
\]

The definitions of the wind load coefficients are according to Peterka and Derickson (1992, pp. 10ff):

\[
\begin{align*}
F_x &= c_{Fx} \cdot \frac{\rho}{2} \cdot V^2 \cdot A \\
F_z &= c_{Fz} \cdot \frac{\rho}{2} \cdot V^2 \cdot A \\
M_y &= c_{My} \cdot \frac{\rho}{2} \cdot V^2 \cdot A \cdot H \\
M_{Hy} &= c_{MHy} \cdot \frac{\rho}{2} \cdot V^2 \cdot A \cdot h
\end{align*}
\]

with

\[
\begin{align*}
c & \quad \text{wind load coefficient} \quad [-] \\
\rho & \quad \text{density of air} \quad [\text{kg/m}^3]
\end{align*}
\]
3 Method

3.1 Selection of tool
For the determination of the Re dependency, computational fluid dynamics (CFD) is not feasible because the prediction of the position of the separation point of round-shaped bodies is not reliable yet.

The determination of the Re dependency in the atmosphere at full scale is hardly possible because the appearance of the needed high wind speeds is seldom and not predictable. Investigations in a wind tunnel at real scale would demand a huge wind tunnel, which was not available. Measurements in conventional wind tunnels would be relatively cheap, but the needed Re cannot be reached; Re reduces with the model scale (Re is linear to the length scale):

\[ \text{Re} = \frac{\rho \cdot V \cdot l}{\eta} \]

with
- \( l \): characteristic length [m]
- \( \eta \): dynamic viscosity [kg·m/s]

Even if the required wind speed could be reached, the results of the measurements would not be reliable because the Mach number would be higher than 1 at regions of high wind speed (especially at the thickest cross section of the cylinder) so the flow could not be regarded as incompressible which is a requirement for the assumption of similarity (Hucho, 2002, pp. 439ff). By roughening of the round shapes the critical Re can be reduced (see Figure 2). But it is still too high to be reached by conventional boundary layer wind tunnels. Furthermore, the flow of the recirculation area would be influenced which would distort the results.

Re can also be increased by using a fluid of lower kinematic viscosity (\( \nu = \eta / \rho \)), like water (15 times lower than air), as realized in water tunnels. But at high fluid speed, cavitation occurs so the achievable Re is too low for the given task (Hucho, 2002, p. 470).

In kryo channels, the kinematic viscosity is reduced as well – through cooling of the fluid. However, the Mach number is also increased and therefore (because of the Mach number limitation) the specified Re number could not be reached at the available Kryo Channel of Cologne (Vieweger, 1989).

Instead of cooling the fluid it also can be pressurized to increase its density. At the High Pressure Wind Tunnel of Göttingen (HDG), up to 100 bars (=10MPa)
and a wind speed of 35m/s can be reached (Försching et al., 1981), which leads to sufficient high $Re$. The impact of the $Re$ number on the wind load coefficient of isolated circular cylinders (compare Figure 2) was investigated in the same wind tunnel by Schewe (1983). A scheme of the HDG and its main characteristics are shown in Figure 5.

![Figure 5: High Pressure Wind Tunnel of Göttingen (HDG)](image)

At the HDG it was not possible to simulate the turbulence of the atmospheric boundary layer. It is true that the lateral fluctuating component of the turbulent wind induces additional lift forces on the torque tube of circular cross-section (Basu and Vickery, 1983) and on the heliostat in all (Peterka and Derickson, 1992; Pfahl et al., 2011). Furthermore, by Cheung and Melbourne (2005) an increase of the span-wise force correlation with increased turbulence intensity was determined. But regarding $Re$ dependency, it is expected that by measurements with low turbulence intensity, all effects that would appear at high turbulence intensity are captured because for circular cylinders the critical $Re$ reduces for higher turbulence intensity to lower values (Fage and Warsap, 1929).

### 3.2 Model and test set-up

A model scale of 1:50 was chosen to ensure the boundary layer of the side walls would not affect the measurements and the blockage was not too high (Isyumov, 1999, p.14). The support structure of the mirrors was roughly modeled by using the advanced sinter metal rapid prototyping technique (Figure 6). In general, the small gaps between the mirror facets are not of significant influence on the wind loads (Wu et al., 2010) nevertheless, they were modelled because it could not be excluded that they have an impact on the $Re$ dependency.
The heliostat model was arranged above a splitter plate, simulating the ground, and connected to a strain gauge balance outside the test section. The whole set-up is integrated into the side wall. Here the heliostat model is mounted by its pylon to the external balance (Figure 7). Although possible in the HDG, no wind-over-ground profile was simulated because for the stow position, it should be of negligible influence. A 90° angle of wind attack to the torque tube at horizontal mirror plane was investigated because at this configuration the influence of the torque tube should be highest.
3.3 Correcting model deflection due to wind loads

The model is more stressed by the wind loads than the original heliostat because:

\[
\sigma = \frac{M}{S} \quad M \sim p \cdot l^3 \quad p \sim \rho \cdot V^2 \quad S \sim l^3
\]

so

\[
\sigma \sim \rho \cdot V^2
\]

with

\begin{align*}
\sigma & \quad \text{maximal bending stress [N/m}^2] \\
M & \quad \text{bending moment [Nm]} \\
S & \quad \text{section modulus [m}^3] \\
l & \quad \text{characteristic length [m]} \\
p & \quad \text{dynamic pressure [N/m}^2]\end{align*}

Assuming a pressure of 70bar (=7MPa) in the wind tunnel and a wind speed of 35 m/s to reach \(Re_d = 1.7 \cdot 10^6\), the stress of the model material would be about 50 times higher than the one of the full scale heliostat at the same \(Re\) (wind speed of 40 m/s). This was partly compensated by using solid profiles, slightly thicker cross sections and a material with high modulus of elasticity for the
model. Nevertheless, at high $Re$, deflection of the model could not be avoided which is critical because it influences the results significantly.

To eliminate the influence of the deflection, the inclination caused by the measured loads at high $Re$ was calculated via FEM (finite element method). The model was validated by calculating and measuring the deflection at a nominal panel inclination angle of the mirror plane of $10^\circ$ and at $Re_d = 1.7 \cdot 10^6$. Taking the backlash of the bearing also into account, a good accordance between measurements and simulation could be assessed (Figure 8).

Figure 8: Calculated (left and middle) and measured (right) deflection of wind tunnel model at $Re = 1.7 \cdot 10^6$

With the FEM model, the influence of the deflection could be eliminated by the following steps:

- Measurement of the moment about the pylon base for a nominal panel inclination of $0^\circ$ at $Re_d = 1.7 \cdot 10^6$
- Calculation of the pressure distribution according to the typical pressure distribution of an even plate at small angles of wind attack and according to the measured moment about the pylon base
- Calculation of the deflection caused by this pressure distribution via FEM model and determination of the resulting inclination of the mirror plane
- Measurement of the wind loads at the calculated inclination at low $Re$
- Comparison of the wind load coefficients at $Re_d = 1.7 \cdot 10^6$ and a nominal panel inclination of $0^\circ$ and at the calculated inclination and low $Re$: If a $Re$ dependency exists the values should be different.

4 Results

All six components of the aerodynamic loads were systematically measured at $Re_d = 0.2 \cdot 10^6 - 1.7 \cdot 10^6$, at nominal inclination (at unloaded mirror plane) and yaw angles of $0^\circ$ (storm idle position). The diagram (Figure 9, solid lines) shows the
coefficients of drag ($c_{Fx}$), lift ($c_{Fz}$), and pitching moment about pylon base ($c_{My}$) over $Re$.

According to Schlichting and Truckenbrodt (1969, pp. 72ff), a linear, increasing pressure toward the edge of attack can be assumed as pressure distribution for even plates at small angles of wind attack. With this approach and taking the measured loads into account, the according pressure distribution was determined and applied to the FEM model. An average deflection of the mirror plane of $4^\circ$ was calculated.

For nominal inclination of $4^\circ$ and low $Re_d=0.45\cdot10^6$, the coefficients of drag ($c_{Fx}$), lift ($c_{Fz}$), and pitching moment ($c_{My}$) were measured and are given in Figure 9 as single measuring points.

The solid lines of Figure 9 represent the measured values for the nominal panel inclination of $0^\circ$, but with the actual load induced inclination between $0^\circ$ (low $Re$-number) and $4^\circ$ (highest $Re$-number). If the measured value at $Re_d=0.45\cdot10^6$ at nominal panel inclination of $4^\circ$ (which needs no correction) is compared with the measured value at $Re_d=1.7\cdot10^6$ at nominal panel inclination of $0^\circ$ which has to be corrected to $4^\circ$, it can be concluded that the design-driving components drag, lift and pitching moment coefficients are not depending on $Re$ (dashed line).

5 Discussion

At the stow position, the drag force $F_x$, lift force $F_z$, pitching moment $M_y$ and hinge moment $M_{Hy}$ reach their maximal value at storm conditions. Thus, their values at stow position are relevant for the design of heliostats. Since $M_{Hy}$ is hard to measure directly, it is calculated by the drag force $F_x$ and by the moment at the
pylon feet $M_y$ (Peterka and Derickson, 1992, p. 10). As the wind load coefficients of $F_x$ and $M_y$ show no $Re$ dependency, the wind load coefficient of $M_{Hy}$ is not $Re$ dependent as well.

c$F_z$ shows a slight decrease with $Re$ (dashed line). But compared to the increase due to deflection (solid line), it is small and is within the range of the uncertainties of the method.

6 Conclusions
No design-relevant $Re$ dependency of the wind load coefficients of heliostats at stow position was measured. Thus, it is valid to determine the wind load coefficients at conventional boundary layer wind tunnels at low $Re$.

But at the layout of heliostats their possible deflection through wind loads and the resulting increase of the inclination of the mirror plane at high $Re$ must be considered. Hence, stiffness and damping of the structure must be high enough to avoid torsional divergence, flutter, galloping and resonance due to vortex shedding of the structure itself or of upstream structures at any possible $Re$ number (Cook, 1985).

The results of this investigation can not be transferred to solar trough collectors because the round shape of the trough is surely of bigger influence than the torque tube of a heliostat. Hosoya et al. (2008, pp. 39f) performed wind tunnel measurements for trough collectors with various $Re$, but the critical $Re$ was not reached (compare with Figure 2). An approval of the $Re$ independency of the wind load coefficients of solar trough collectors is still absent and could be also examined in the High Pressure Wind Tunnel of Göttingen.

7 Acknowledgment
The authors thank the DLR division “Energy” for the financing of the measurements.

8 References


