



Dynamics of slab tear faults: Insights from numerical modelling

Alina J. Hale ^{a,*}, Klaus-D. Gottschaldt ^{b,1}, Gideon Rosenbaum ^c, Laurent Bourgoin ^b,
Matthieu Bauchy ^b, Hans Mühlhaus ^b

^a The School of Geosciences, The University of Sydney, Australia

^b ESSCC, School of Earth Sciences, The University of Queensland, Australia

^c School of Earth Sciences, The University of Queensland, Australia

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ABSTRACT

Tear resistance at the edge of a slab is an important parameter controlling the evolution of subduction zones. However, compared with other subduction parameters such as plate strength, plate viscosity, plate thickness and trench width, the dynamics of tearing are poorly understood. Here we obtain a first-order understanding of the dynamics and morphology of subduction zones to resistance during tear propagation, by developing and using a novel computational modelling technique for subducting slabs, with side boundaries described by visco-plastic weak zones, developing into tear faults. Our 3D model is based upon a visco-plastic slab that sinks into the less dense mantle, generating poloidal and toroidal flows. The asthenospheric mantle field is static and only develops flow due to the subducting slab. We use the finite element code eScript/Finley and the level set method to describe the lithosphere to solve this fluid dynamics problem. Our results show the importance of tear resistance for the speed of trench migration and for shaping the final geometry of subduction systems. We show that slab tearing along a weak layer can result in a relatively straight slab hinge shape, while increasing the strength in the weak layer results in the curvature of the hinge increasing substantially. High tear resistance at the slab edges may hinder rollback to the extent that the slab becomes stretched and recumbently folded at the base of the domain. Tear resistance also controls whether the subducting lithosphere can experience accelerating rollback velocities or a constant rollback velocity.

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1. Introduction

The lifecycle of subduction zones typically involves subduction initiation, accelerated sinking of the slab tip through the upper mantle, interaction with the 660-km discontinuity, and steady subduction until the arrival of buoyant lithosphere that prevents further subduction (Funicello et al., 2003). During this lifecycle, most subduction hinges migrate with respect to the lower mantle, typically in a direction opposite to the dip of subduction (Garfunkel et al., 1986; Royden, 1993; Schellart, 2008; Schellart et al., 2008). This process, known as subduction rollback, is affected by the interaction of the slab with induced or background asthenospheric mantle flow (Dvorkin et al., 1993; Schellart, 2004a). Subduction rollback also plays a crucial role in the development of back-arc extensional basins, in particular when the velocity of subduction rollback exceeds the velocity of plate convergence (Dewey, 1980).

Uniform subduction rollback and its associated mantle flow are relatively well understood and has been simulated in numerous

experimental and numerical studies (Funicello et al., 2003; Schellart, 2004a; Morra et al., 2006; Piromallo et al., 2006; Stegman et al., 2006; Schellart et al., 2007). However, much less is known about the dynamic response to non-uniform rollback velocities along the length of the subduction system. Such responses include the progressive curvature of subduction zones (e.g. Morra et al., 2006; Schellart et al., 2007) and the development of vertical slab tear faults (Govers and Wortel, 2005; Rosenbaum et al., 2008). The latter would propagate horizontally provided that subduction continues and the lithospheric strength is less than the slab strength. Otherwise subduction may stall or the slab may break off.

In this paper, we numerically model the evolution of a subducting slab with side boundaries controlled by tear faults. In published subduction models (e.g. Morra et al., 2006; Stegman et al., 2006; Schellart et al., 2007), tear resistance at the slab boundaries is implicitly neglected allowing free slab propagation. However, slab propagation is likely to be significantly affected by any resistance to tearing. The instantaneous lithospheric response to a subduction edge has been considered by Govers and Wortel (2005), however their models neglect the dynamics of trench migration and tear propagation. In the following models we address this issue, showing how tear resistance at a propagating fault affects trench migration and the geometry of subduction.

* Corresponding author.

E-mail address: a.hale@usyd.edu.au (A.J. Hale).

¹ Now at: Deutsches Zentrum für Luft- und Raumfahrt, Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany.

2. The mechanism of tear propagation

Tear propagation in subducting slabs is dominated by shear stresses acting parallel to the fault plane and parallel to the crack front (similar to a Mode 3 Crack in fracture mechanics). The $\sigma_{z\theta}$ component of the stress tensor describes the shear stress acting on all planes that radiate from the crack front, where Z is the axis perpendicular to the crack trace in plan-form view and θ is the polar angle measured from the projection of the crack trace ahead of the crack tip (Fig. 1). Propagation of a tear fault is facilitated through the failure of such planes, connected to the crack tip. Considering a half-infinite crack in an infinite 2D domain, the relevant component of the stress tensor near the tip is $\sigma_{z\theta} \propto R^{-0.5} \cos(\theta/2)$, with R being the distance from the tip (Zehnder, 2006). Since the maximum value of $\sigma_{z\theta}$ is immediately in front of the crack tip, the tear fault is most likely propagating parallel to the direction of subduction rollback, consistent with observations (Govers and Wortel, 2005; Rosenbaum et al., 2008).

The direction of tear propagation can be modified by more complex flow dynamics in the subduction system due to the interaction of rollback, tear resistance at the fault and induced mantle flow. Furthermore, the dependence of $\sigma_{z\theta}$ on θ is rather weak. Inhomogeneities may reduce the strength of the lithosphere near the crack front resulting in a weak zone and failure occurring away from the preferred propagation direction; a tear fault is likely to follow the path of least resistance in a direction generally in front of the propagating fault. Local changes to the propagation direction may ultimately affect the general direction of tear propagation, thereby changing the whole subduction zone. These weakest points could be along pre-existing faults (e.g. passive margins, Gurnis et al., 2000), weakened zones (e.g. back-arc basins), margins of strengthened lithosphere (e.g. seamount chains) or where mantle plumes impinge on the lithosphere. Mantle flow around edges of retreating slabs may itself produce volcanism that weakens the lithosphere at the tear fault (Govers and Wortel, 2005). The effective viscosity of vertically averaged continental lithosphere is estimated to be at least an order of magnitude smaller than that of oceanic lithosphere (Gordon, 2000). Since continental crust is more buoyant and unlikely to be subducted, tear faults are preferentially likely to propagate in the oceanic lithosphere, possibly along continental margins. Here we only consider tear faults in oceanic lithosphere.

3. Methodology

Our models aim to generate a first-order understanding of resistance to tear propagation on the dynamics and morphology of subduction zones. We use idealized numerical models to isolate the effects of tear resistance on a subducting slab. Subduction zones are localised features and therefore we neglect the sphericity of the Earth.

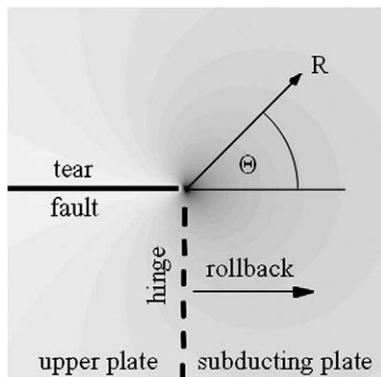


Fig. 1. Plan-view geometry of an idealized subduction zone edge. Grey contours show the variation of $\sigma_{z\theta}$ around the tip of the propagating tear fault (STEP), with darker shades corresponding to higher stress.

Subduction is modelled as fluid flow with infinite Prandtl number in a 3D Cartesian geometry with a dense oceanic lithosphere region sinking into less dense sublithospheric mantle. We do not consider an elasticity component in our simulations. This setup permits subduction rollback with tear propagation and induced mantle flow occurring naturally, driven by the negative buoyancy of the slab.

3.1. Equation solved

The dynamics of this system is governed by the conservation of mass in an incompressible medium;

$$\nabla \cdot \vec{v} = 0, \quad (1)$$

and conservation of momentum;

$$\nabla \cdot \tau - \nabla P = \Delta \rho \vec{g}, \quad (2)$$

with the deviatoric stress tensor;

$$\tau = \tau_{ij} = \eta \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right), \quad (3)$$

where velocity is \vec{v} , pressure is P , the lateral density variation is $\Delta \rho$, gravitational acceleration is \vec{g} and dynamic viscosity is η . The density variations driving subduction are mainly due to cooling of the lithosphere. We impose an unstable density stratification as an initial condition. Although thermal diffusion is present in real subduction, it acts on a longer timescale than advection. Hence, we neglect the energy equation, because it is expected to have negligible effects on the density distribution over the duration (<50 Myr) of our numerical experiments.

We use a linear viscous rheology for the mantle. Parts of the lithosphere are viscous, while other parts are brittle. The brittle parts of the lithosphere can be modelled in the continuum limit by introducing a visco-plastic rheology with the non-linear effective viscosity (Moresi and Solomatov, 1998);

$$\eta = \eta_{\text{creep}} \quad \text{if } \tau_{\text{creep}} < \tau_{\text{yield}} \\ \eta = \eta_{\text{yield}} \quad \text{if } \tau_{\text{creep}} \geq \tau_{\text{yield}} \quad (4)$$

Viscous deformation occurs when the second invariant of the stress tensor $\tau_{\text{creep}} = 2\eta_{\text{creep}} \dot{\epsilon}_{II}$ falls below the isotropic yield stress τ_{yield} , where $\dot{\epsilon}_{II} = \sqrt{\frac{1}{2} \dot{\epsilon}_{ij} \dot{\epsilon}_{ij}}$ is the second invariant of the strain rate tensor. When stresses reach τ_{yield} in the viscous mode, the effective viscosity is lowered in an iterative procedure to;

$$\eta_{\text{yield}} = \frac{\tau_{\text{yield}}}{2 \dot{\epsilon}_{II}} \quad (5)$$

For our numerical simulations we vary the yield strength within a weak layer of the subducting slab.

3.2. Numerical methods

For the simulations presented in this paper we use the FEM software eScript and the FEM library Finley (Gross et al., 2007). We use a first-order element type with 20 km spacing. The Uzawa algorithm (a saddle-point algorithm) is used to solve the pressure-velocity field and we use a Courant condition to calculate the time-step $dt = 0.3 \frac{h}{v_{\text{max}}}$ for the displacement of the subducting lithosphere, where h is the element spacing and v_{max} is the maximum velocity in the model domain.

We use the level set method to track the moving and deforming interface between the lithosphere and mantle. This method is based

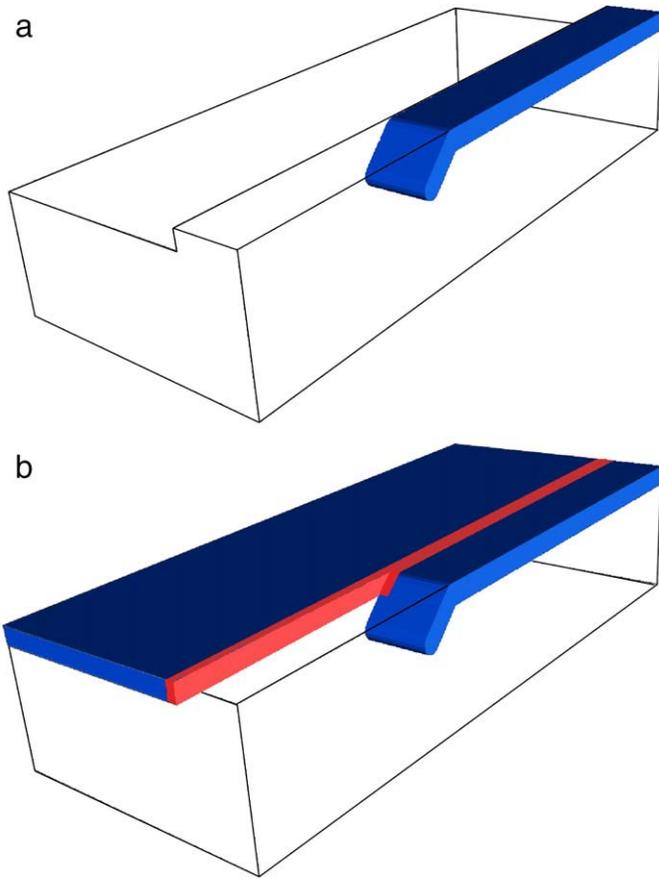


Fig. 3. Model domain initial conditions are shown for the two model meshes considered. For simulations with free-slip boundary conditions in the weak region mesh a) is used. For all simulations, except when free-slip boundary conditions are applied at the weak-boundary, the model domain b) is used. In Figure b) the weak region is shown by the red area. The subducting lithosphere is blue (shown as partly dipping), and in addition to this there is lithosphere with fixed boundary conditions on the other side of the weak region, which does not subduct. Note that in both figures mantle material surrounding the slab is shown as transparent.

with an average of 65 Myr (Lallemand et al., 2005). This corresponds to l_{lith} being between 30 and 125 km, and using a lithosphere thickness of 100 km corresponds to a lithosphere age of approximately 65 Ma.

The density difference $\Delta\rho$ between lithospheric slab and upper mantle can be estimated from Airy compensation at different water depths at mid oceanic ridges before reaching a subduction trench. Sea floor depth for a 100 km thick lithospheric plate is approximately 5.5 km (Schubert et al., 2001), which translates into $\Delta\rho = 69 \text{ kg m}^{-3}$ (Royden and Husson, 2006). An independent estimate based on petrological and geophysical data suggests a lower depth-averaged density contrast of $\Delta\rho = 40 \text{ kg m}^{-3}$ between plate and adiabatic mantle (Afonso et al., 2007); however, we use the more established higher value.

The rheology is likely to be highly variable throughout the oceanic lithosphere. Elasticity plays a role near the surface (the upper 10–20 km) forming faults by the process of brittle failure due to micro-physical processes. Elasticity also serves to advect momentum, generating bending at shallow levels, and straightening of the slab at deeper levels. While flexural stresses on the non-subducting slab region contribute to the stress field near the subduction hinge. Below this depth deformation is most likely accommodated by distributed microcracks (i.e. a semi-brittle rheology, Kohlstedt et al., 1995) and lattice processes (i.e. semi-ductile rheology). Macroscopic plastic flow

Table 1
Parameters common to all models.

Parameter	Symbol	Value
Gravitational acceleration	g	10 m s^{-2}
Domain depth	l_z	660 km
Domain length	l_x	3120 km
Domain width	l_y	1300 km
Lithosphere thickness	l_{lith}	100 km
Initial length of lithosphere	l_s	2000 km
Plate viscosity	η_{lith}	$8 \times 10^{22} \text{ Pa s}$
Upper mantle viscosity	η_{UM}	$4 \times 10^{20} \text{ Pa s}$
Density of lithosphere	ρ_{lith}	3220 kg m^{-3}
Density of upper mantle	ρ_{UM}	3289 kg m^{-3}

occurs when the pressure exceeds the plastic yield strength of the rocks (Tackley, 2000b) which can be modelled from a continuum mechanical perspective. This thermally activated viscous creep occurs at approximately 40 km depth, in medium age lithosphere (Kohlstedt et al., 1995). Elastic deformation on tear faults is in the order of kilometres (Govers and Wortel, 2005), with earthquakes and brittle deformation dissipating elastic energy on time scales of less than 1000 years. Since we are interested in time scales of 10^5 – 10^7 years, where elastic deformation is small compared to plastic and viscous flow, the assumption of a visco-plastic lithospheric rheology (Eq. (4)) is appropriate for the time scales presented in this study.

An appropriate effective viscosity range for oceanic lithosphere, η_{lith} , has been constrained to be between 10^{22} and 10^{23} Pa s (Steinberger and Calderwood, 2006). Stegman et al. (2006) use an upper mantle shear viscosity, η_{UM} , which is between 100 and 200 times smaller than the lithosphere shear viscosity. Hence, we use a shear upper mantle viscosity of $\eta_{\text{UM}} = 4 \times 10^{20} \text{ Pa s}$ and an ocean lithosphere viscosity of $\eta_{\text{lith}} = 8 \times 10^{22} \text{ Pa s}$. Higher effective viscosities are expected for the interior of plates (Steinberger and Calderwood, 2006), but lithospheric deformation is localized at the hinge in our model setup. Therefore we assign a constant value from within this weak range to the entire lithosphere and expect only limited further weakening by yielding.

Lithospheric strength in the brittle zone is determined by the frictional strength of faults, and is approximately proportional to pressure (Byerlee, 1968). In the semi-brittle/semi-ductile zone, the yield strength depends only weakly on pressure and decreases in the viscous lower lithosphere due to increasing temperature (Kohlstedt et al., 1995). To keep our models simple, we approximate this strength profile with a constant isotropic yield strength, τ_{yield} . The value for such an effective yield strength is undetermined but is likely to be in the range 1–1000 MPa (Kaus and Podladchikov, 2006). Large-scale tectonic systems are likely to have lower strengths than intact laboratory samples (with strengths of approximately 500 MPa) due

Table 2

Parameters that are varied. Since the model is symmetric at one side, only half of the subduction zone is modelled.

Run	τ_{yield} [MPa] Weak zone	τ_{yield} [MPa] Plate	$\Delta\rho$ [kg m^{-3}] Plate/mantle	l_{lith} [km] Plate	l_{slab} [km] Plate
0	0	100	69	100	600
1	1	100	69	100	600
2	5	100	69	100	600
3	10	100	69	100	600
4	25	100	69	100	600
5	50	100	69	100	600
6	75	100	69	100	600
7	100	100	69	100	600
8	Fixed	100	69	100	600
9	25	100	69	100	400
10	25	10	69	100	800
11	5	10	40	100	600

τ_{yield} is the yield stress, l_{slab} the width of the trench.

to strain weakening or pre-existing faults (Tackley, 2000b). Furthermore, energy feedbacks, such as shear heating and thermal expansion, also play an important role in weakening the lithosphere (Regenauer-Lieb et al., 2006; Regenauer-Lieb et al., 2008). The lowest yield strength values, estimated to be around 10 MPa from the stress release of earthquakes, describe the strength of the lithosphere with well-developed faults (Lachenbruch and Sass, 1991). Self-consistent models of plate tectonics (based on visco-plastic yielding) are successful for yield stresses in the order 100–150 MPa (Tackley, 2000a,b). This might be an appropriate approximation for the effective strength of oceanic lithosphere without well-developed faults.

We assign $\tau_{\text{yield}} = 100$ MPa to our modelled lithosphere and we assign a tear region in our model domain along which slab tearing can occur (Fig. 3). The tear region is introduced along the path where tearing is most likely to occur, as discussed in Section 2. Fig. 3a shows the model domain used for $\tau_{\text{yield}} = 0$ MPa (i.e. no tear resistance). For this specific simulation, it was necessary to define the free-slip edge as

a boundary condition. Otherwise the viscosity would drop to zero for $\tau_{\text{yield}} = 0$ MPa (Eq. (5)) in the weak zone, leading to a situation that our numerical model would be unable to solve. Fig. 3b shows the model domain used for simulations with $\tau_{\text{yield}} > 0$ MPa, with the weak region shown as red (corresponding to one element wide) and a fixed and deformable slab shown as blue. Both vertical, lithosphere cutting features approximate pre-existing weak zones. Other inhomogeneities of the subducting plate, like buoyant terranes or areas of higher strength, are not considered in this study.

Introducing these two model domains and boundary conditions allows us to address the two end-member states. That is, when the weak layer is entirely yielding ($\tau_{\text{yield}} = 0$ MPa) versus when it is not (when fixed boundary conditions are used at the edge of the slab). Between these two end-member states there will be a combination of yielding and non-yielding regions of the weak layer as shown in our results.

We neglect the upper plate in our models since its influence is beyond the scope of this study, but it needs to be considered in the

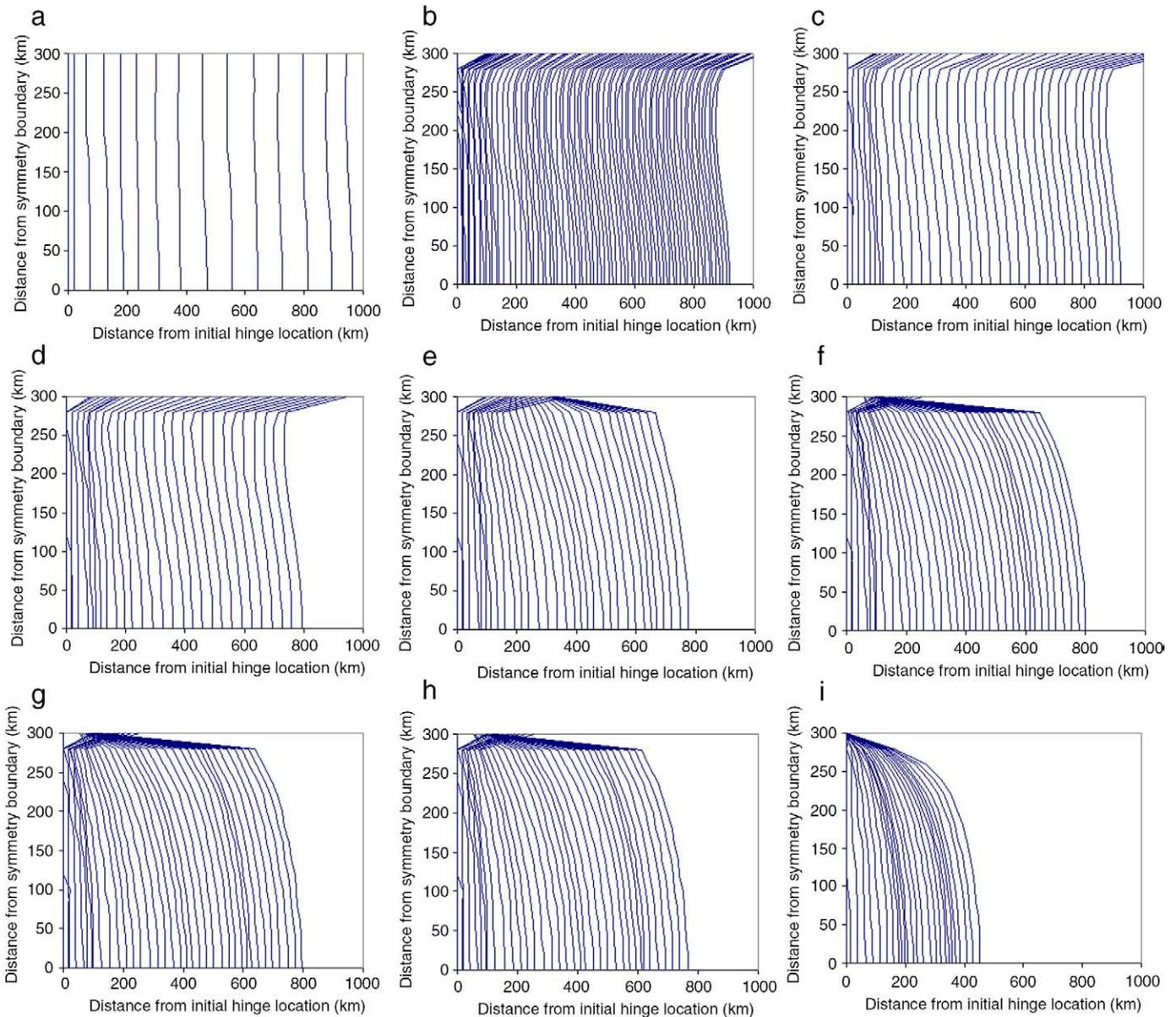


Fig. 4. Results showing the shape of the evolving slab hinge at 10 time-step intervals at the free-surface. All simulations have a yield strength of 100 MPa for the plate and a density difference between plate and mantle of $\Delta\rho = 69 \text{ kg m}^{-3}$, unless otherwise stated. The slab hinge is initiated at a distance of 0 perpendicular to the reflected boundary. The weak layer is between a distance of 300 and 320 km (i.e. outside the domain shown in these figures). Key in Table 2. a) Free-slip in weak zone (i.e. 0 MPa). b) Weak region = 1 MPa. c) Weak region = 5 MPa. d) Weak region = 10 MPa. e) Weak region = 25 MPa. f) Weak region = 50 MPa. g) Weak region = 75 MPa. h) Weak region = 100 MPa. i) Fixed boundary in weak zone.

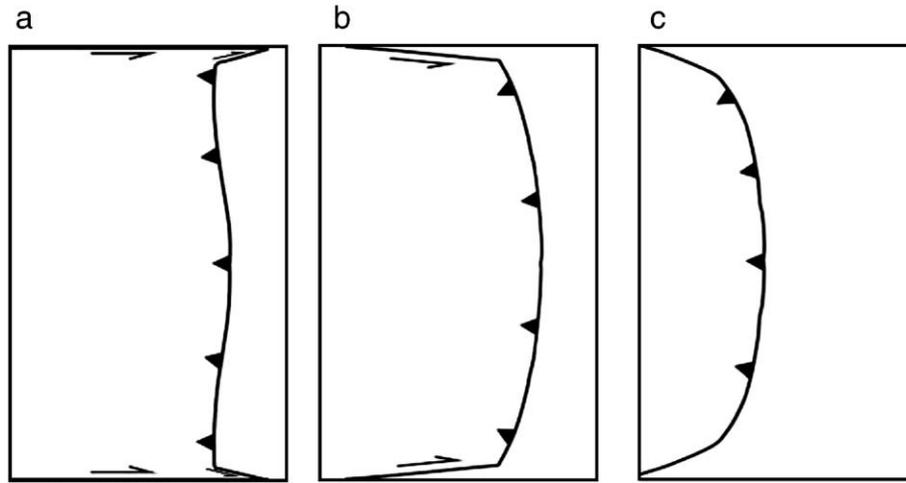


Fig. 5. Schematic showing that slab tearing with low yield strength promotes accelerated rates of subduction rollback while the arc shape remains relatively straight (a). Both effective rollback and arc curvature are obtained with higher values of yield strength (25–100 MPa; b), whereas boundaries with maximum resistance result in curvature at the central slab segment but no tearing (c). The arrows correspond to region of tearing.

interpretation of our results. This simplification also makes it easier to isolate the effects of tearing at the edges of the subduction zone. Plate velocities are limited by the resistance of the mantle rather than by the frictional resistance at the trench (Moresi and Solomatov, 1998). Hence no special constitutive model is necessary for the decoupling zone, where upper and subducting plates interact.

Plate motion is determined by the integral of all forces acting on the plate. These include drag from the underlying mantle and forces of different magnitudes and directions from the different rim segments, i.e. convergent, divergent and transform boundaries. It is highly unlikely that a single subducting slab will determine the motion of the plate. Any particular subduction zone will instead generate a velocity between subducting plate and mantle. This velocity could be termed mantle wind in a plate-fixed reference system, or plate motion in a mantle-fixed system. Since our model contains only a part of one plate with a single subduction zone we fix the sides of the plate to the respective domain boundaries. Our setup deliberately neglects mantle wind, to better isolate the effects of tear resistance at the slab edges.

3.5. Modelling strategy

The parameter values that are maintained constant for all the simulations considered are listed in Table 1. Table 2 shows the combination of varied parameters for each simulation.

4. Model results

4.1. Arc shape

Model results showing the map-view shape of the subduction hinge are presented in Fig. 4. Results are shown at 10 time-step intervals and highlight the relative importance of mantle flow and tear resistance for shaping the subduction hinge. The length of each time-step is governed by the velocity field and typically ranges from 0.10 to 0.45 Ma.

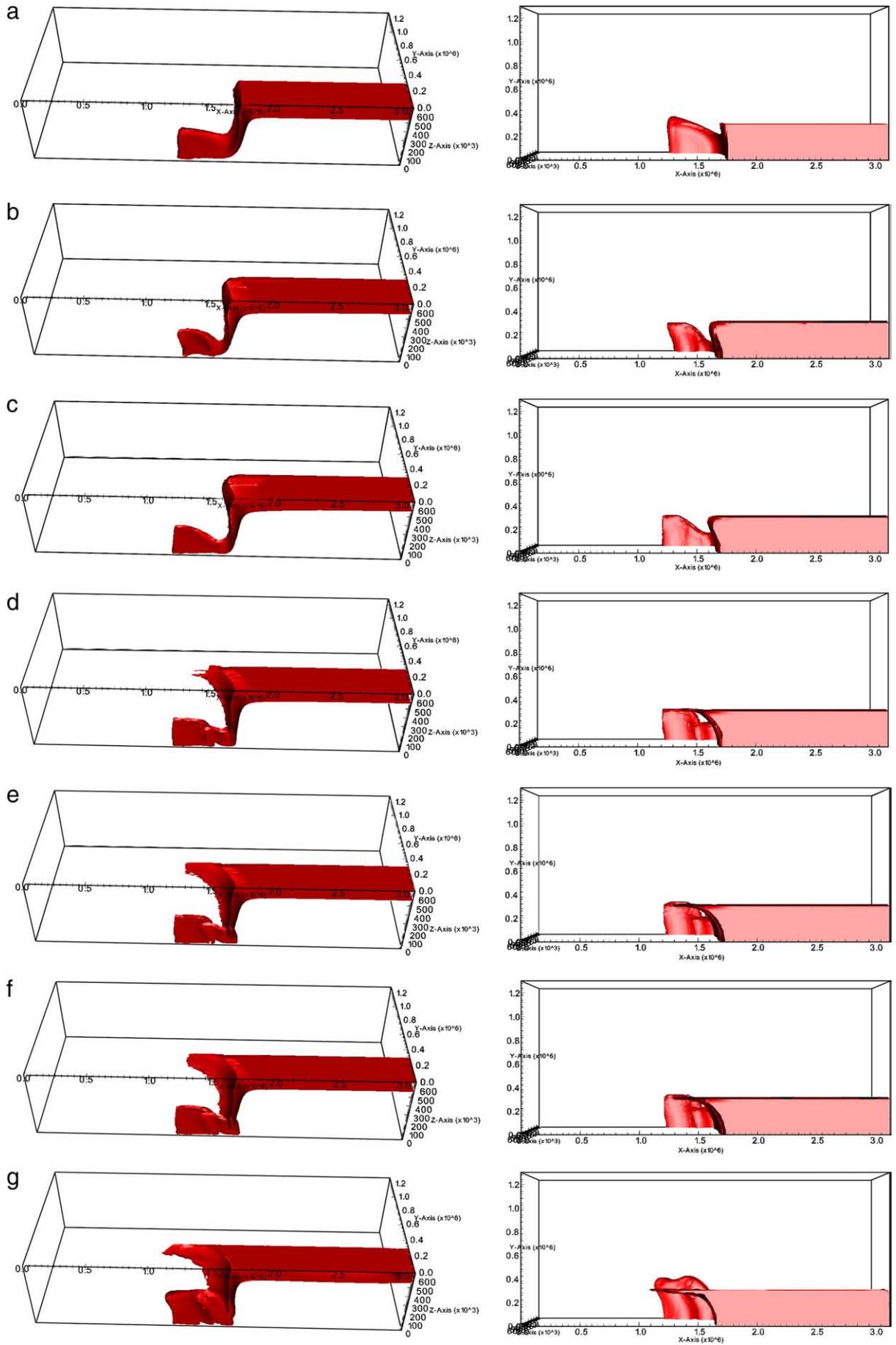
Fig. 4a shows the shape of the slab hinge at the free-surface when using a free-slip boundary condition adjacent to the slab edge (i.e. a model set-up as described in Fig. 3a is used). The shape of the slab hinge is solely governed by the interaction with the induced mantle flow, since there is zero tear resistance. Under these conditions negligible arc curvature develops (Fig. 4a), in contrast with previous numerical results (e.g. Stegman et al., 2006). The reason for this discrepancy is because hinge curvature in the models of Stegman et al. (2006) are strongly affected by toroidal flow around the slab edge

which extends to the free-surface of the domain, i.e. the slab is completely embedded in the mantle. In contrast, our model setup acts to suppress toroidal flow near the surface by imposing a no-slip boundary to a depth of 100 km below the domain free-surface in both sides of the subducting slab. Therefore, while our models are useful in quantifying slab deformation in response to tear resistance, they may underestimate additional deformation induced by toroidal flow. For comparison with previous studies (e.g. Stegman et al., 2006) we also simulate a subducting slab with a domain setup as described in Fig. 3b, but without the fixed plate or a weak layer region (see Appendix B). Then the slab edge is embedded into mantle material, which flows around the slab during rollback, initially producing a more prominent arc shape.

Our model with a free-slip tear zone (Fig. 4a) shows uniform rollback velocities along the hinge. However, results in Fig. 4b–d show that the largest rollback velocities occur close to the slab edge (280–300 km). This is due to the very low yield strength values (1 MPa–10 MPa), and hence low viscosities, in the weak zone of these models (see Eq. (5)). Our models with a low yield strength weak layer impose no restrictions upon the movement of the slab edge into the less viscous mantle, other than the yield strength. Hence, the slab edge experiences less resistance to deformation in the y -direction, compared to other parts of the relatively stiff slab. This leads to preferential detachment and deformation in the weak zone, faster sinking at the edge and hence faster rollback.

Simulations that impose a higher yield strength in the weak zone (25 MPa–100 MPa, Fig. 4e–h) show an initial increase in rollback velocities close to the slab edge (similarly to Fig. 4b–d) followed by deceleration and pinning of rollback velocities at the slab edge. This is a consequence of decreasing the slab pull forces and other negative buoyancy forces acting on the slab (e.g. Schellart, 2004b). The relative importance of yielding and tearing near the surface decreases as the slab volume in the mantle grows. This is due to both toroidal flow and slab stretching. Induced toroidal flow hinders rollback at the slab edge and pushes the slab back in the middle. Interaction with induced mantle flow becomes more important if a bigger slab area is ploughing through the mantle, i.e. when the slab has sunken deep enough. Slab stretching (as discussed further in Section 4.2) acts to decrease the volume of slab sinking into the mantle which reduces the negative buoyancy forces. These effects explain increasing rollback velocities away from the slab edge and even roll-forward in some models, when mantle flow has become established.

In Fig. 4i, the slab is pinned at the boundary. Therefore toroidal flow is minimal and plays no role in shaping the slab edge. The shape



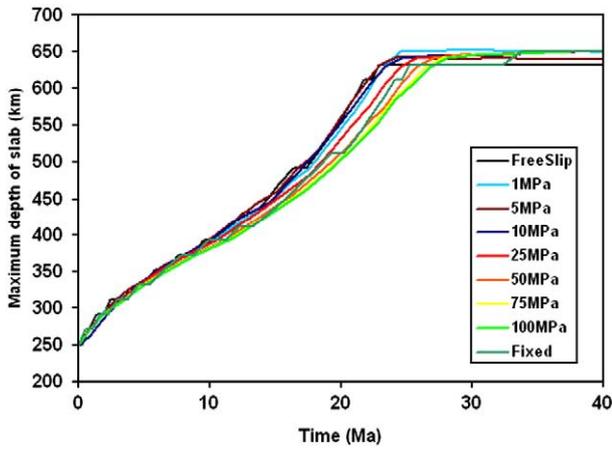


Fig. 7. Results show the maximum depth reached by the subducting slab below the free-surface against time for all simulations (the slab is initiated at a maximum depth of 250 km below the free-surface). The key for the graph is given in Table 2.

of the hinge zone is still that of an arc, because rollback is least hindered in the centre of the slab.

In summary, results show that slab tearing with low yield strength promotes accelerated rates of subduction rollback while the arc shape remains relatively straight (Fig. 5a). Both effective rollback and arc curvature are obtained with higher values of yield strength (25–100 MPa; Fig. 5b), whereas boundaries with maximum resistance result in curvature at the central slab segment but no tearing (Fig. 5c). Our results affirm earlier suggestions that interactions between subduction rollback and toroidal flow are important controls on arc curvature (Schellart and Lister, 2004; Stegman et al., 2006; Schellart et al., 2007). In addition, we recognize tear resistance as another controlling parameter for the dynamics of subduction zones. While for a free-slip boundary condition, the curvature of the slab is purely controlled by toroidal flow (Stegman et al., 2006), increasing the yield strength along the tear fault corresponds to settings in which the subducting slab is controlled more by the weak layer and less by the toroidal flow around the slab.

4.2. Slab morphology

We used the OpenGL software package VisIt (<https://wci.llnl.gov/codes/visit/>) to visualize snapshots of the subducting lithosphere within the model domain as shown in Fig. 6. The snapshots show the subducting lithosphere after rollback of the slab hinge to a maximum distance of 500 km (i.e. the slab hinge at the symmetry boundary reaches a distance of 1700 km in the model domain since it was initialised at a distance of 1200 km). Results show that as the yield strength in the weak layer is increased, the curvature created by the hinge also increases (as shown in Fig. 4). However, Fig. 6 also shows that as the yield strength in the weak layer is increased, the subducting slab can become recumbently folded at the base of the domain. This is a consequence of the increasing resistance to slab rollback at the slab boundary as the yield strength in the weak layer is increased. As a result, the slab length increases by stretching without rollback being sufficiently fast to compensate. Slab stretching can be observed in Fig. 6b,c for yield strength of 1 MPa and 5 MPa in the weak layer, respectively. The subducting slab in Fig. 6c, which has the higher yield strength, experiences more stretching than the subducting slab in Fig. 6b. Fig. 6 also shows that as the yield strength in the weak layer is increased, the slab becomes more resistant to tearing and a thin

Fig. 6. The OpenGL software package VisIt (<https://wci.llnl.gov/codes/visit/>) is used to visualize snapshots of the subducting lithosphere within the model domain from the side (left snapshots) and from above (right snapshots). The snapshots show the subducting lithosphere after the slab hinge has rolled-back a maximum distance of 500 km. The yield strength used in the weak layer is shown below the snapshots. a) Free-slip in weak zone (i.e. 0 MPa). b) Weak region = 1 MPa. c) Weak region = 5 MPa. d) Weak region = 25 MPa. e) Weak region = 50 MPa. f) Weak region = 100 MPa. g) Fixed boundary in weak zone.

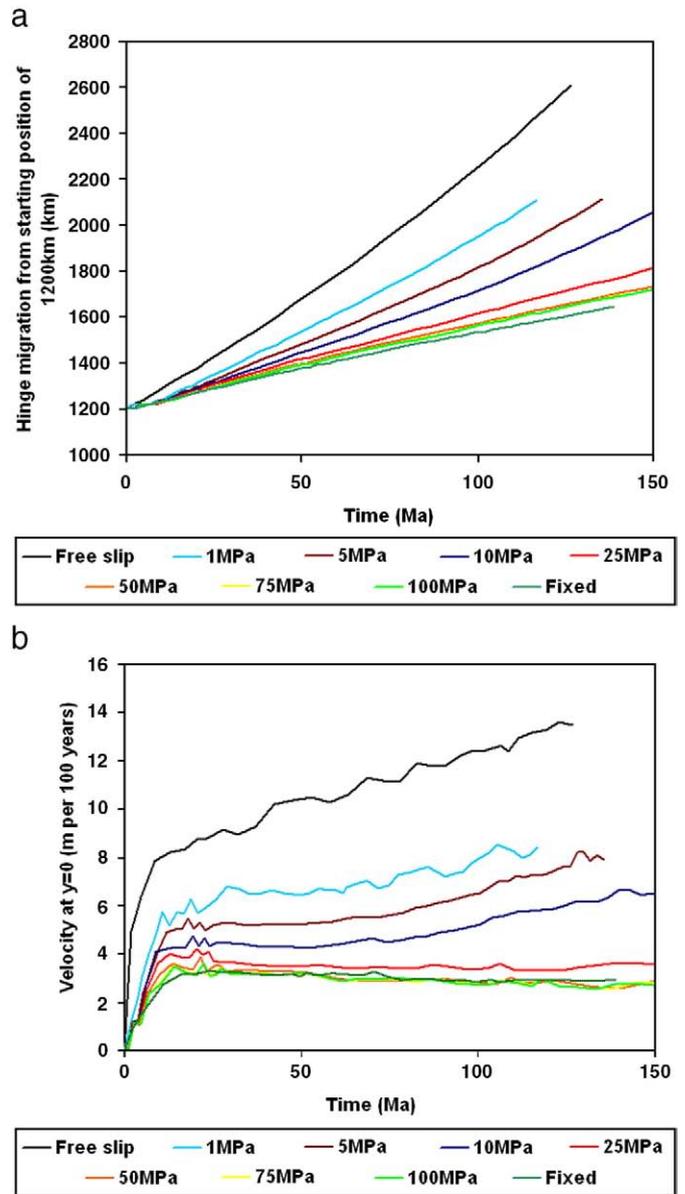


Fig. 8. (a) Results show hinge migration distance at the symmetry boundary from an initial distance of 1200 km against time for all simulations. The key for the graph is given in Table 2. All simulation have a yield strength of 100 MPa for the plate and a density difference between plate and mantle of $\Delta\rho = 69 \text{ kg m}^{-3}$. (b) Results show slab rollback velocity at the symmetry boundary from an initial distance of 1200 km against time for all simulations. The key for the graph is given in Table 2. All simulations have a yield strength of 100 MPa for the plate and a density difference between plate and mantle of $\Delta\rho = 69 \text{ kg m}^{-3}$.

layer of lithosphere can remain attached to the weak layer boundary, as shown in Fig. 6d–g.

As discussed in Section 4.1, the shape that the subducting hinge makes with the free-surface is partially controlled by the magnitude of the yield strength in the weak layer. Low yield strength can result in the slab edge experiencing the largest rollback rates. While higher yield strength in the weak zone can result in the slab remaining attached to the fixed slab, as well as slab stretching, necking and reduced negative buoyancy forces.

4.3. Maximum slab depth

Fig. 7 shows the maximum depth of the slab at the symmetry boundary ($y=0$) for simulations with varying yield strength values (simulations 0–8 in Table 2). Results show that increasing tear resistance slows the sinking of the slab. A subducting slab with no tear resistance would reach the base of the model domain approximately 3 Myr earlier than the subducting slab with maximum tear resistance. This difference accounts for approximately 10% of the total time taken for the slab to reach the bottom of the domain.

Qualitatively, all simulations are characterized by similar behaviour (Fig. 7), suggesting that the dynamics of this diagnostic parameter (maximum depth of the subducting slab) is primarily controlled by the geometry of our model setup. Ultimately it is the combination of the competing forces: the negative buoyancy forces, mantle drag, resistance to bending at the surface and tear resistance at the slab edge that controls the sinking velocity. Resistance to bending at the slab hinge and tearing at the slab edge are approximately constant throughout a simulation. The negative buoyancy forces are proportional to the volume of lithosphere embedded in the mantle material above the bottom of the domain, whereas mantle drag is proportional to the area of the slab. We can therefore identify four stages of subduction dynamics. In stage 1, the slab sinks rapidly and relatively uniformly, characterised by mainly poloidal flow and minimum mantle drag. During stage 2, induced toroidal to poloidal flow increases, the cross section of the slab increases and hence mantle drag increases. Consequently the sinking speed of the slab decreases. Stage 3 shows accelerated sinking of the slab due to the increasing volume to area ratio of the slab with lithospheric deformation dominated by slab negative buoyancy forces rather than mantle drag. The last stage (stage 4) corresponds to the interaction of the slab with the 660 km boundary.

4.4. Hinge migration

Fig. 8a shows the hinge location of the slab at the symmetry boundary ($y=0$) for simulations, with varying yield strength values (simulations 0–8 in Table 2). Results show that as the tear resistance is increased, the hinge rollback migrating speed is reduced, showing that hinge migration can be significantly affected by tear resistance. Comparing the simulation with a tearing yield resistance of 100 MPa to the simulation with free-slip, the migration of the hinge at $y=0$ moves approximately one third of the distance for the same time-period.

Fig. 8b shows the hinge migration velocity at the symmetry boundary ($y=0$), which is arguably the most important kinematic

parameter in subduction zones (Schellart et al., 2008). Our simulated subduction models have hinge migration velocities at the symmetry boundary ($y=0$) of 2.5 cm/year–15.5 cm/year. These values are within the observed range of –2.5 cm/year–15.5 cm/year for comparable slab widths (Schellart et al., 2007). All our simulations show that the slab experiences accelerating hinge migration velocity until it interacts with the 660 km boundary. This is mainly due to the increasing negative buoyancy forces acting on the slab modulated by smaller effects, as discussed in the previous sections.

Once the slab interacts with the 660 km boundary, hinge rollback maintains a constant speed (for simulations with high yield strength values) or increases at a slower rate (for simulations with low yield strength values). Simulations in which hinge rollback continues to accelerate (after the slab has reached the 660 km boundary) correspond to simulations in which the slab edge (280 km–300 km) experiences the largest rollback rates (Fig. 4). Accelerating rollback without increasing the negative buoyancy forces suggests that preferential subduction at the edge (see Section 4.1) imposes an unbalanced force on the rest of the slab. Simulations with tear zone yield strengths less than 10 MPa do not experience accelerating rollback at the slab edge during mature subduction, and consequently only constant rollback in the centre of the slab. Hinge migration is also approximately the same for all high yield strength models since tear resistance in these simulations plays only a minor role on central hinge migration.

We conclude that the negative buoyancy forces are the main control on hinge migration during incipient subduction, but tear resistance becomes significant for controlling the speed of subduction rollback. Our simulation results fall into two categories for mature subduction: accelerating rollback versus constant rollback. A low tear (yield) resistance in the weak layer permits continued acceleration of the subduction hinge, whereas a high tear (yield) resistance in the weak zone results in a constant rollback velocity.

We note that the oscillations for the hinge rollback velocity in Fig. 8b are an artefact of how the velocity is calculated at the hinge. We perform a linear interpolation for the velocity based on the exact location of the hinge. However, since we cannot expect the velocity field between the node in the slab closest to the hinge and the adjacent node outside the slab to be linear, this results in the observed fluctuations in velocity.

4.5. Trench width

Trench width is an important parameter for subduction dynamics and has been extensively explored (Stegman et al., 2006; Schellart et al., 2007). These studies have shown that rollback velocity is

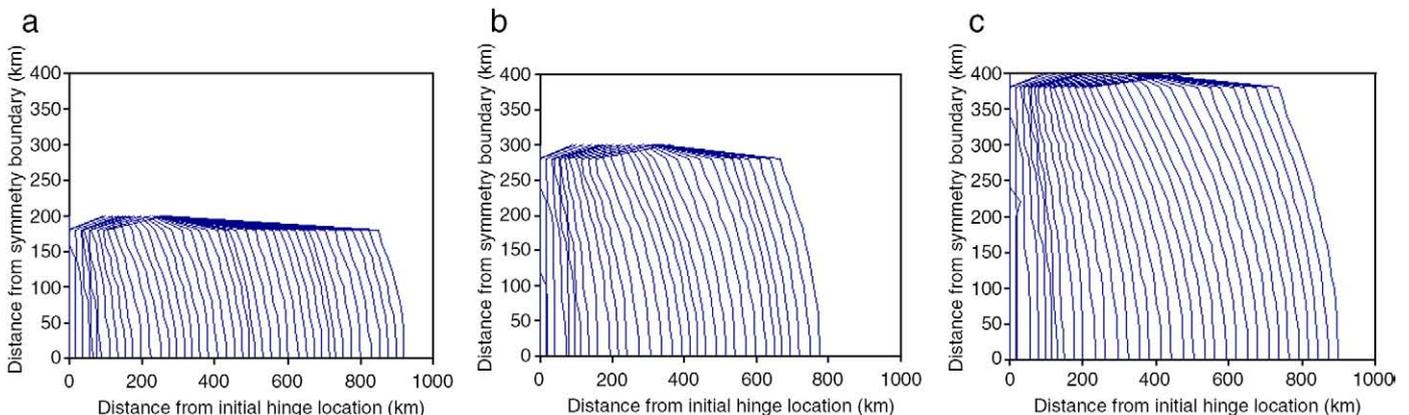


Fig. 9. All simulation results have a yield strength of 25 MPa for the slab, corresponding to simulations 4, 9 and 10 in Table 2. Fig. 9 a–c show the shape of the subducting slab hinge at the free-surface at 10 time-step intervals. The weak layer is between a distance of 200 and 220 km for figure a, 300 and 320 km for figure b and 400 and 420 km for figure c. a) Slab width = 400 km. b) Slab width = 600 km. c) Slab width = 800 km.

fastest approximately 300 km from the subduction edge, suggesting that induced toroidal flow is most significant at aiding rollback at that distance from the edge. However, it is the overall force balance which determines slab movement, and fast rollback velocities have also been observed/modelled in slab segments up to 900 km away from the next edge (Stegman et al., 2006; Schellart et al., 2007). This suggests a strong dependence on the tectonic setting/model configuration for rollback velocities. We performed simulations with different slab widths and constant tear resistances to observe the significance of our model setup and how it may influence the slab geometry.

All simulations shown in Fig. 9 have yield strength values of 25 MPa in the weak zone, corresponding to simulations 4, 9 and 10 in

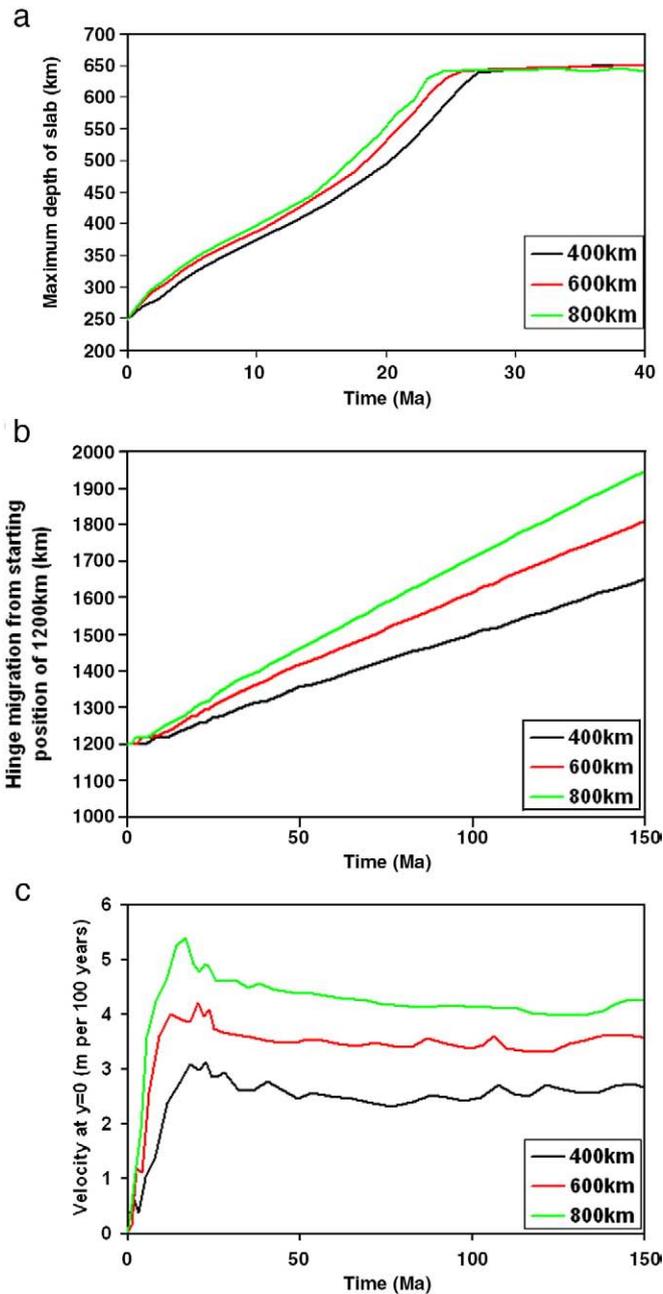


Fig. 10. All simulation results have a yield strength of 25 MPa for the slab, corresponding to simulations 4, 9 and 10 in Table 2. a) Shows the maximum depth of the slab at $y=0$, the symmetry boundary. b) Shows the hinge migration location of the slab at $y=0$, the symmetry boundary. c) Shows the hinge migration velocity of the slab at $y=0$, the symmetry boundary.

Table 2. Fig. 9a–c shows the shape of the subducting slab hinge at the free-surface at 10 time-step intervals. As the width of the slab is increased, the hinge curvature also increases. This indicates that the effective scale of induced toroidal flow in our setup increases at least up to 400 km. Note that as the width of the slab is increased, the weak layer experiences less rollback in this region.

Fig. 10a shows the maximum depth of the slab at $y=0$, the symmetry boundary, for subducting slabs with widths from 400 km to 800 km. Our model results show qualitatively the same behaviour as discussed in Section 4.3. Increasing the width of the slab enhances the speed at which the slab descends into the mantle due to increased slab negative buoyancy forces (Fig. 10b). Lastly, Fig. 10c shows the hinge migration velocity of the slab at the symmetry boundary ($y=0$). Hinge rollback is fastest for the widest slab, consistent with the previous diagnostic parameters.

Hence our setup acts to shift the point of maximum rollback (due to induced flow) further away from the edge.

5. Discussion and conclusions

We presented simulations of lithospheric subduction with tearing at the slab edges. Our results indicate that tear resistance is an important controlling parameter in the dynamics of subduction zones, in addition to interactions between subduction rollback and toroidal flow (Schellart and Lister, 2004; Stegman et al., 2006; Schellart et al., 2007).

Our simulation results follow an evolution in which the slab initially sinks rapidly and relatively uniformly since increasing slab negative buoyancy forces are the main control on hinge migration in incipient subduction. As the sinking slab begins to experience enhanced mantle drag, the rate of slab sinking begins to decrease. Following this, slab negative buoyancy forces can dominate over mantle drag, leading to accelerated sinking again. Lastly the slab interacts with the 660 km boundary.

Simulation results show that the curvature of the slab hinge is controlled by toroidal flow and the resistance experienced in the tear region. Slab tearing with low or zero yield strength results in a slab hinge shape that remains relatively straight, whereas increasing the yield strength within the tear region results in the curvature of the hinge becoming more prominent. Increasing the yield strength along the tear region corresponds to settings in which the subducting slab is controlled more by the weak layer and less by the toroidal flow around the slab. For a pinned boundary at the edge of the subducting slab, toroidal flow plays no role in the shape of the subducting slab, but the slab hinge shape produced is that of an arc. Hence, our simulations show that there are three inherent end-members controlling the slab hinge shape: slab-pinning, slab rollback controlled by tearing and slab rollback controlled by toroidal flow. Please note that our models are simplified with respect to real tectonic settings. Neglected features include mantle wind and lithospheric inhomogeneities, which also affect subduction. Visualised snapshots of the subducting lithosphere show how the geometry of the slab is influenced by the resistance in the weak layer. As the yield strength in the weak layer is increased, the subducting slab can become recumbently folded at the base of the domain. This is due to the slab length increasing due to stretching without rollback being sufficiently fast to compensate. Introducing a higher viscosity lower mantle region to the base of our domain is likely to affect the volume of lithosphere sinking into the lower mantle due to recumbent folding. As the yield strength in the weak layer is increased, slab stretching can result in reduced slab negative buoyant forces due to the slab thinning. In contrast, for low yield strengths in the weak layer, the largest rollback velocities can occur close to the slab edge due to the generation of a low viscosity layer at the slab edge.

Increasing the tear resistance at the edge of the slab acts to slow the sinking of the slab by up to 10%. The migration velocity of subduction

zones 200–400 km from the edge of the slab are in the range -2.5 cm/year– 15.5 cm/year (Schellart et al., 2008). This is comparable with our simulated values of 2.5 cm/year– 15.5 cm/year. Further, our simulation results fall into two categories for mature subduction: accelerating rollback versus constant rollback. It is the magnitude of tear resistance that controls hinge migration, with constant rollback maintained for tear zones with high resistance. However, for low or zero resistance in tear zones the slab can experience continuing accelerated rollback.

The simulations presented in this paper impose a no-slip boundary condition at a depth of 100 km below the domain free-surface, either side of the subducting slab. In reality, either side of the subducting slab will be neighbored by lithosphere. The lithosphere resists deformation through mantle drag, but it is not completely rigid. Therefore, our simulations act to minimise additional deformation induced by toroidal flow in this region, while subduction models by Stegman et al. (2006) consider the neighbouring lithosphere behaving as deformable mantle. The real natural behaviour is possibly somewhere in between.

For simplicity we imposed the location of the tear region in our simulations. However, in reality the location of the tear zone will be governed by the shear stresses acting on the slab, which is likely to be modified by the interaction of rollback, tear resistance at the fault, induced mantle flow and inhomogeneities in the lithosphere. All of these processes may result in tearing occurring away from the preferred propagation direction. In addition to this, our simulations can be considered as being somewhat artificial by imposing the same tearing resistance for either side of the subducting slab, which in nature is likely to be a rather unusual situation. Our modelling technique has been shown to be very powerful for this natural phenomenon. Future models will consider scenarios in which the tear resistance is different for the two tear zones, which could have significant implications for explaining trench rotation, such as that observed at the Tonga–Kermadec–Hikurangi subduction zone.

Our visco-plastic models lack the inclusion of a strong core which has shown to be important in acting as a stress-guide to maintain slab pull (Morra et al., 2006). By including a stress-guide in future models, the slab would exert a stronger backwards propagating hinge migration and larger slab pull.

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Appendix A. Stokes flow past a sphere

Stokes flow past a sphere is a solution for the frictional force, or drag force, exerted on spherical objects with very small Reynolds numbers in a continuous viscous fluid. Stokes' law is derived by

Table A1

Parameters used for falling sphere benchmark model presented in Appendix A.

Parameter	Symbol	Value
Density contrast between fluids	$\Delta\rho$	10 kg/m^3
Radius of sphere	a	120 m
Height of domain	h	5400 m
Viscosity of fluid	η_f	10^{10} Pa s
Viscosity of sphere	η_s	10^{13} Pa s
Gravity	g	10 m/s^2

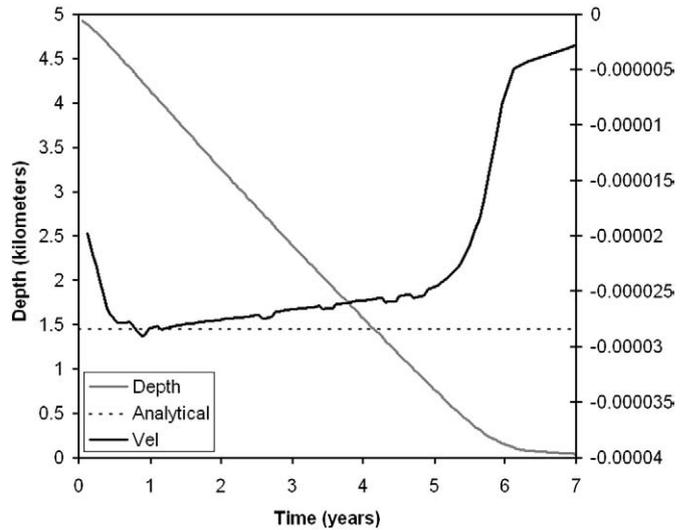


Fig. A1. Figure shows the velocity (black line) and depth (grey line) for a high viscosity sphere falling through a viscous fluid. Also shown is the analytical solution (dashed line) equal to $3.2 \times 10^{-5} \text{ m s}^{-1}$.

solving the Stokes flow limit for small Reynolds numbers. With inertia neglected Stokes' flow is given by:

$$\frac{\partial P_i}{\partial x_j} = \eta \rho \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right) \quad (\text{A6})$$

where P is pressure, v the velocity and η the viscosity of the fluid. The pressure gradient is responsible for driving the flow by overcoming viscous resistance. Equating the drag and buoyant forces on the particle we can form an analytical solution for the free-falling terminal velocity, v_0 :

$$v_0 = \frac{2}{9} g a^2 \frac{\Delta\rho}{\eta_f} \quad (\text{A7})$$

where $\Delta\rho$ is the density contrast between the fluids and a the radius of the sphere. For our benchmark model we model a falling sphere as a high viscosity droplet with the parameter values given in Table A1. Using these parameters the maximum free-fall velocity of the sphere should equal $3.2 \times 10^{-5} \text{ m s}^{-1}$. Results for a high viscosity sphere falling through a viscous fluid are shown in Fig. A1. Our simulation results start with the sphere velocity equal to zero, resulting in an initial period of acceleration. After a time of approximately 1 year, the falling sphere has reached its terminal velocity, equal to approximately $3.2 \times 10^{-5} \text{ m s}^{-1}$, as shown by the dashed analytical line. The model domain was 5 km in length and from a time of one year onwards the falling sphere begins to experience the edge effects of the model domain, resulting in the sphere falling with decreasing velocity. The sphere reaches the base of the model domain after a period of approximately 6 years.

Appendix B. Comparison to slab embedded in mantle models

For completeness we simulate a subducting slab with a domain set-up as described in Fig. 4b, but without a fixed plate or a weak layer region, for comparison to previous studies (e.g. Stegman et al., 2006). Fig. A2a shows model results for the map-view shape of the subduction hinge for the simulation with free-slip at $y = 300$ km. Fig. A2b shows results for the map-view shape of the subduction hinge for exactly the same model parameters as the results shown for Fig. A2a, except that this simulation has no fixed boundary condition at $y = 300$ km. Results are shown at 10 time-step

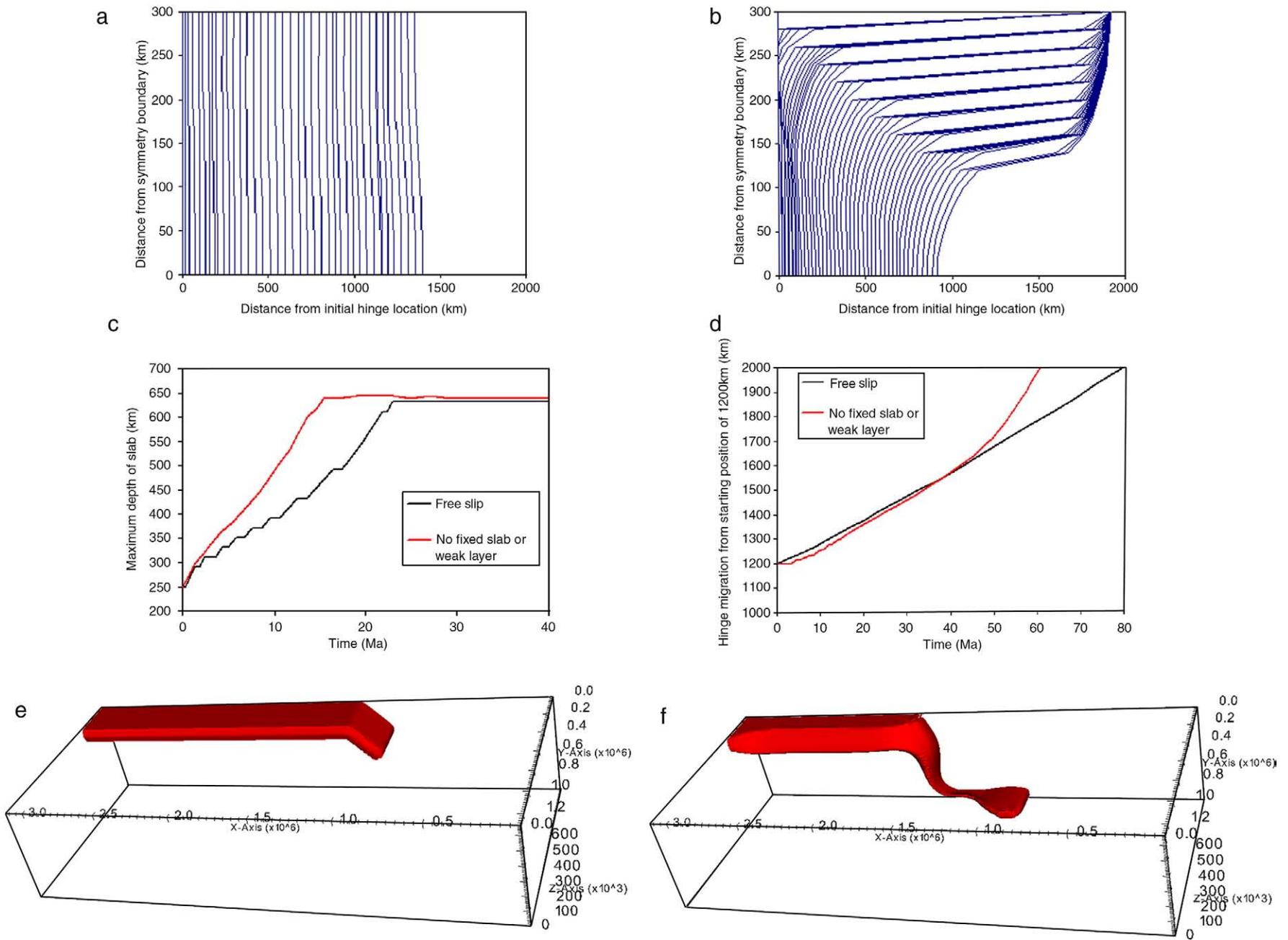


Fig. A2. a) Model results for the map-view shape of the subduction hinge for the simulation with free-slip at $y = 300$ km. b) Results for the map-view shape of the subduction hinge for no fixed boundary condition at $y = 300$ km. Results are shown at 10 time-step intervals. Panels c) and d) show the maximum depth of the slab and hinge migration, respectively. Panels e) and f) show snapshots of the subducting lithosphere within the model domain at the start of the simulation after a time of approximately 50 Ma, respectively.

intervals and show the significance of the simulated boundary condition at the edge of the slab. Without a fixed boundary the slab edge is embedded into the mantle material, which flows around the slab during rollback, initially producing a more prominent arc shape until the edges of the slab begin to advance into the centre of the slab.

Fig. A2c and d show the maximum depth of the slab and hinge migration, respectively, for the simulations with a free-slip boundary condition and for the slab embedded in the mantle. These results show that the depth of the slab reaches in time in enhanced when the slab is embedded within the mantle.

Fig. A2e and f show snapshots of the subducting lithosphere within the model domain, for the simulation with no fixed boundary condition at $y=300$ km, at the start of the simulation after a time of approximately 50 Ma, respectively. These snapshots show how the edge of the slab (as well as the end) subducts into the mantle.

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