**Ionospheric Threat Model Assessment**

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**ABSTRACT**

This paper presents the first results of a German study (ITMA) that attempts to validate the GBAS CAT I ionosphere threat space that was developed for US CONUS. In phase 1 of this study the German Aerospace Center DLR and the German Air Navigation Service Provider DFS tried to determine the normal residual ionospheric uncertainty ($\sigma_{\text{vig}}$) and to identify periods with severe ionospheric activities relevant for GBAS. Dual-frequency RINEX data of up to 80 geodetic stations in and around Germany over an 11 year solar cycle from 1998 (25 stations) to 2008 (80 stations) was processed. Based on this data evaluation the study determined 16 periods with disturbed ionosphere in the years 2000 to 2003 and one day in 2005.

These periods will be analyzed in more detail in phase 2 of the study to populate the GBAS CAT I ionosphere threat space. To determine the necessary parameters slope, velocity and width of the identified ionospheric fronts it is necessary to use additional GNSS data from German geodetic networks. This additional data should improve the resolution in the areas where the ionospheric front was detected. Phase 2 of the study should be completed in autumn 2009. The database may then be used to validate the assumptions regarding ionospheric effects for GAST-D.

**INTRODUCTION**

The ionosphere is one of the error sources in ground-based augmentation systems. Usually, the ionosphere-induced errors in GBAS are small. However, very strong variations in the ionospheric plasma have been found which can compromise the safety of GBAS [4].

The total electron content (TEC) is given as the integral of the electron density along the ray path [7]

$$ TEC = \int n_e \, ds . $$

The unit for $TEC$ is 1 TECU $= 10^{16} \, e/m^2$. Since the ionospheric plasma is a dispersive medium, signals with different frequencies propagate in a different way. The effect of the ionosphere on the range measurements is proportional to $f^{-2} \, TEC$, phase measurements are affected with reversed sign. Since GBAS is a differential system, not the absolute level of ionization is important but ionospheric gradients. The errors induced in GBAS by ionospheric gradients are dealt with as follows:

- Nominal vertical ionospheric gradients are described by the parameter $\sigma_{\text{vig}}$ which is a parameter transmitted in the type 2 message of a GBAS ground station [2][3]
- Anomalous ionospheric gradients are described by a threat model and can be mitigated, e.g., by geometry-screening methods [4][5][6].

Within the ITMA project both types of gradient information are determined for the region $2°E - 18°E, 45°N - 58°N$ (see Fig. 2).

The data from an entire solar cycle 1998-2008 was processed. In the following some of the results obtained in phase 1 of the project are described in more detail.

**METHODOLOGY**

From dual-frequency GPS data, relative ionospheric range errors can be obtained from different combinations of observables

$$ I_{\text{phase\_diff}} = \frac{f_2^2}{f_1^2 - f_2^2} (L_1 - L_2) $$

$$ I_{\text{code\_diff}} = \frac{f_2^2}{f_1^2 - f_2^2} (P_2 - P_1) $$

$$ I_{\text{code\_phase}} = \frac{1}{2} (P_2 - L_1) $$

Here, $L_1, L_2$ and $P_1, P_2$ are the phase and code measurements on the two GPS-frequencies $f_1, f_2$. All three combinations, $I_{\text{code\_diff}}, I_{\text{phase\_diff}}$ and $I_{\text{code\_phase}}$ are relative estimates of the ionospheric range error on the first GPS frequency, since they contain instrumentation offsets (e.g. differential-code-biases) and phase ambiguities. The relationship between $TEC$ and these combinations is given by
\[ I_{\text{phase\_diff}} = 0.1623 \times TEC + b, \quad (5) \]

and analogously for \( I_{\text{code\_diff}} \) and \( I_{\text{code\_phase}} \).

Following the MOPS [2][3], the ionosphere is approximated as an infinitesimally thin layer at a fixed height \( h_{\text{iono}} = 350 \text{ km} \). Slant and vertical ionospheric range errors are related by the so-called obliquity function

\[ M(\text{elev}) = \left( 1 - \frac{r_E \cos(\text{elev})}{r_E + h_{\text{iono}}} \right)^{1/2} \quad (6) \]

\[ I_{\text{slant}} = M(\text{elev}) \cdot I_{\text{vert}}. \quad (7) \]

**Determinaton of an over-bound of \( \sigma_{\text{vig}} \)**

In order to determine an over-bound for \( \sigma_{\text{vig}} \), we compute calibrated vertical ionospheric range errors \( I_{\text{vert},i,j} \) and their ionospheric pierce points \( I_{\text{IPP},i,j} \) at a single epoch from a number of ground stations [7]. Then vertical ionospheric gradients \( \text{vig}_{i,j} \) between each pair of measurements \( i,j \) may be computed as

\[ \text{vig}_{i,j} = \frac{I_{\text{vert},i,j} - I_{\text{vert},i,j}}{\text{dist}(I_{\text{IPP},i}, I_{\text{IPP},j})}. \quad (8) \]

where the distance \( \text{dist}(I_{\text{IPP},i}, I_{\text{IPP},j}) \) between the ionospheric pierce points is computed at the height \( h_{\text{iono}} \). Since even small calibration errors in \( I_{\text{vert}} \) can generate large gradients at small IPP-distances, only pairs of measurements within the range \( 250 \text{ km} < \text{dist}(I_{\text{IPP},i}, I_{\text{IPP},j}) < 500 \text{ km} \) are used.

**Determination of anomalous ionospheric gradients**

Anomalous ionospheric gradients are taken into account in the GBAS integrity analysis by a threat model [5][6]. The threat model describes the worst-case ionospheric threat which is caused by moving ionospheric fronts. The threat space is determined from historical measurements. The anomalous ionosphere threat model has three dimensions, i.e. an ionospheric front is characterized by (see Figure 1)

- slope \( g \) (mm/km=ppm)
- velocity \( v \) (m/s)
- width \( W \) (km).

Unlike \( \sigma_{\text{vig}} \), which quantifies vertical ionospheric gradients, the anomalous ionosphere threat model describes slant ionospheric range errors.

In order to establish the threat model for a certain region, a minimal domain in its three-dimensional parameter space has to be determined. Within the ITMA project the following two-step process is used

**RESULTS**

We used data downloaded from SOPAC (Scripps Orbit and Permanent Array Center) and from BKG (Bundesamt für Kartographie und Geodäsie). For the period of 1998-2008 we determined the availability of GPS data in the region of interest which is indicated by the blue square in Figure 2. While in 1998 data from about 25 stations is available, the number of available stations increases and reaches about 80 stations in the year 2008.

In order to determine \( \sigma_{\text{vig}} \), we used data from different seasons and from different levels of solar activity, as indicated in Table 1; the number of used data points for each period is displayed in Table 2. The resulting complementary cumulative distribution functions of vertical ionospheric gradients for each period and the Gaussian over-bound for \( \sigma_{\text{vig}} = 2.07 \text{ mm/km} \) is shown in Figure 3.
Figure 2: Available GPS-Stations from SOPAC and BKG

Table 1: Vertical ionospheric gradients have been computed from 30s RINEX data both for summer and winter periods in high- and low-solar-activity periods. The date format is YYYY-DOY.

<table>
<thead>
<tr>
<th>Period</th>
<th>Number of used data points</th>
</tr>
</thead>
<tbody>
<tr>
<td>HSA winter</td>
<td>114903</td>
</tr>
<tr>
<td>HSA summer</td>
<td>91630</td>
</tr>
<tr>
<td>LSA winter</td>
<td>322595</td>
</tr>
<tr>
<td>LSA summer</td>
<td>241245</td>
</tr>
</tbody>
</table>

\[ \Sigma = 810273 \]

Table 2: Number of used data points for \( \sigma_{\text{vig}} \).

Periods with anomalous ionospheric activity have been determined by analyzing 30s RINEX data for each day in 1998-2008 in the following way:

- Computation of \( \text{grad}_{\text{ROT}} \) -values from 30s RINEX data
- Applying the \( \text{grad}_{\text{ROT}} \) -filter to the data in order to remove bad data points.
- Determination of \( N_{30}, N_{50}, N_{100}, N_{150}, N_{200} \): the number of data points with \( \text{grad}_{\text{ROT}} > 30, 50, 100, 150, \) and 200 mm/km
- If \( N_{100} > 1 \) and \( N_{50} > N_{100} + 1 \) the day is marked as a day with anomalous ionospheric activity.

Figure 3: CCDF for vertical ionospheric gradients: blue = winter, green = summer, solid lines = high solar activity, dashed lines = low solar activity. The dotted lines show the CCDF of Gaussian distributions with \( \sigma_{\text{vig}} = 4 \text{ mm/km} \) (red dots) and the over-bound \( \sigma_{\text{vig}} = 2.07 \text{ mm/km} \) (orange dots).

Figure 4: In the top plot the number of data points is shown in blue, \( N_{100} \) (number of data points with \( \text{grad}_{\text{ROT}} > 100 \text{ mm/km} \)) in red and the number of excluded data points is displayed in green. The bottom plot shows the geo-magnetic \( A_p \) and \( D_{\text{ST}} \) indices for the same period of time.

For the year 2001 the resulting \( N_{100} \) values are shown in Figure 4, along with geo-magnetic indices \[9\] for the same period of time. It can be seen that anomalous ionospheric activities occur when the indices indicate a geo-magnetic disturbance. The converse statement, however, is not true, which is the reason for performing the data-screening with RINEX data instead of solely relying on geo-magnetic indices.

In Figure 5, we show relative slant ionospheric delays and the corresponding \( \text{grad}_{\text{ROT}} \) -values for July 15, 2000 for a number of ground stations and the same GPS satellite G09. Note \( \text{grad}_{\text{ROT}} \) -values as determined by equation (9) are not corrected for the movement of the iono front. The plots are used to crosscheck the results based on time.
difference of slant ionospheric range errors with the other combinations of observables mentioned earlier.

![Figure 5: The upper plot of each location shows relative ionospheric range errors $I_{\text{phase\_diff}}$ (red line), $I_{\text{code\_phase}}$ (blue line) and $I_{\text{code\_diff}}$ (green dots). The lower plot of each location shows the corresponding $\text{grad}_{\text{ROT}}$-values computed from $I_{\text{phase\_diff}}$.](image)

CONCLUSIONS

In the first phase of the ITMA project we have

- determined an Gaussian over-bound for vertical ionospheric gradients $\sigma_{\text{sig}} = 2.07 \text{ mm/km}$ using calibrated vertical ionospheric range errors from periods of high- and low-solar-activity and from different seasons.

- identified 16 periods with anomalous ionospheric activity by screening 30s RINEX data from 1998-2008 using up to 80 stations.

For the second phase, the periods with anomalous ionospheric activity have to be analyzed with respect to the parameters in the threat model.

ACKNOWLEDGMENTS

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REFERENCES


http://www.ngdc.noaa.gov/stp/GEOMAG/kp_ap.htm