



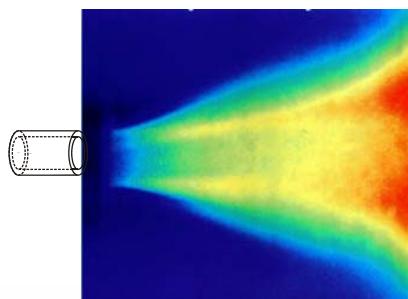
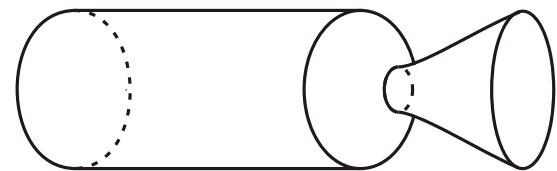
Investigation of the Combustion Chamber Acoustics and its Interaction with LOX/H₂-Spray Flames

M. Oschwald, B. Knapp

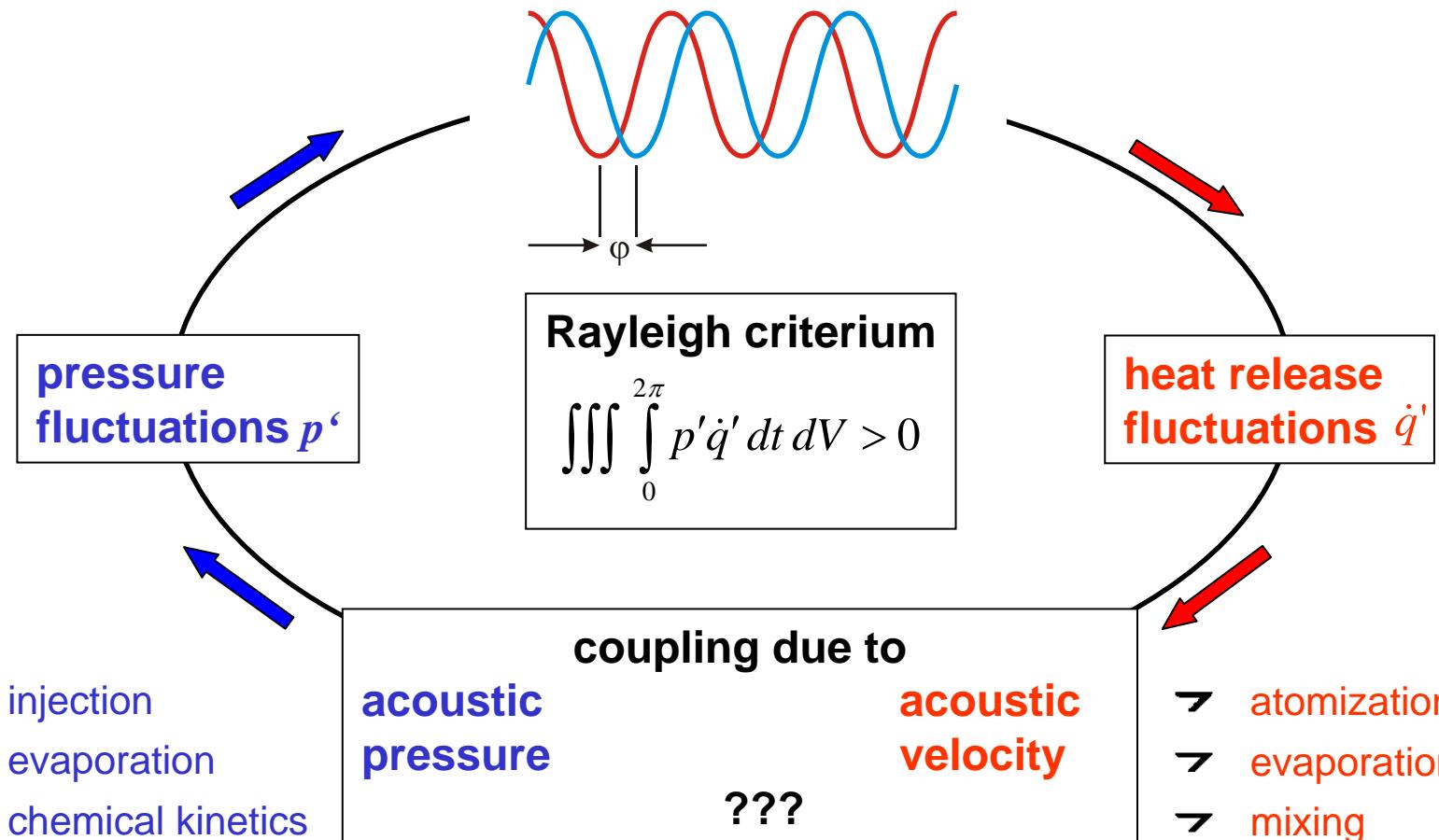
HF combustion instabilities

coupling of acoustic combustor resonances to combustion processes

- ☛ chamber acoustics
 - ☛ eigenmodes of a cylindrical resonator
- ☛ combustion processes
 - ☛ propellant injection
 - ☛ atomization
 - ☛ secondary atomization
 - ☛ droplet evaporation
 - ☛ chemical kinetics



coupling mechanisms



combustion chamber as acoustic resonator

- ↗ chamber in good approximation treated as cylindrical volume
- ↗ chamber acoustically closed at the throat
- ↗ linear acoustics

$$\frac{\partial^2 P'}{\partial t^2} - c^2 \Delta P' = 0$$

- ↗ Eigen value equation

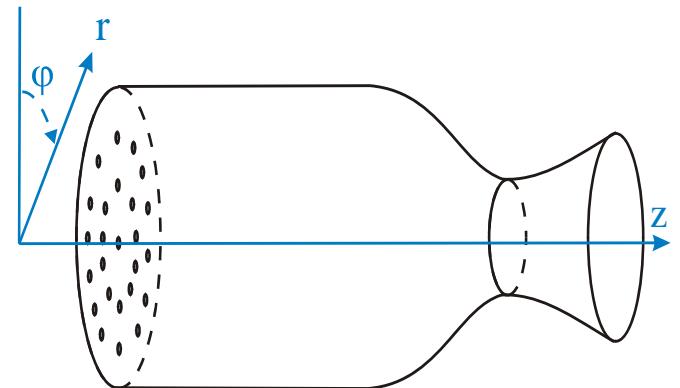
$$\Delta P' = -\frac{\omega^2}{c^2} P'$$

$$P'(z, r, \varphi) = \cos(n\varphi) J_n(\alpha_{nm} \frac{r}{R}) \cos(l\pi \frac{z}{L})$$

$l = 0, 1, 2 \dots$ longitudinal modes

$n = 0, 1, 2 \dots$ tangential modes

$m = 1, 2, 3 \dots$ radial modes



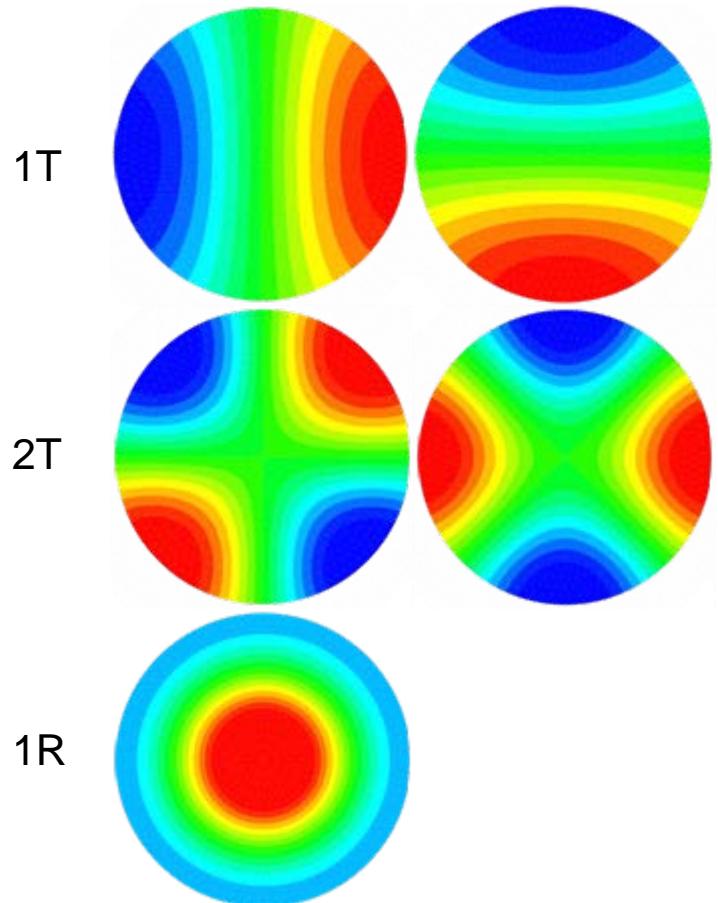
eigen modes of a cylindrical resonator

$$f_{nm} = \frac{\alpha_{nm} c}{2\pi R}$$

Mode	n	m	α_{nm}
1T	1	1	1.841
2T	2	1	3.054
1R	0	2	3.832
1T1R	1	2	5.331

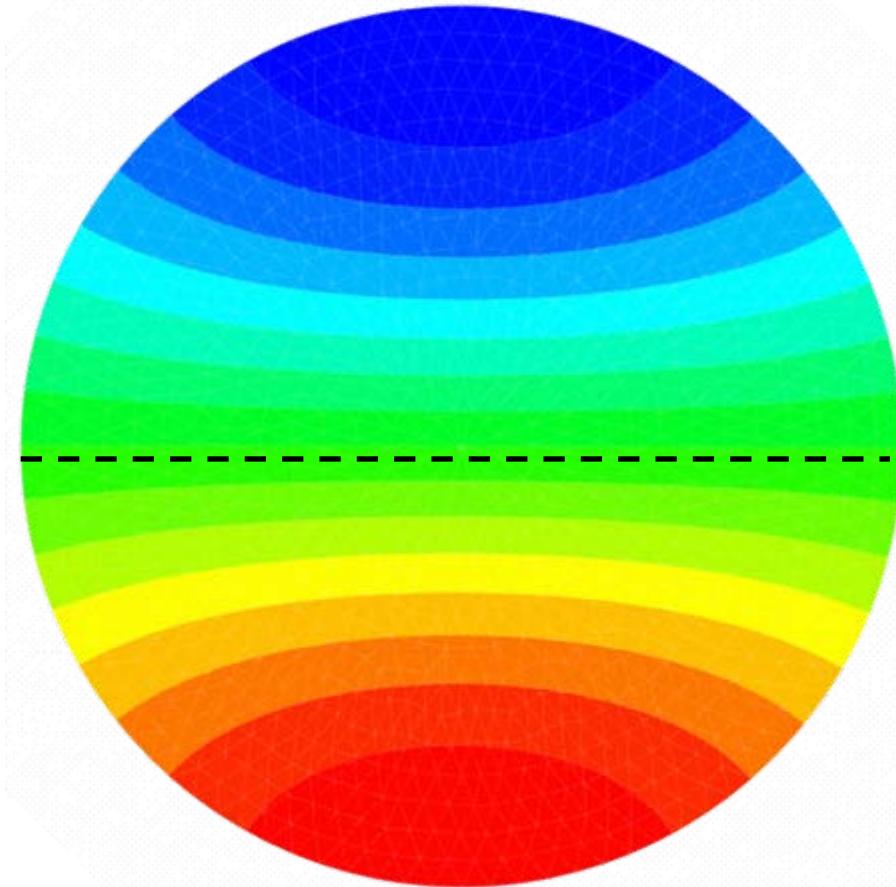
$$R \approx 0.1m$$

- ↗ ambient air:
 $c = 343m / s$
 $f_{1T} = 1.0kHz$
- ↗ hot fire test:
 $c \approx 1370m / s$
 $f_{1T} = 4.0kHz$
- ↗ tangential modes are 2-fold degenerate
- ↗ usually longitudinal modes not involved in HF-instabilities

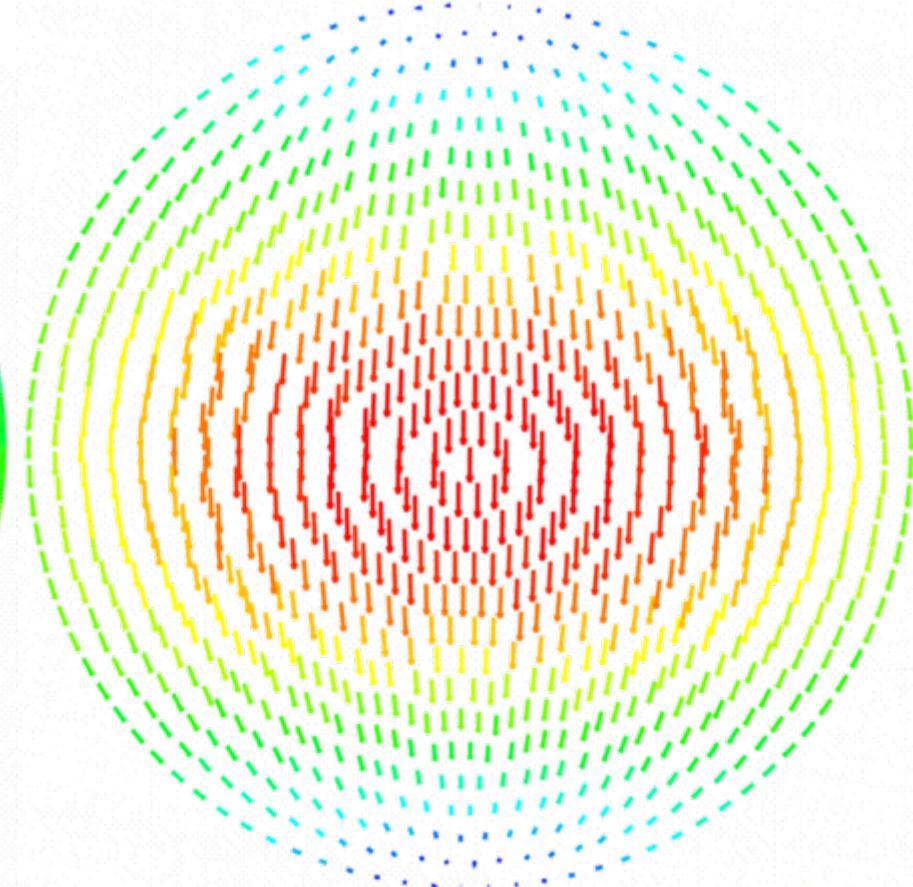


1T eigen mode

pressure field

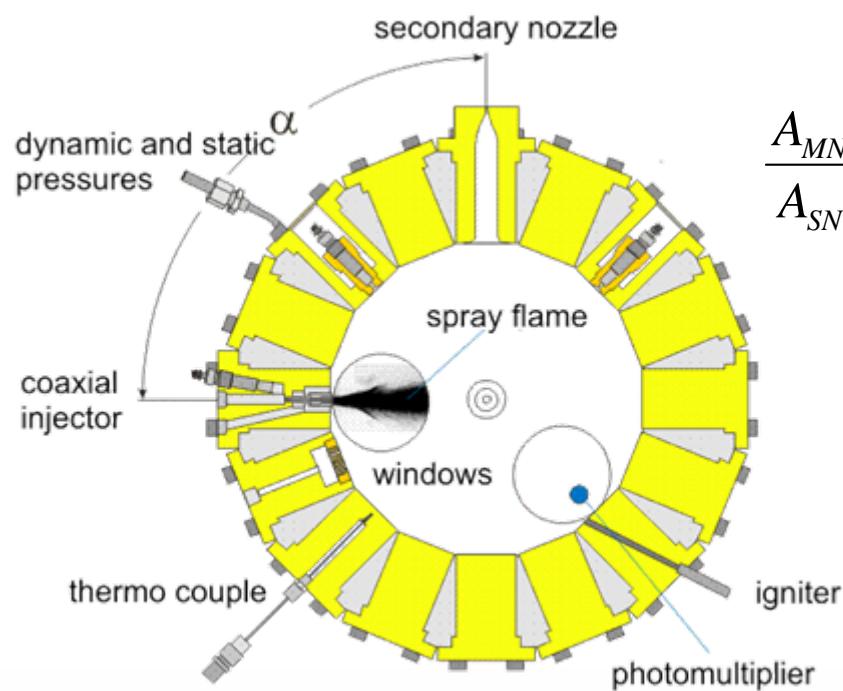
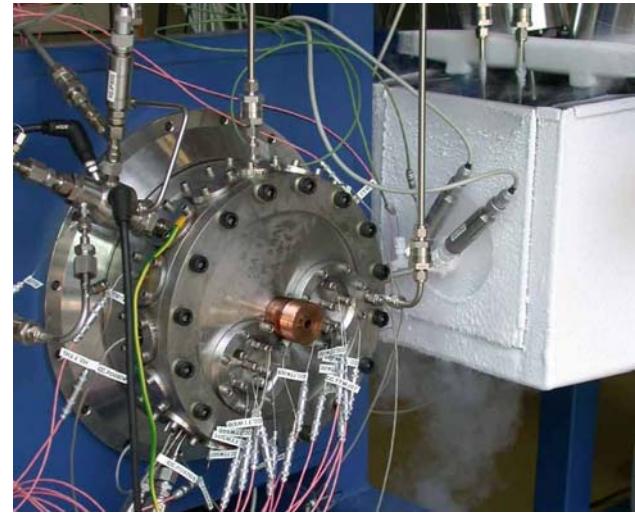


velocity field

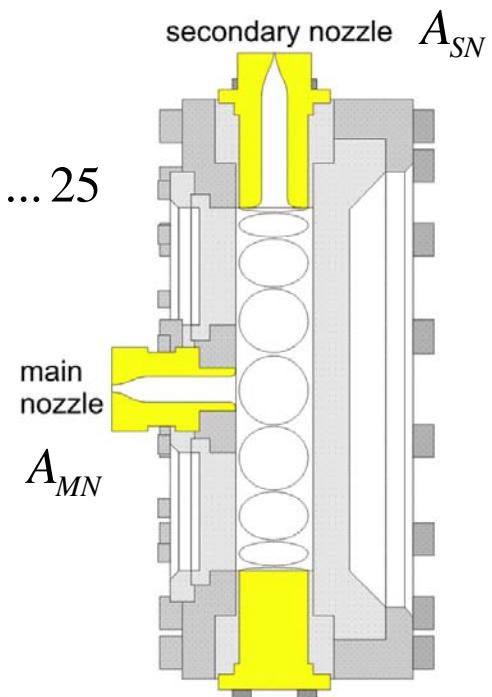


HF-combustor (CRC)

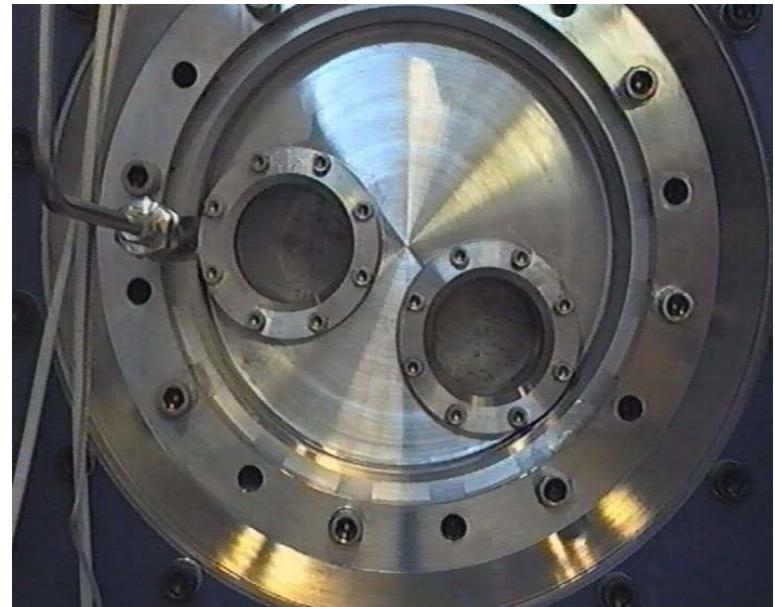
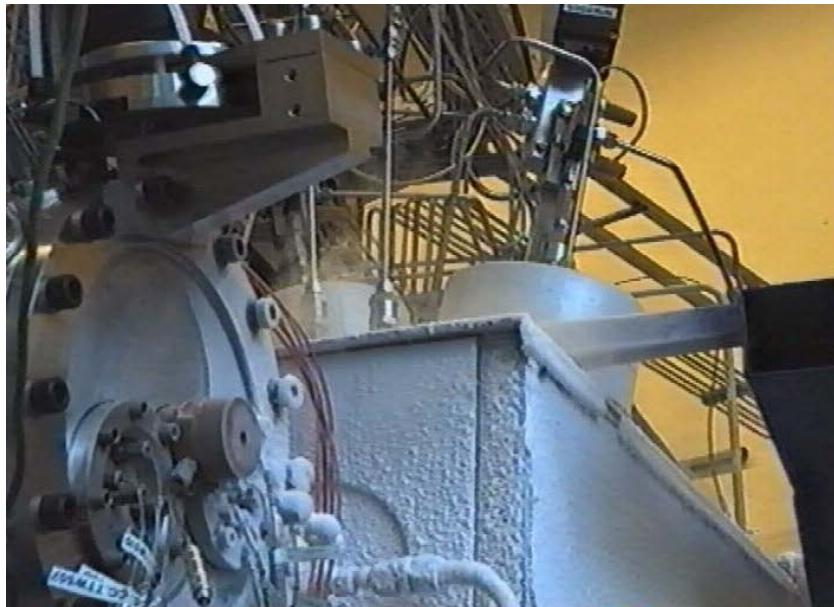
- diameter x height: 20 cm x 4 cm
- transversal modes at representative frequencies
- p_c up to 10 bar
- LOX, GH₂ @ 77K
- coaxial injector
- injection in radial direction



$$\frac{A_{MN}}{A_{SN}} = 6 \dots 25$$

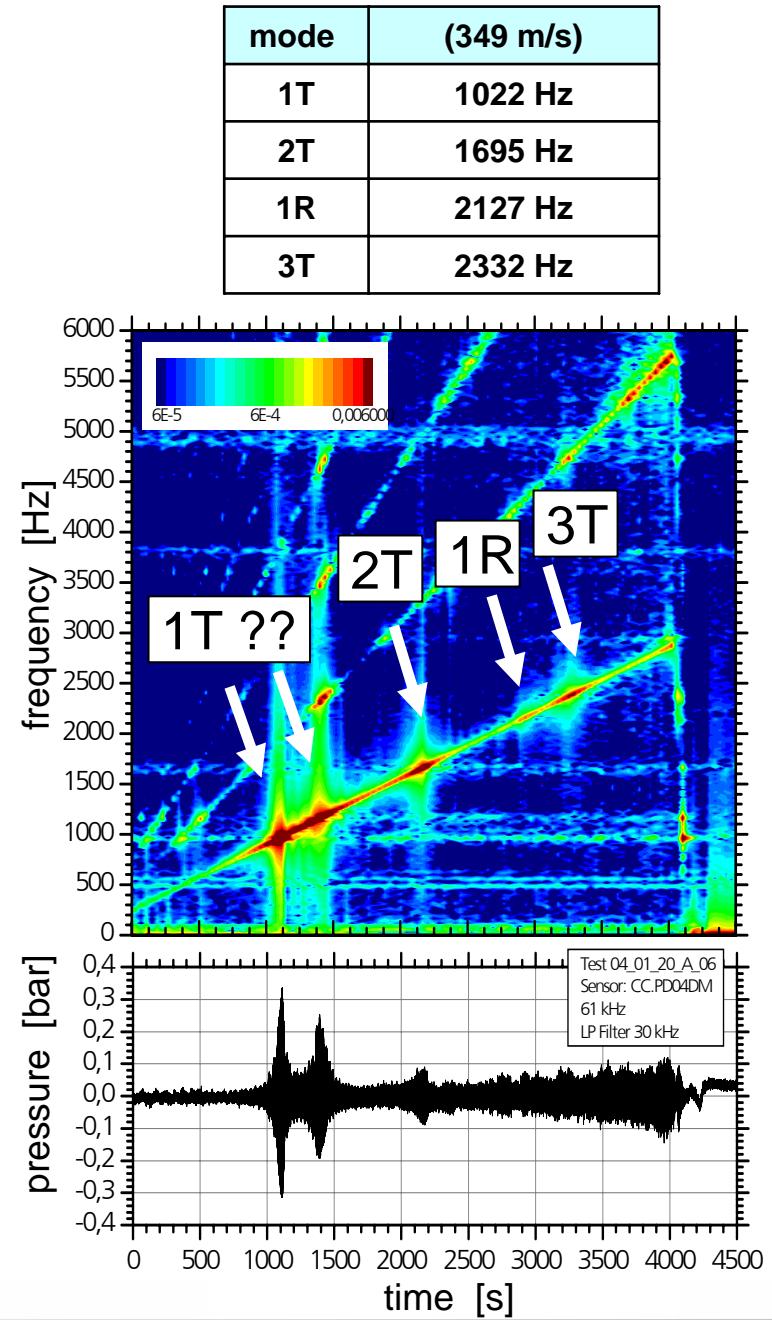
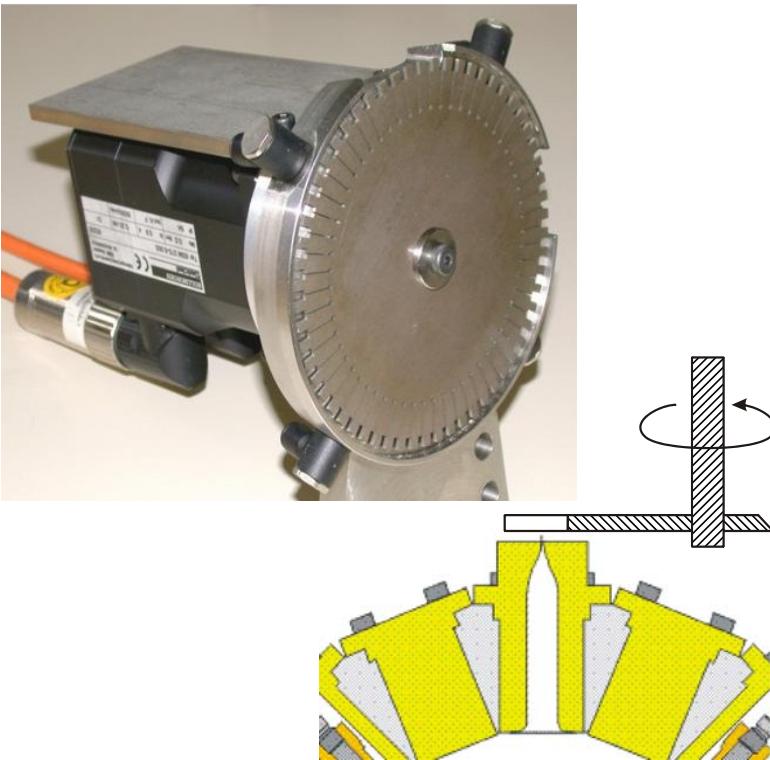


LOX/H₂-spray combustion in the CRC



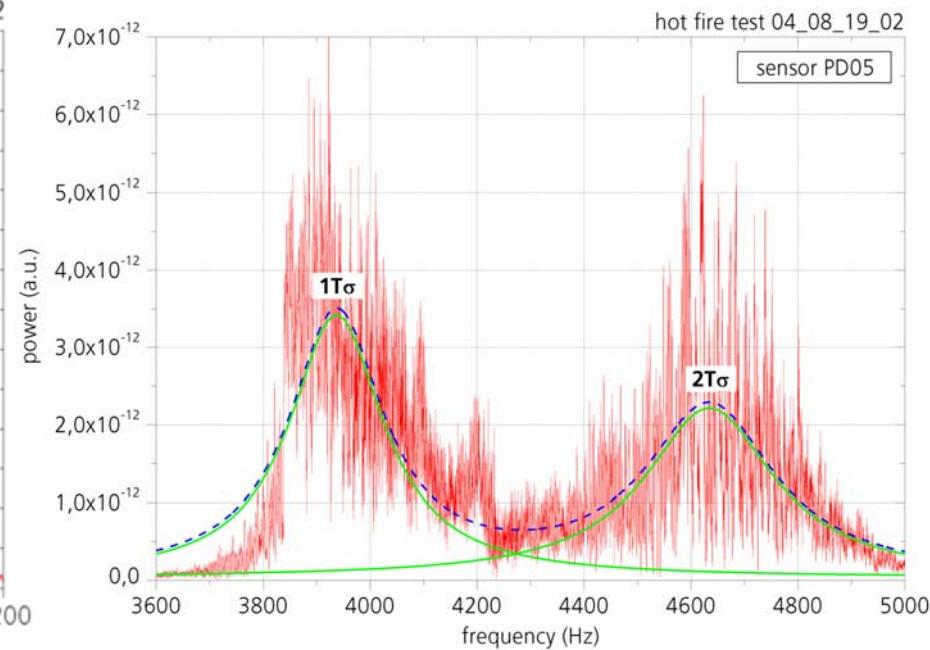
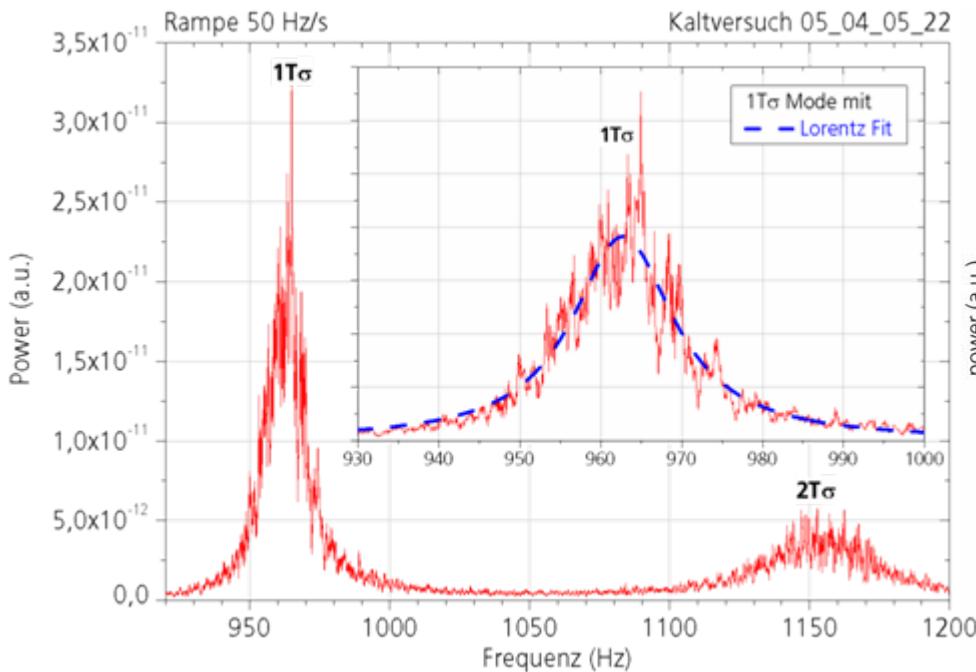
external excitation by siren ambient air

- ✓ siren at secondary nozzle exit
- ✓ frequency ramping during test with 500 Hz/s



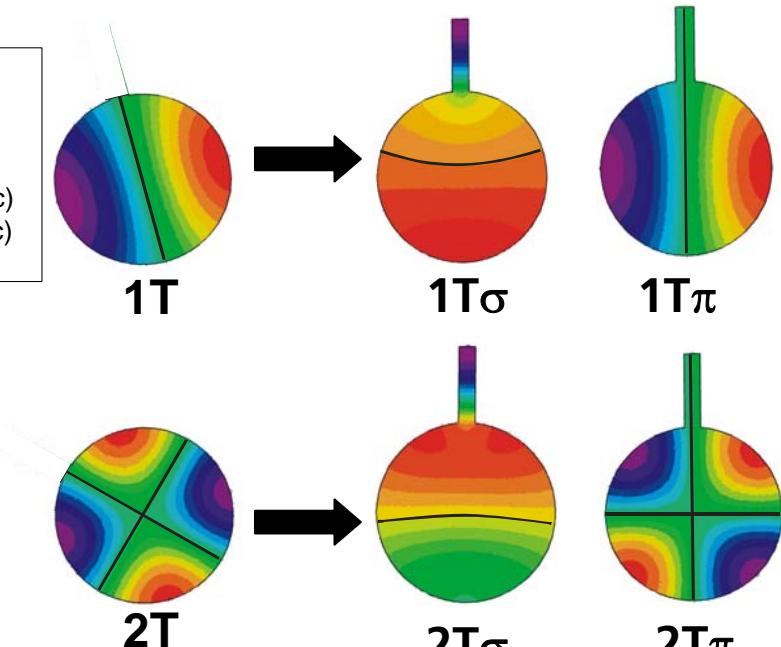
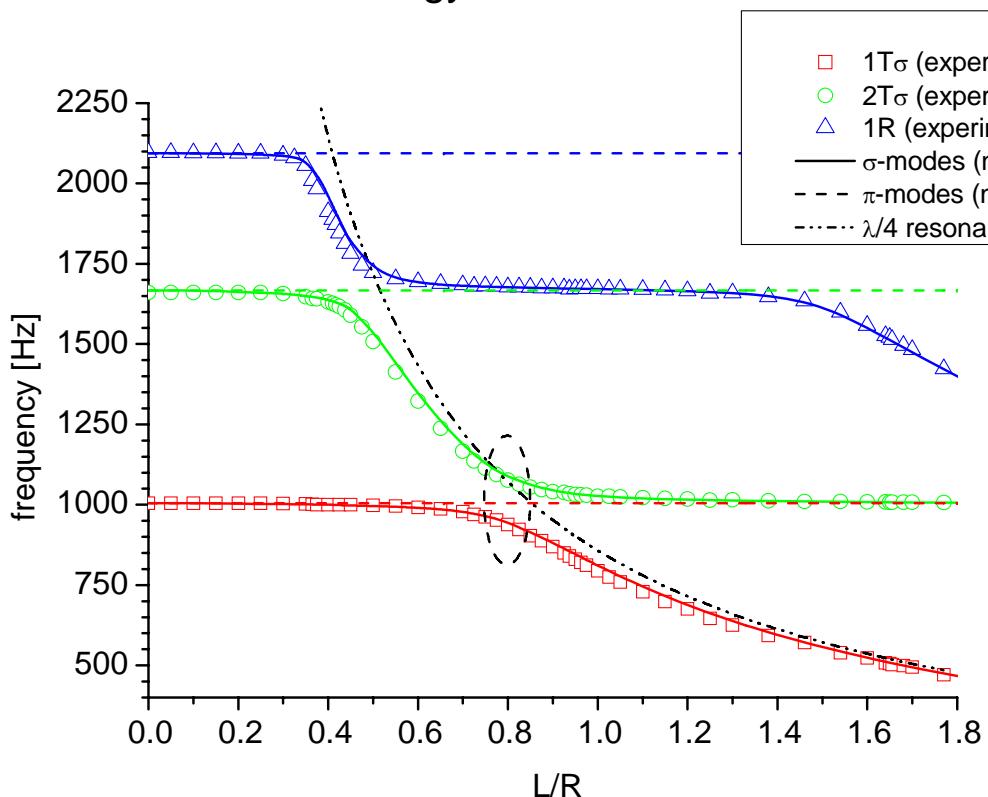
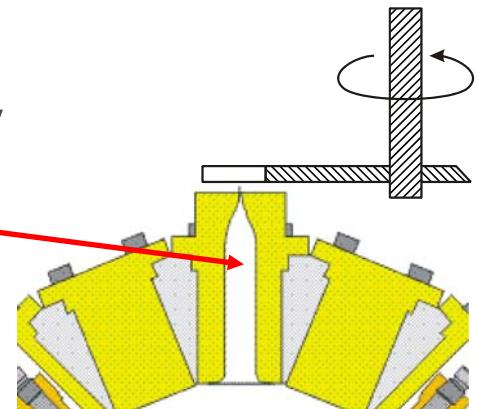
resonances near 1T-cylinder mode in combustor with secondary nozzle

- "noisy" appearance of resonances with siren excitation
- hot fire tests: line width and asymmetric profile indication for combustion/acoustics interaction



eigenfrequencies of cylinder with cavity

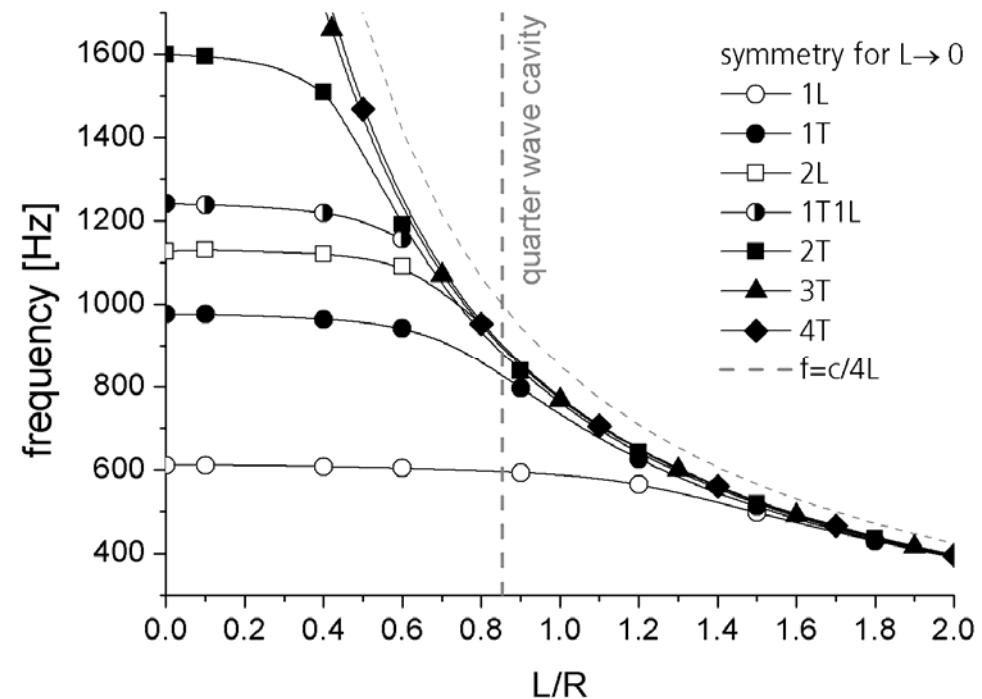
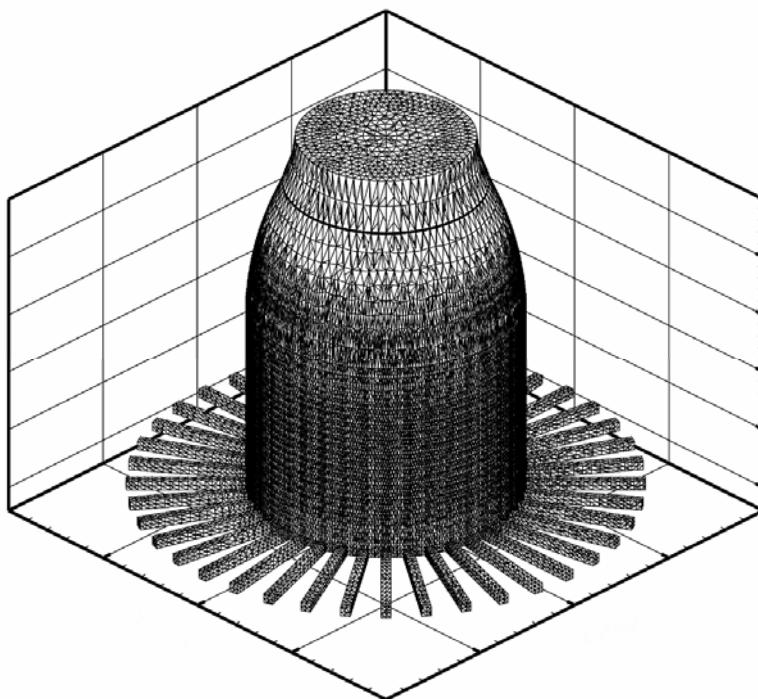
- ↗ secondary nozzle forms additional resonance volume
- ↗ cavity breaks 2-fold degeneracy of tangential eigenmodes
 - ↗ two eigenmodes of different symmetries and eigenfrequencies
- ↗ N.B.: analogy to $\lambda/4$ -absorbers



M. Oschwald, Z. Farago, G. Searby, F. Cheuret,
 "Resonance frequencies and damping of a cylindrical
 combustor acoustically coupled to an absorber",
 submitted to Journal of Propulsion and Power, June 2007

eigenfrequencies for combustor with absorber ring

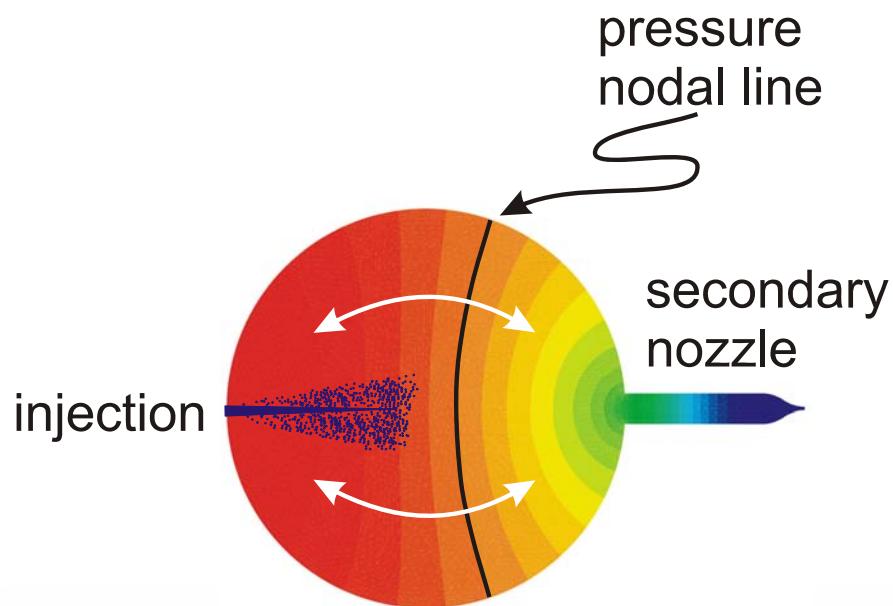
- first 8 low lying modes analyzed
- absorber ring detunes acoustic system
- modes group near to the cavities $\lambda/4$ -resonance



pressure distribution for SN at 90° and 180°

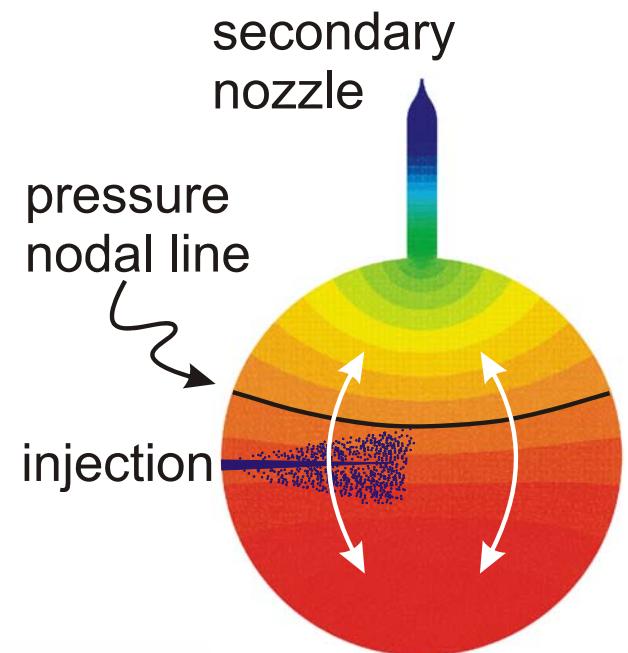
SN at 90°

- ↗ spray exposed to strong acoustic pressure fluctuation
- ↗ no transversal velocity fluctuation

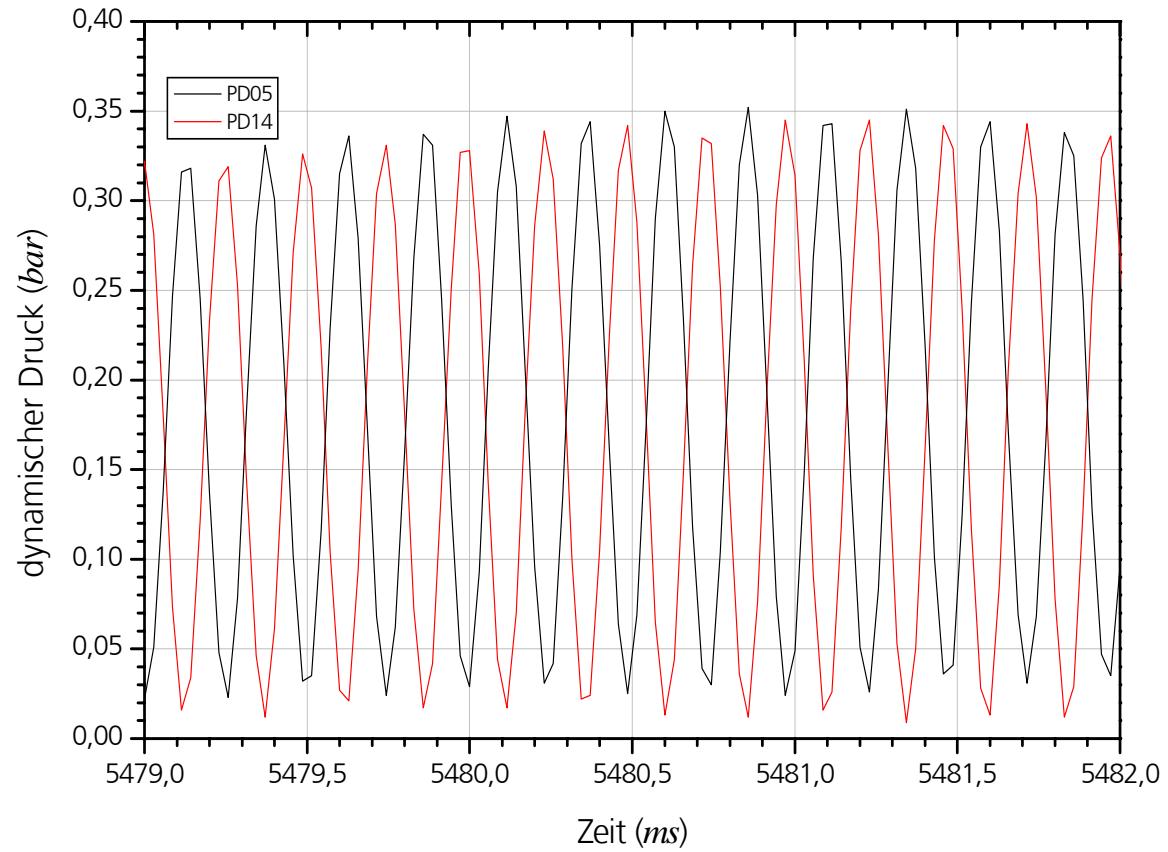
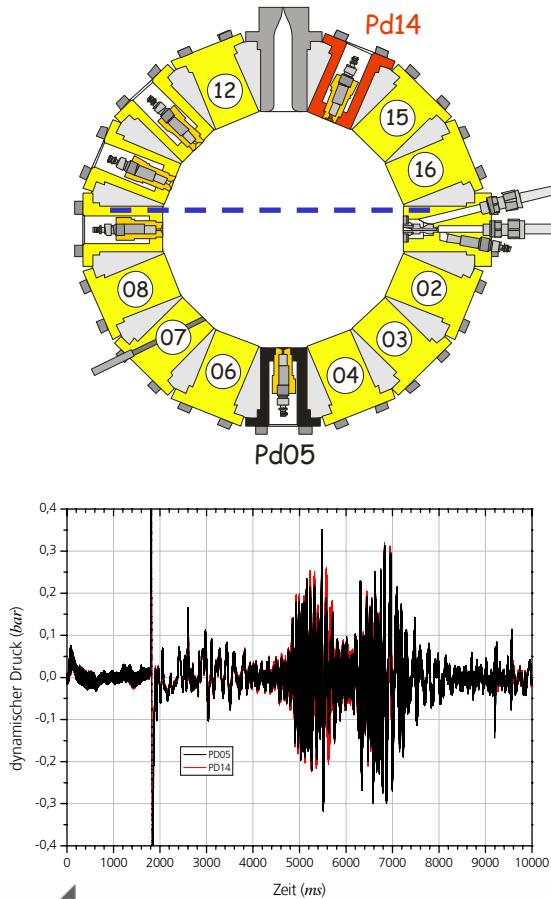


SN at 180°

- ↗ spray exposed to strong transversal acoustic velocity fluctuations
- ↗ very small pressure fluctuations

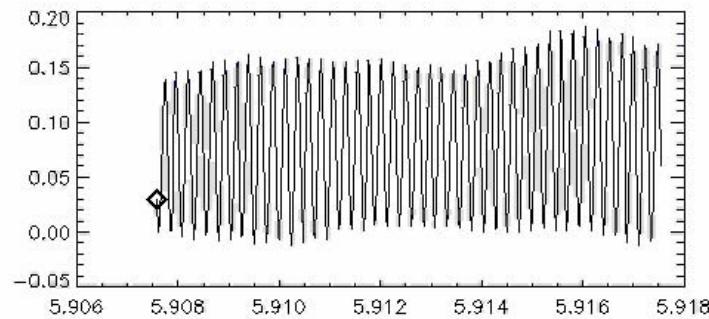
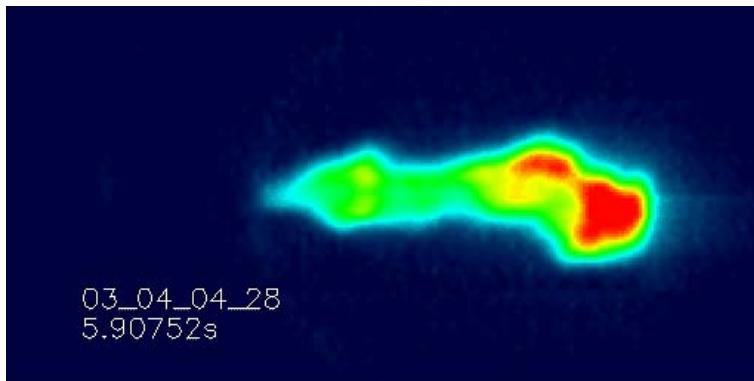


dynamic pressure on resonance for SN at 90°

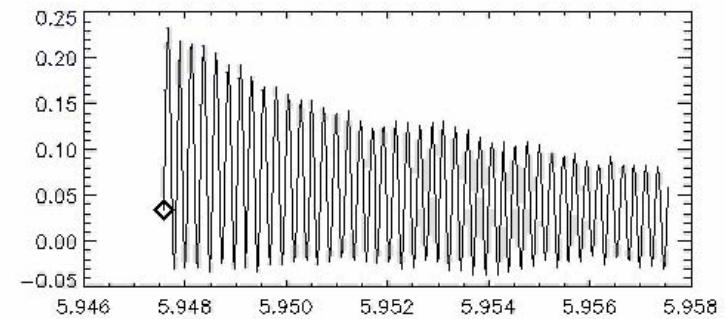
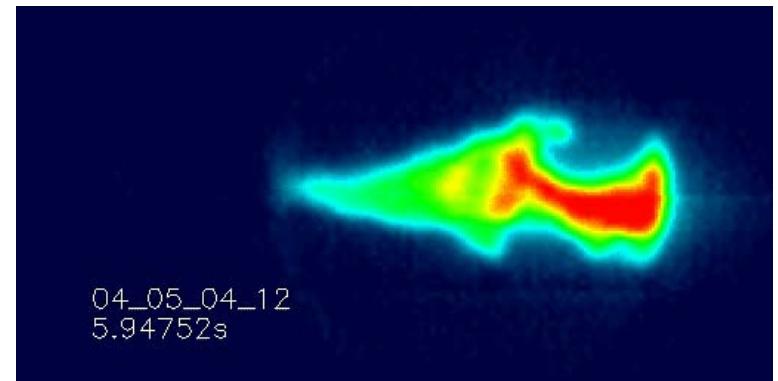


OH-chemiluminescence during excitation

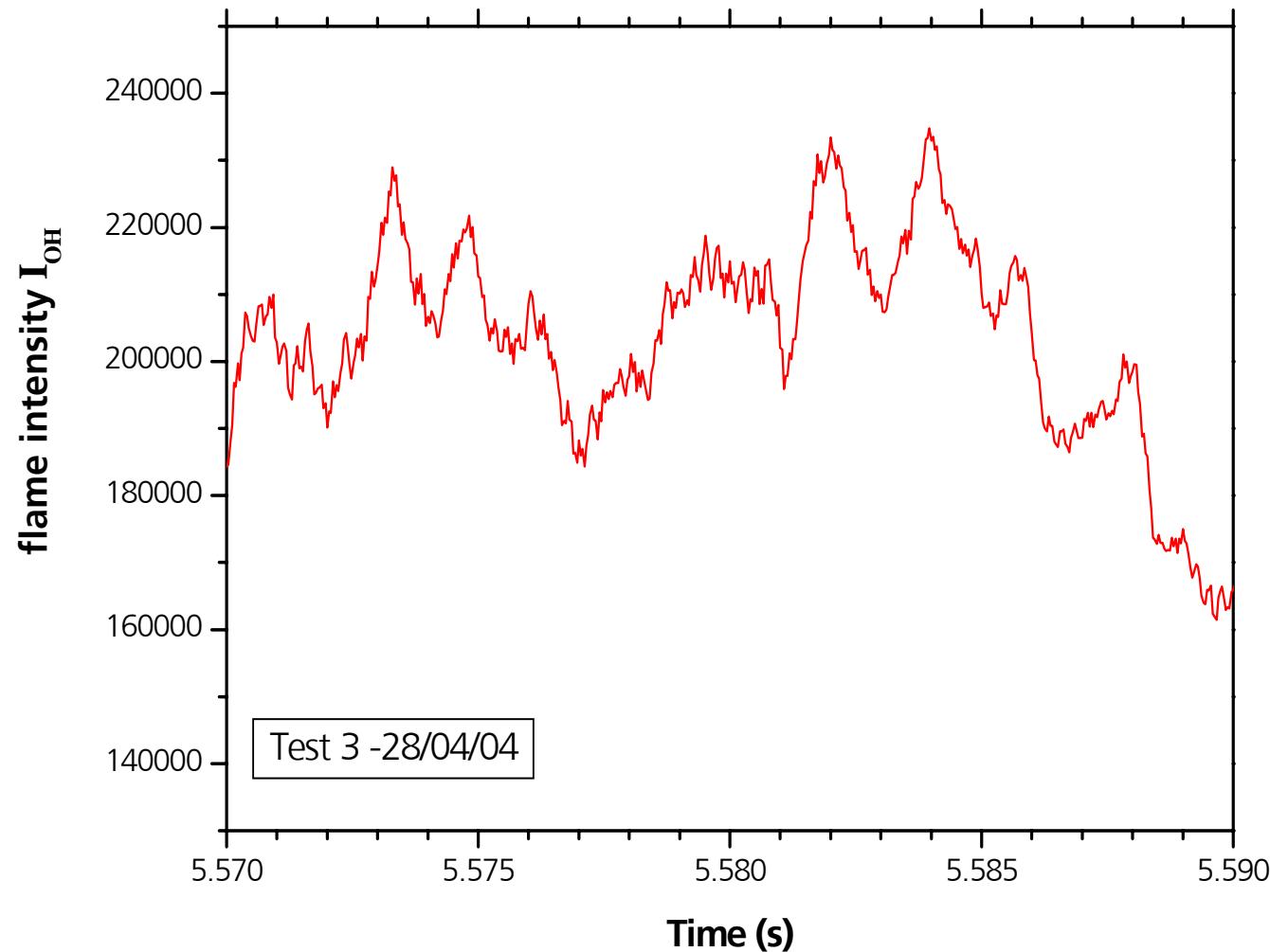
excitation with SN at 90°



excitation with SN at 180°



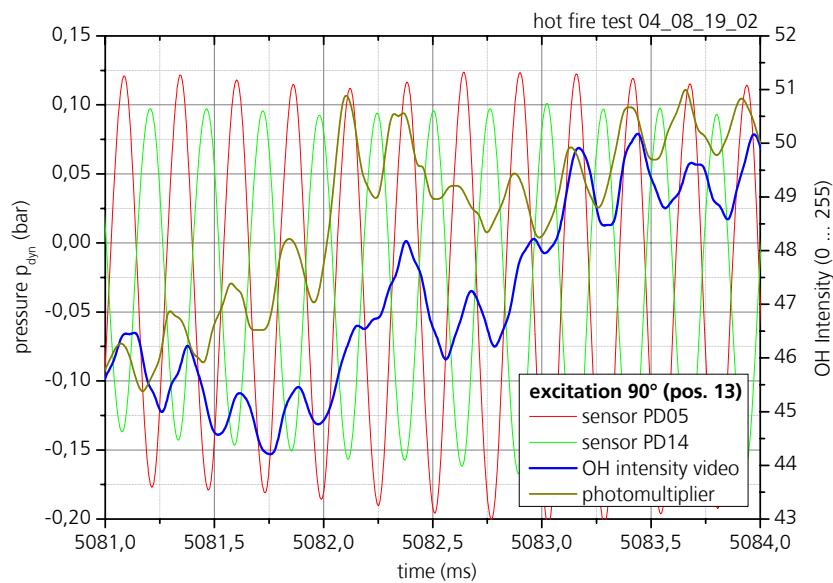
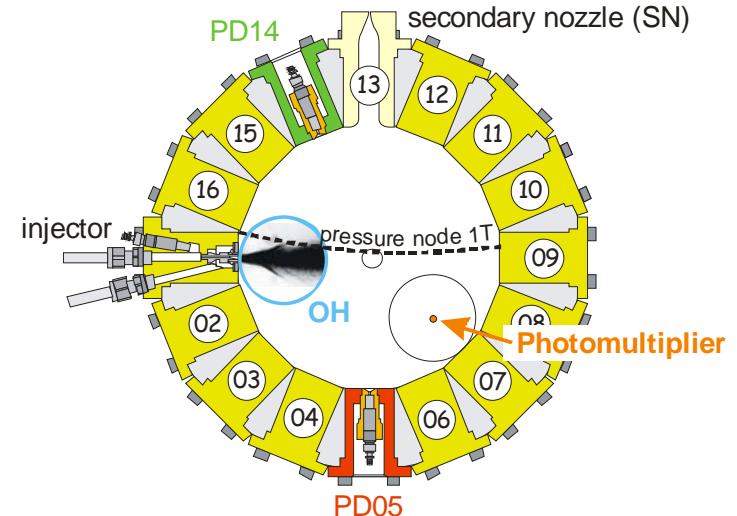
OH-chemiluminescence during excitation



intensified CCD, 27KHz, filter with transmission at 300-310nm

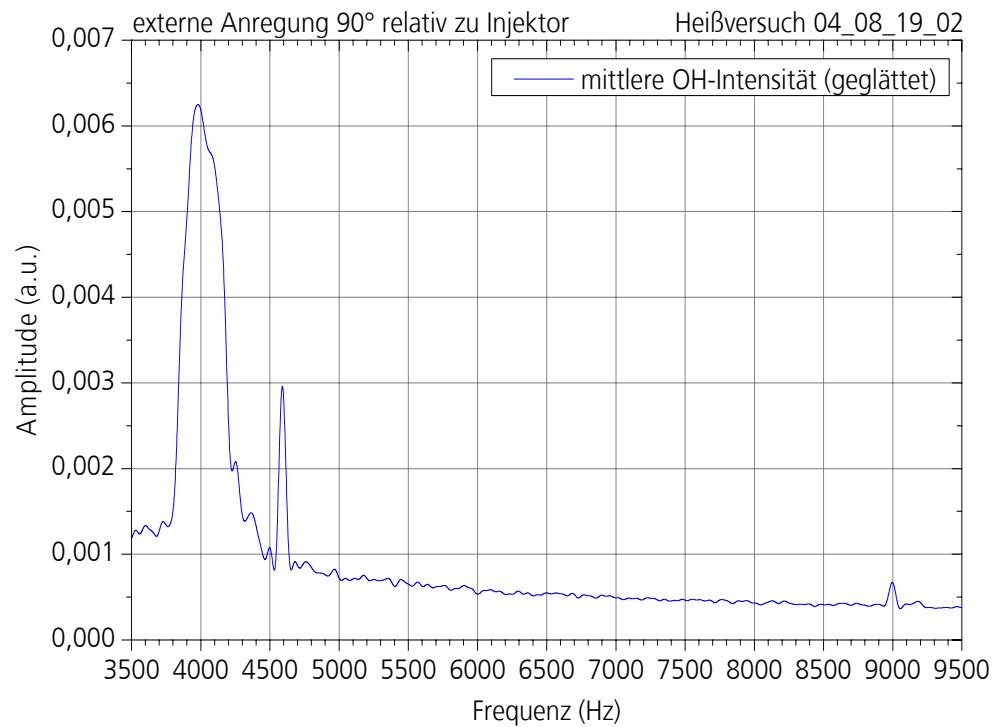
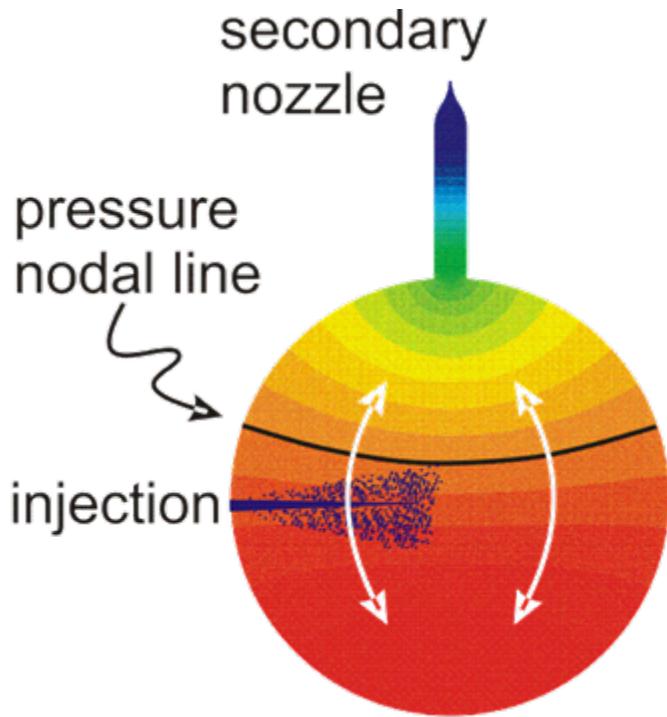
combustion response

- ↗ fluctuation of pressure and OH-emission in phase:
 - ↗ positive coupling of combustion and acoustics (Rayleigh criterium)
- ↗ excitation levels up to $p'/p \sim 20\%$: no combustion instability observed
 - ↗ damping effects suppress gain due to positive coupling
- ↗ excitation level did not show any correlation with injection conditions (J , We , R_V , ...)
 - ↗ no coupling of acoustics to spray processes in the experiments



combustion response

- at excitation with SN at 90° no significant frequency component at 2ω
 - coupling due to pressure sensitive processes



interaction index

↗ Rayleigh Kriterium:

$$\int_V \int_t Q' \cdot P' dt dV$$

↗ response factor:

$$p = \bar{p} + p' \cdot \cos(\omega t)$$

harmonic time dependency

$$\bar{Q} = \dot{\bar{Q}} + \dot{Q}' \cdot \cos(\omega t + \varphi)$$

$$N = \frac{\int_V \int_t (Q' / \bar{Q}) \cdot (p' / \bar{p}) dt dV}{\int_V \int_t (p' / \bar{p})^2 dt dV} = \frac{\dot{Q}' / \dot{\bar{Q}}}{p' / \bar{p}} \cdot \cos(\varphi)$$

$$N = \frac{I' / \bar{I}}{p' / \bar{p}}$$

chemiluminescence = heat release
 $\varphi=0$

mean flame intensity for SN at 90°

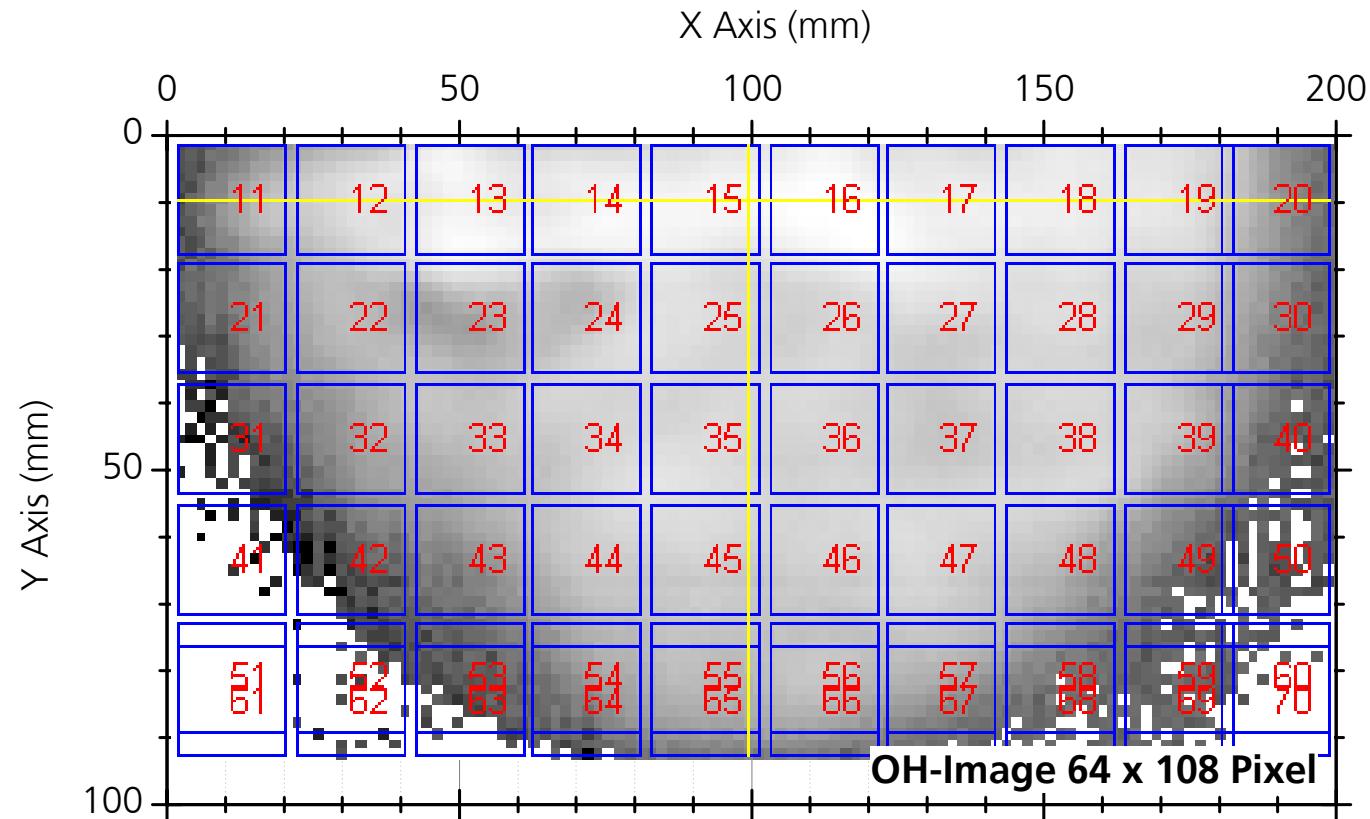
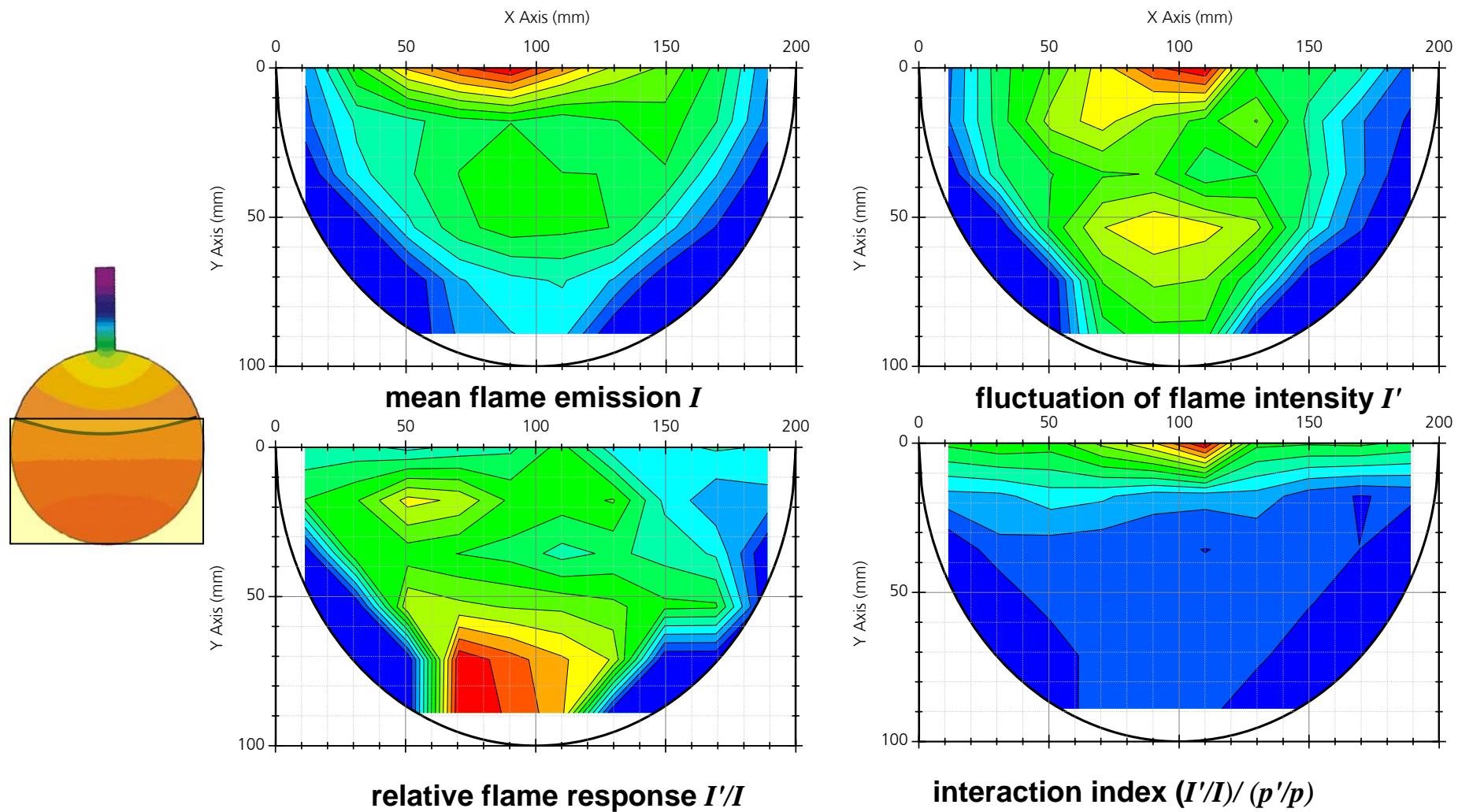


image processing on sub areas

- mean intensity I
- fluctuation I'
- reconstruction of pressure field p, p' from dynamic pressure sensors

interaction index for SN at 90°



interaction index for SN at 180°

