Design of an Optical Fiber Amplifier with Multiple Serial Pumping for Space Communications

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ABSTRACT

The feasibility of an optical fiber amplifier as a booster amplifier for transmitter-terminals of free-space coherent laser communication systems has been investigated. To enhance the amplifier’s efficiency and reliability in a harsh space environment a new pumping-scheme has been analyzed and demonstrated in an experimental set-up. The amplifier features efficient multiple serial coupling of the pump light into the multimode core of the double-clad fiber by using directional Y-couplers. Special attention has been paid to fiber-geometry, pump light absorption efficiency in the neodymium-doped single-mode core and the attenuation of pump and signal light.

Keywords: fiber amplifier, double-clad fiber, optical space communications, multimode Y-coupler

1. INTRODUCTION

The German Aerospace Research Establishment investigates the feasibility of coherent optical free space data transmission for links in satellite networks, between space probes, satellites and ground stations [1]. Nd-YAG lasers operating at 1064nm are used because of their good overall power efficiency combined with frequency stability, which is necessary for data transmission using phase modulation and coherent heterodyning in the receiver.

Though Nd-YAG lasers with the required output power (>1W) are now available, post-amplification in the transmitter is necessary because the integrated optical phase modulators cannot endure the high power levels. The modulators also cause around 5dB signal attenuation [2].

Double-clad fibers (DCF) with a Nd-doped inner signal core surrounded by a multimode pump light core are already used as single mode fiber lasers. DCFs can provide a sufficient single-pass gain when pump light intensity is optimized.

In this paper a means for cascaded multiple pump light leading based on directional multimode Y-couplers is introduced, theoretically examined and compared to experimental results. The proposed amplifier setup provides a modular design that enables redundant pump light sources and scaleable output power, both crucial in optical satellite communications.

2. EXPERIMENTAL SETUP

2.1 Structure and properties of the DCF

Using double-clad fibers for weakly pumped 4-level-system fiber amplifiers enables high-power multimode laser diodes as pump-sources, which can easily be launched into the large outer DCF multimode cladding. The used DCF (produced by IPHT, Jena) has a 5µm diameter single-mode signal core situated concentrically inside the 110µm diameter multimode pump light core. The outer cladding consists of silicon providing the required low refraction index. The pump light occasionally crosses the inner core and thereby excites the Nd-ions.

![Cross section of the applied double-clad fiber](image-url)
2.2 Pump light leading by Y-couplers

In a conventional DCF setup the pump light is end-coupled into the multimode core (MMC). This limits the number of pump sources to one laser diode (LD) at each end. By superpositioning two beams through polarizing beam splitter cubes, four LDs can be applied. The LDs are broad area emitters with $P_{PD,\text{optical}}=1\text{W}$ at $\lambda_{0,p}=809\text{nm}$ which matches well with the absorption bandwidth of the DCF at $804\text{nm} \pm 12\text{nm}$. For the Y-coupler, the LD-power is first coupled into a multimode coupling fiber (CF) which guides the light into the DCF using a grinded directional multimode Y-coupler.

![Fig.2 Cut through the multimode Y-coupler](image)

For proper matching, the diameters of both surfaces should be equal. One can solve for the grind-depth "h" and DCF bend-radius "R":

$$h = \frac{D_{DCF-MMC}}{2} \sqrt{D_{DCF-MMC}^2 - D_{CF}^2}$$

$$R = \frac{D_{CF}^2}{8 \cdot h \cdot \sin^2(\beta)} + \frac{h}{2}$$

The inner core of the DCF is not damaged by this process when $D_{DCF} > D_{CF}$. Using this geometry the axes of both fibers nearly merge into one another.

Index matching oil is needed, otherwise the unavoidable air gap between the two surfaces would cause total inner reflection of the pump light at the lapped fiber end of the CF. Bringing both areas close enough together (<1µm) allows for frustrated total inner reflection, however this was not feasible with standard grinding and positioning equipment. After the alignment process the two parts of the Y-coupler are fixed together and the index matching oil is sealed.

There are two main sources for loss of pump light at the Y-coupler. The small angle of incidence causes reflections at the transitions between the fibers and the index matching oil. To prevent total inner reflection, the relationship $n_{CF} < n_{oil} < n_{DCF-MMC}$ must be observed. At present there is no multimode fiber with exactly the DCF-MMC’s refraction index commercially available. The finite angle between CF and DCF causes an optical funnel and leads to radiation losses when steep rays exceed the DCF’s maximum angle as shown in fig.3. This can be avoided by using a CF with a smaller numerical aperture (NA) than the DCF-MMC, but this lowers the LD-to-CF coupling efficiency.

![Fig.3 Radiation losses at the Y-coupler](image)

The calculated achievable coupler efficiency is above 80%. Tests with different fibers and index matching oil combinations produced a coupling efficiency $\eta_Y$ between 64% and 86%. With $P_{PD,\text{optical}} = 1\text{W}$, the Y-coupler loss combined with the coupling loss between LD and CF (≈20%) allow for about 0.7W pump power to be introduced into the DCF-MMC.

The attenuation of pump light already inside the DCF before the coupler (“through-coupling attenuation”) is approximately 70%.

A way to side-pump the DCF by micro-prisms has been reported by [7] and [12] but with lower coupling efficiency.

3. SIGNAL AMPLIFICATION MECHANISM

3.1 Rate equation of the simplified Nd-glass system

![Fig.4 Simplified four level Nd-glass system](image)
With $\tau_{32}$ and $\tau_{21}$ being very small compared to $\tau_{21}$ the rate equation becomes

$$\frac{\delta n_i(t,z)}{\delta t} = -\sigma_{21} \cdot \phi_{io}(t,z) \cdot n_2(t,z) -$$

$$\frac{1}{\tau_f} \cdot n_2(t,z) + \eta_p \cdot W_{03}(z) \cdot [n_3 - n_2(t,z)] \leq 0$$

The change-rate of level-2 population equals the rate of pumped Nd-ions minus the rate of spontaneous and stimulated emission. In continuous-wave (cw) amplification this rate must be zero. It will be shown that $n_2$ is always small against $n_{tot}$ in the fiber amplifier so that the pump parameter $W_{03}$ is not a function of $n_2$. The gaussian radial distribution of signal intensity inside the SMC has been approximated by a rectangular distribution so intensity ratios can be substituted with power ratios.

### 3.2 Absorption and attenuation of pump light

The effective absorption coefficient for 808nm inside the doped SMC is difficult to calculate due to the uncertain absorption cross section $\sigma_{03}$ but has been measured at 23$m^{-1}$ (100dB/m). The absorption of pump light inside the DCF-SMC depends on the ability of MMC-rays to transit through the SMC. Ideally the pump light power inside the SMC ($P_{p,MMC}$) is given by the cross section ratio $\epsilon_{p,MMC}$

$$P_{p,MMC} = \epsilon_{p,MMC} \cdot P_p$$

$$\epsilon_{p,MMC} = \frac{A_{MMC}}{A_{MM}}$$

However the mode-selective absorption and reflections distort this simplified image. The refraction index step between DCF-MMC and $\cdot$SMC causes small power reflections away from the SMC for steeper angles of incidence, but reaches high values for flat angles of incidence (R=0,25 for $\psi=2^\circ$ and R=0,5 for $\psi=1^\circ$ in our DCF). As [6] has shown, the absorption coefficient for pump light in a regularly coiled DCF over fiber length starts at a rate approximately twice that of $\epsilon_{p,SMC}$, and after the absorption of the higher order axial modes drops to a value about $\frac{1}{2}$ $\epsilon_{p,SMC}$. Helical modes cannot be absorbed by the SMC. Mode mixing from helical to axial modes can be enhanced by periodically bending the winding of the DCF and by an eccentric placement of the SMC or an asymmetric MMC cross section [5]. As the DCF in our experiment is wound up to enhance mode mixing, the cross section ratio is a sufficient approximation and will be applied to further calculations.

The low transparency of the silicon cladding causes an attenuation coefficient of $\alpha_{MMC}=0.007$m$^{-1}$ (30dB/km) for the total inner reflections at the MMC-silicon transition. The combined absorption and attenuation coefficient for the pump power is

$$\alpha_{p,tot} = \alpha_{MMC} + \epsilon_{p,SMC} \cdot \alpha_{abs}$$

### 3.3 Amplification and attenuation of signal light

At $P_{sig} = P_{sat}$ spontaneous emission equals stimulated emission. $P_{sat}$ has been calculated through the measured fluorescence lifetime $\tau_i = 360\mu$s to be 6mW. The inversion-ratio for $P_{sig} << P_{sat}$ (small signal inversion) can be calculated according to

$$\frac{n_{2,small}}{n_{tot}} = \frac{W_p \cdot \tau_f}{W_p \cdot \tau_f + 1}$$

For our amplifier, this ratio could theoretically reach 26% at coupler locations with 2W pump light absorbed optimally and no stimulated emission present. With $P_{sig} >> P_{sat}$ (amplifier operating at saturation) this ratio falls to approx. 4% and thus bleaching of the ground state will not occur. This fact helps us to calculate the pump rate $W_p(z)$.

$$W_p(z) = \eta_p \cdot W_{03}(z)$$

$$\eta_p = \left(1 + \frac{\tau_{32}}{\tau_{21}} + \frac{\tau_{32}}{\tau_{30}}\right)^{-1} \leq 1$$

$$W_{03}(z) = \sigma_{03} \cdot c \cdot \phi_p(z)$$

$$\phi_p(z) = \epsilon_{p,SMC} \cdot \frac{P_{p,MMC}(z)}{A_{SMC}(\hbar \cdot c \cdot \nu_{08})}$$

The branching ratio $\eta_p$ represents losses by pumped Nd-ions that do not end up at the upper laser level. For our fiber $\eta_p \approx 0.9$. The small-signal gain ($P_{sig} << P_{sat}$) is then

$$g_{0}(z) = \sigma_{21} \cdot n_{tot} \cdot \frac{W_p(z) \cdot \tau_f}{W_p(z) \cdot \tau_f + 1} = \sigma_{21} \cdot n_2$$
and the effective gain with applied signal power

\[ g(z) = \frac{g_0(z)}{1 + \frac{P_{\text{sig}}(z)}{P_{\text{sat}}}} \]  \hspace{1cm} (13)

The absorption coefficient \( \alpha_{\text{sig}} \) caused by the necessary silica dopents is much smaller than in laser crystals, but it becomes a significant design parameter due to the long signal path through the DCF. The signal power builds up along \( z \) according to

\[ \frac{\delta P_{\text{sig}}(z)}{\delta z} = g(z) \cdot P_{\text{sig}}(z) - \alpha_{\text{sig}} \cdot P_{\text{sig}}(z) \]  \hspace{1cm} (14)

Three different gain regions can be distinguished in Fig.5. First \( P_{\text{sig}} \) rises exponentially with \( g(z) \approx \text{constant} \). When \( P_{\text{sig}} > P_{\text{sat}} \), \( g(z) \) starts to fall which causes a net linear growth of \( P_{\text{sig}} \). Finally, the gain equals the attenuation and amplification no longer occurs. In an optimized amplifier setup one can avoid the inefficient first meters before \( P_{\text{sig}} \gg P_{\text{sat}} \) by starting with a signal power above saturation (e.g. with 30mW).

This is also important from a communication-technological point of view, because a low \( P_{\text{sig}} \) allows a high amount of amplified spontaneous emission (ASE).

Fig.5 is not a realistic representation because \( P_{\text{p}} \) is not constant over \( z \) and therefore \( W_{\text{p}}(z) \) and \( g(z) \) vary as described in the following sections.

4. GAIN WITH DIFFERENT PUMPING SCHEMES

In a fiber amplifier the development of \( W_{\text{c}} \) and thus \( g \) depend on the way the pump power is coupled to the fiber. By varying the location and orientation of the Y-couplers, total signal gain and power efficiency can be influenced.

4.1 Pumping schemes for one DCF section

4.1.1 Co-directional pumping

The pump light power over fiber length for pumping in the signal direction at \( z=0 \) with \( P_{\text{p0,MMC}} \) is

\[ P_{\text{p,c,MMC}}(z) = P_{\text{p0,c,MMC}} \cdot \exp\left(-\alpha_{\text{p,tot}} \cdot z\right) \]  \hspace{1cm} (15)

with \( \alpha_{\text{p,tot}}=0.0645\text{m}^{-1} \) for our DCF. Numerical solutions are shown in fig.6 for three different initial signal powers and two different pump powers.

In contrast to Fig.5 the signal degenerates when the pump intensity diminishes. With higher initial signal powers the maximum output power is reached after a shorter fiber section.
The gain is decreasing and higher pump power is required to overcome attenuation and obtain useful amplifications.

4.1.2 Reverse pumping

In the case of reverse pumping at $z=L$ in the negative $z$-direction, we derive

$$P_{p_r\cdot MMC}(z) = P_{p_0\cdot MMC}\exp(-\alpha_{p,\text{tot}}(z-L))$$  \hspace{1cm} (16)

No signal reduction takes place at the end of the section because pump power grows steadily with signal power towards the coupler. However this does not affect signal output very much for small $P_{sig0}$. The effective gain is slightly higher than in the co-directional pumping case. With higher initial signal powers, the attenuation due to excessive fiber length rises significantly and the optimum fiber length is shorter.

4.1.3 Bi-directional pumping

Pumping from both section ends with $P_{p_0,c}$ at $z=0$ and $P_{p_0,r}$ at $z=L$ results in the following pump power distribution

$$P_{p_b\cdot MMC}(z) = P_{p_0,c\cdot MMC}\exp(-\alpha_{p,\text{tot}}(z-L)) + P_{p_0,r\cdot MMC}\exp(-\alpha_{p,\text{tot}}(L-z))$$  \hspace{1cm} (17)
4.1.4 Discussion of the three cases

Higher pump power causes a better average gain coefficient with high $P_{\text{sig0}}$ and therefore efficiency rises with stronger LDs. The optimum fiber length gets shorter as $P_{\text{sig0}}$ increases. Combinations of co- and reverse-pumping must take into account the optimum fiber length which is derived by the preceding calculations.

In all three cases fiber length is relatively uncritical when $P_{\text{sig}}$ is small and becomes crucial with higher powers because of the attenuation inside the SMC.

4.2 Cascaded multiple pumping

This section discusses signal amplification for one of the several possible pumping schemes.

The investigated setup has an initial reverse-pumping coupler followed by seven bi-directional pumped fiber sections. $P_{\text{sig0}} = 5P_{\text{sat}}$ and $P_{\text{p0}}=700\text{mW}$ at every Y-coupler has been presumed.

Fig.12 Bi-directional pumping with large $P_{\text{sig0}}$ and optimum L

The signal output power after 305m of DCF is 3.1W. This means an efficiency of $3.1\text{W} / (0.7 \times 15\text{W}) = 0.30$ inside the DCF.

The remaining pump power from the preceding fiber section is hereby supposed to be totally attenuated inside the Y-Coupler. Through-coupling of this power can be enhanced by optimizing the coupler geometry with this aspect. An arrangement as depicted in Fig.15 would provide the highest gain and efficiency for one fiber section. Methods to enhance through-coupling are discussed in section 6.

Fig.14 Growing of $P_{\text{sig}}$ with cascaded bi-directional pumping and optimized fiber section lengths. Couplers are positioned at the marked lengths.

Fig.15 Summing up the powers of several LDs with improved Y-couplers.

5. RESULTS

Directional multimode Y-couplers have been practically tested to couple up to 86% of pump light from a standard multimode fiber into a DCF-MMC. The feasibility of building a cascaded multiple pumped DCF amplifier with output greater than 3W has been shown by simulation.

The total calculated system efficiency (socket-to-$P_{\text{sig,out}}$)

$$\eta_{\text{tot}} = \eta_{\text{LD,el-opt}} \cdot \eta_{\text{LD-dCF}} \cdot \eta_{\text{CF}} \cdot \eta_{\text{abs,SMC}} \cdot \eta_{\text{abs,SMC}} \cdot \eta_{\text{pout}} \cdot \eta_{\text{gain}}$$

lies between 7% and 14%, depending on the applied constellation. The CF-to-output efficiency (without $\eta_{\text{LD,el-opt}}$ and $\eta_{\text{LD-dCF}}$) is then between 20% and 40%.

With higher required output powers the fiber sections between the couplers must be shortened to maintain a high pump rate. This leads to a lower $\eta_{\text{abs,SMC}}$ because remaining pump light inside the DCF is radiated out of
6. CONCLUSION AND IMPROVEMENTS

Losses of remaining pump light at the Y-couplers ("through-coupling-efficiency") can be reduced by using a smaller CF as this loss is proportional with the size of the coupler’s transitional area. Ignoring the problem of poorer laser diode to CF coupling allows narrower positioning of the couplers and thus enhances pump power, without losing the pump light from the preceding coupler. Much higher signal output power could then be achieved. This variant has not yet been investigated because our couplers attenuate the remaining pump light too much. However, high power laser diodes with improved beam quality are now commercially available, so efficient coupling from the LDs into a pigtailed CF of about 50µm is now feasible.

A computer ray-tracing model of the Y-coupler is being set up to find the optimum coupler geometry. This model will also take into account multiple back-reflections along the coupler length, losses by rays that exceed the fibers' N.A., helical modes, polarization dependent effects and losses by non-optimum surface-shapes and alignment. It would also allow investigations of the mode-distribution and the helical-ray ratio inside the DCF-MMC.

The silicon cladding causes problems due to the attenuation of the pump light and its susceptibility to damage. Its thermal instability prevents the construction of a fused Y-coupler between the pump fiber and the DCF. The fiber producer is currently working on a hard-cladding to replace the silicon. A fused coupler combined with matching refraction indices of pump fiber and DCF-MMC would have the lowest coupling losses. Besides, the DCF can not be glued tightly enough to the polishing block with the soft silicon and so the glass core sometimes breaks during the polishing process, another argument for a hard outer cladding.

Higher Nd-doping will increase the small signal gain coefficient. However from a certain concentration on the Nd-ions tend to build clusters and thus the signal attenuation rises stronger than the overall gain improves. Optimum has to be found. A smaller MMC to SMC cross-section ratio (maximum possible single mode diameter is approx. 7.5µm) also increases the pump rate inside the SMC. Increasing of \( \tau \) could reduce losses by spontaneous emission and thus increase amplifier gain and overall efficiency. The ASE would become smaller and thus the additional signal noise would diminish. In certain Nd-glass, a \( \tau \) of 600µs has been observed.

Rayleigh-Scattering has not been regarded as an additional noise source, because after the amplifier fiber there is free space transmission and thus no further scattering takes place like in fiber communications.

Only one variation of several possible coupler constellations could be investigated in this paper as an optimum design depends on too many parameters. A tradeoff must be found between output power and other amplifier requirements, i.e. overall power efficiency, redundancy for LD failures and scaleability of output power.

The concept of multiple cascaded pumping by Y-couplers offers a wide variety of DCF-amplifier setups to fulfill the application-specific differing demands.

7. ACKNOWLEDGMENTS

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8. REFERENCES

9. SUMMARY OF DCF PROPERTIES

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<td>NAMMC</td>
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<tr>
<td>NASMC</td>
<td>0.14</td>
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<tr>
<td>NaNd</td>
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</tr>
<tr>
<td>( \tau )</td>
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<td>( P_{sat} )</td>
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<tr>
<td>( \alpha_{MMC} )</td>
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<td>( \alpha_{abs} )</td>
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<td>( \alpha_{sig} )</td>
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<tr>
<td>( \sigma_{03} )</td>
<td>( \approx 1 * 10^{-24} ) m^2</td>
</tr>
<tr>
<td>( \sigma_{21} )</td>
<td>( \approx 1.1 * 10^{-24} ) m^2</td>
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<tr>
<td>( c )</td>
<td>1.95 * 10^8 m/s</td>
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<td>( v_{1064} )</td>
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<tr>
<td>( v_{808} )</td>
<td>3.7 * 10^14 s^-1</td>
</tr>
<tr>
<td>( \eta_{p} )</td>
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10. ABBREVIATIONS

DCF: double-clad fiber  
SMC: single mode core  
MMC: multi mode core  
LD: laser diode  
CF: coupling fiber, carrying the pump light from the laser diode into the DCF  
\( W_p \): pump rate  
\( W_{03} \): pump parameter  
\( \phi_{p} \): photon-flux of pump light inside DCF-SMC  
\( \phi_{sig} \): photon-flux of signal light inside DCF-SMC  
\( \eta_{p} \): pumping efficiency ("branching ratio")  
\( \epsilon_{p,SMC} \): transit coefficient for pump light from MMC through SMC  
\( \alpha_{sig} \): att. coeff. of signal light in the SMC  
\( \alpha_{MMC} \): att. coeff. of pump light in the MMC  
\( \alpha_{abs} \): absorption coeff. of pump light in the SMC  
\( \alpha_{tot} \): combined absorption and attenuation coeff. of pump light  
\( \sigma_{03} \): absorption cross section of Nd for 809nm  
\( \sigma_{21} \): stimulated emission cross section of Nd for 1064nm  
\( \tau_{F} \): fluorescence lifetime without stimulated emission  
\( c \): speed of light inside the DCF  
\( P_{sat} \): saturation signal power  
\( P_{p0} \): inserted multimode pump power at Y-coupler  
\( P_{sig0} \): signal power at the start of one fiber section  
\( g_0 \): small signal gain coefficient  
\( g \): actual signal gain coefficient  
ASE: amplified spontaneous emission