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Diversifying training data does not improve generalizability of neural network models for PV identification ⊕ ⊘

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ABSTRACT

Data about behind-the-meter photovoltaics (PV) installations may be difficult to obtain for researchers. A number of investigators have considered deep learning as an attractive solution to this challenge, capable of directly identifying PV installations from aerial or satellite images. Deep learning models are well known to experience challenges when working with data from sources that they have never been exposed to. This study investigated whether generalizability can be improved by diversifying training data across available labeled data sources. We assessed the performance of models trained on all possible combinations of six different labeled datasets of aerial PV imagery, with a fixed number of total training images. Unfortunately, our results indicate that no combination of model training data achieved generalized performance that approaches models trained on data from a target data source. This implies that generalized ResNet models cannot be developed simply by modifying the configuration of the training data. Consequently, researchers should expect that some degree of data labeling is likely to be necessary when adapting these models to new applications, but our results do indicate that significant performance improvements are possible with only small (~20%) introductions of target data. Future work may investigate alternative architectures, expanded training datasets, or ways to reduce the amount of labeled data necessary to adapt a model for a given application.

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I. INTRODUCTION

A global transition away from carbon-intensive energy sources is under way, requiring growth of renewable, carbon-free forms of energy generation to meet societal energy needs. In particular, solar photovoltaics (PV) represent a renewable energy source that directly converts freely available solar irradiance into electricity. PV generation is growing quickly due to its comparatively low levelized cost of electricity, leading solar to represent a significant share of optimal energy scenarios for the United States.

The distributed placement of generation facilities is a common feature of most renewable energy systems, arising from the distributed nature of renewable energy resources. PV generation facilities vary widely in scale, ranging from large "utility-scale" generation facilities consisting of thousands of panels down to small scale systems on residential rooftops that may be made up of only a few panels. The largest of utility scale systems are rated to produce on the order of hundreds of megawatts at the peak capacity, while residential systems may be rated for a few kilowatts. While this represents a scale difference as large as five orders of magnitude, residential systems are not negligible. To the contrary, small but numerous residential PV systems have been reported to represent more than 40% of global PV capacity.²

In order for the energy transition to be planned for, studied and understood, access to information about PV installations is a strict necessity. For example, technical data about distributed PV installations are necessary to forecast aggregate-level generation, needed to monitor and operate regional electricity grids. In general, no worldwide comprehensive inventory of PV installations exists, particularly when considering small-scale residential systems.³ Where data exist, it is likely to vary significantly by jurisdiction in the level of aggregation, comprehensiveness, and availability. Nonetheless, there is at present a gap in accessible information about small-scale, behind-the-meter PV installations that remains of interest to researchers, policy-makers, utility operators, and other stakeholders.

One potential solution to this problem lies in the use of computer vision systems operating on satellite or aerial imagery. These types of imagery offer visual indication of the presence of PV systems and

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could potentially allow investigators to quantify details of PV installations.⁴ Advances in computing technology have made implementation of deep learning-based computer vision techniques accessible for individual researchers, enabling this avenue of constructing a PV inventory. While studies have demonstrated this application for identifying PV installations,⁵ no ready-to-use system for general identification of PV installations exists, and a significant amount of ongoing research continues to advance the field. The most desirable system for the research community would be flexible and easy to access, allowing individual researchers to reliably process new image datasets as they become available so that data about PV installations can be used for further analyses. Thus, in order to serve as a tool for the research community, an ideal PV identification system would be available with low barrier to entry (e.g., open access, small and efficient, works on individual desktop computers) and could be generalized across unseen images. This study will examine the literature with respect to this ideal and investigate the generalizability of common small scale models for identification of PV from image data.

II. BACKGROUND

As stated previously, data on small-scale PV installations (e.g., location, capacity, and characteristics) are needed for many research and operational activities, but are typically not openly available³ or suffer from incongruities across data sources. Work by Yu *et al.*⁵ leverages computer vision to identify PV installations and demonstrates the practical outcomes of using automated processes to build a database of PV installations. They apply the generated installation data for analysis of PV development measured against other geospatial and demographic variables. A follow-up study from the same group also considered similar analyses including time resolved effects.⁶ Another example application comes from Perry and Campos,⁴ who demonstrate the ability of processing Google Earth imagery to verify metadata about PV installations.

A. Architectures

Consequently, research into PV identification using computer vision on remote sensing imagery has been an area of interest from several investigators in recent years. Early efforts made use of generalized machine learning techniques, but most more recent efforts employ deep convolutional neural network (CNN) based approaches. For example, Yu et al. conducted an extensive study utilizing deep learning techniques. Other groups have also demonstrated the use of neural networks to identify PV installations using data from Germany, 6.9 China and worldwide data. 11,12

Some studies have focused on advancement of different CNN architectures to improve performance at the task. Zhu *et al.* developed a network architecture specifically for identification of PV and performed transfer learning on a highly similar site with good success. Guo *et al.* noted the difficulty of class imbalance as a common issue for PV segmentation tasks, whereby more negative (i.e., background) than positive pixels are typically present in datasets. Hey develop an architecture with characteristics that show favorable performance on a single dataset when dealing with variation in resolution and accommodating class imbalance. Let Zech and Ranalli utilized a method that estimates uncertainty of the predictions as a part of the characterization of PV identification task.

B. Generalizability

Challenges remain in developing these techniques for more generalized applications. To make the most use of a PV identification system, users need to be able to apply the system to inventory PV installations in new data as it becomes available. This is difficult, because studies have shown that CNN performance suffers when applied to data that is different from its training data. ¹⁵ Insufficient attention has been paid to the problem of generalization because for most research, models are often trained and evaluated on data from the same geographic location. ¹⁵

When it comes to generalization of CNN models, statistical similarity between training data and the target application location is important. Often this similarity is disturbed by geographic differences.^{3,15} Differences in data may arise from the nature of the remote measurement (e.g., satellite vs aerial imagery, use of orthographic rectification, and different spatial resolution), differences in the sensor (e.g., type, sensitivity, and calibration), differences in the site geography (e.g., urban vs rural, construction similarities, and types of features), or differences induced by temporal effects (e.g., images from summer vs winter, varying atmospheric conditions, and different shadowing).3,16 Dataset quality is also a potential source of error due to unknown mistakes in the labeled "truth" data. Openness of data, code, and methods is important for research in terms of developing repeatable approaches that can also be practically applied. Satellite data, which offer potentially the widest geographic coverage, may be limited by spatial resolution. Li et al. investigated varying pixel resolutions, observing that best performance occurred with resolutions finer than 0.3 m, ¹⁶ which does allow for some satellite data to be useful, but is close to current resolution limits.

A few studies have attempted to investigate the generalizability of CNN models. Wang *et al.* compared performance from two cities in California (Fresno and Stockton) from the same data source and observed poor generalization.¹⁵ They determined that improved performance requires substantial quantities of local data, but less than the full training dataset. They were also able to use analysis of encoded data through a t-SNE algorithm to identify some of the limitations in performance.¹⁵ Hu *et al.* conducted a comparison of predictions on data from the United States, comparing data from Connecticut and San Diego, California, and observed significant difficulty in generalizing.³ It is not yet known to what degree is possible to deliberately create a generalized model based on the existing training data.

C. Contribution of this work

This study, an extension of a work presented at a recent conference, ¹⁷ aims to fill a gap in research on generalization of CNN for PV identification tasks. Specifically, we investigate how well ResNet models trained on a single small dataset can be applied to data from other locations and sources, and whether diversification of the training data can improve performance. We conducted a comprehensive evaluation of how results from a model trained on a given dataset generalize to other locations by incorporating data from six distinct aerial imagery datasets covering Northern Germany, Southern France, and the United States. These datasets were sourced from different labeling methodologies and acquisition modalities, making them indicative of the variety of imagery data that researchers may encounter when attempting to perform analyses on a new location. We investigate whether generalizability can be improved by incorporating more

diverse training data from multiple locations to provide a realistic representation of how well models can be applied outside their initially trained context.

III. METHODOLOGY

A. Model architecture

Most modern image identification tasks make use of fully convolutional neural network architectures. U-net architectures, first introduced for the segmentation of biological imagery, ¹⁸ have been applied for identification by several previous investigations. ^{9,14} In u-net architectures, the encoder and decoder have a symmetric configuration that resembles a *u*-shape. In this study, we utilized open-source python implementations of u-net from the *segmentation models* library, ¹⁹ built upon Tensorflow and Keras. ²⁰ All models in our study were trained beginning with pretrained weights from *ImageNet*, ²¹ which were included with the library.

Multiple backbones were considered for the u-net model including ResNet-34, ResNet-50, and ResNet-101. Initial tests indicated that there was no significant difference in performance with increasing backbone complexity when comparing models trained and tested on the same dataset. The results for this comparison are shown in Table I. This is consistent with prior results in a different study by the authors⁹ for this task. Consequently, subsequent results reported here will come from the ResNet-34 based models, as those offered faster compute times. In addition to comparing ResNet backbones, we also ran each model for two different random seeds to ensure that results were independent of the individual image subset selection. Using these comparisons, we also obtained information about the repeatability via values for the average standard deviation of the metrics. Standard deviations of the metrics were 0.04 for intersection over union (IoU) score, 0.05 for precision, and 0.06 for recall. These levels will be used as indicators of the statistical significance of subsequent results.

Other architectures for neural network based image segmentation exist and have various advantages or disadvantages. We limited ourselves to ResNet architectures in this study because they are common, well supported by existing open source implementations, and meet the need of being easy to implement on desktop hardware by individual investigators. As our primary interest was in comparing the impact of diversifying the training data on generalizability of the resultant model, using a fixed architecture still provides the opportunity to explore training dataset combinations. Nonetheless, we acknowledge the use of a fixed architecture as a limitation of this work and leave exploration of the architecture space for future investigations.

B. Training and evaluation

The primary goal of this study was to compare the generalizability of trained models using across diversification of the training

TABLE I. Backbone performance comparison.

		IoU score by train/Test dataset							
Backbone	CA-F	CA-S	FR-G	FR-I	DE-G	NY-Q			
ResNet-34	0.71	0.61	0.81	0.69	0.63	0.81			
ResNet-50	0.68	0.57	0.81	0.67	0.63	0.81			
ResNet-101	0.67	0.60	0.80	0.68	0.63	0.83			

datasets. Consequently, to maintain consistency between the models, we used a fixed architecture (ResNet-34 as described previously), loss function, and tuned set of hyperparameters for the DE-G dataset that were identified by the authors in a previous work on the topic. The process focused on workflows achievable by consumer-grade desktop computing hardware (Xeon Silver 4210R processor with 32 GB RAM and NVIDIA RTX A2000 12GB GPU). Code was developed in Python and made use of the segmentation models library, 19 which utilizes Tensorflow and Keras²⁰ as the basis for formulating the model architecture. Each model was trained individually from a common starting point. Training of each model required approximately 3 h, which was a reasonable timeframe for iteration and improvement. Encoder weights were frozen throughout training, and early stopping after 10 consecutive epochs without a reduction in the loss function was used to prevent overfitting, retaining the weights with the best validation loss performance. While the 1000 image datasets considered here are relatively small by computer vision standards, we utilized data augmentation with the following parameters to simulate the effects of a larger dataset: rotation (up to 30°), zoom (factor of 0.2), and height and width shifts (factor of 0.1 each).

Several metrics were used to evaluate the performance of each individual model. These are based upon the four truth categories for the predictions: true positives (TP), false positives (FP), true negatives (TN), and false negatives (FN). We relied on the intersection over union (IoU) measure to indicate the overall performance of the models, as it produces values that depend most closely on overall match between ground truth and predictions. Precision and recall are also useful metrics that provide other indications about model performance. Precision indicates the percent of positive predicted pixels that correspond to ground truth positives, while recall indicates the percentage of ground truth positives that were predicted. Definitions of these metrics are given by the following three equations:

$$IoU = \frac{TP}{TP + FP + FN},$$
 (1)

$$p = \frac{TP}{TP + FP},\tag{2}$$

$$r = \frac{TP}{TP + FN}. (3)$$

C. Source data

To compare the generalizability of the neural network models, we utilized six datasets that contained labeled PV installations. These datasets represented different sources, resolutions, and labeling methodologies. All datasets were filtered to retain only images that contained PV. Datasets with large tiles were first sliced to a manageable size. On final processing, all images were scaled to have an image size of 576×576 for compatibility with the model workflow, which resulted in a corresponding scaling up or down of the resolution of each image. Descriptions of the datasets will continue in the following paragraphs, but a summary of each resultant dataset is provided in Table II.

Two datasets consisted of openly available labels and PV imagery data from nearby cities in California: Fresno (CA-F) and Stockton (CA-S). These were previously published by Bradbury *et al.*²² These datasets consist of 30 cm resolution aerial orthoimagery tiles obtained from the United States Geological Survey (USGS). Images were

TABLE II. Datasets. 17

Dataset	Tot. tiles	Tile size	Resolution	Scaled res	Refs.
CA-F	1044	625 × 625	0.3 m/pix	0.32 m/pix	22
CA-S	4192	625×625	0.3 m/pix	0.32 m/pix	22
FR-G	13 303	400×400	0.1 m/pix	0.07 m/pix	23
FR-I	7865	400×400	0.2 m/pix	0.14 m/pix	23
DE-G	1325	639×640	0.18 m/pix	0.2 m/pix	9
NY-Q ^a	1007	625×625	0.15 m/pix	0.16 m/pix	25

^aLabeling of this dataset is still ongoing, expected final size 5000.

natively provided as 5000×5000 tiles, but were sliced into 625×625 tiles for processing by the network. Only tiles containing positive pixels (i.e., the presence of PV arrays) were retained.

Two datasets utilized openly available labels and PV imagery data from France, as described by Kasmi *et al.*²³ One of these used data from Google Earth (FR-G) with resolution of 10 cm/pixel. The second used imagery from the French National Institute of Geographical and Forestry information (IGN), with a resolution of 20 cm/pixel, designated as FR-I. These datasets were created using a crowdsourced labeling process and were unique in that images containing PV were centered on the PV feature. Both datasets used tiles of 400×400 pixels.

A dataset based on Google Earth imagery from northern Germany is designated DE-G. It was first described in a previous study by the authors. The native tile resolution was 18 cm/pixel, and tiles were 639×640 pixels. Labeling was conducted manually by visual inspection using the *labelme* software package. ²⁴

The sixth dataset consists of 2018 orthoimagery from New York City (specifically Queens) in the United States (designated NY-Q). Data are obtained from the New York GIS Clearinghouse. The native data consist of 5000×5000 tiles with a resolution of 15 cm/pixel. As with the California datasets, the tiles were sliced to a size of 625×625 prior to processing. Labeling of this dataset was conducted by manual inspection of images and construction of polygons around the PV installations using $labelme^{24}$ and is still ongoing. We hope to make it openly available when complete. The results in this study are based on an initial sampling of around 1000 positive tiles from the in-progress labeling.

In order to study the generalizability across datasets, we worked with a fixed dataset size of 1000 tiles, roughly corresponding to the number of images in datasets with the least number of positive tiles available (CA-F, DE-G, and NY-Q). Holding the number of images fixed at 1000, while representing a relatively small amount of training data, allows us to compare across combinations of these datasets on a fixed quantity of training data. Tiles were chosen randomly from each dataset, and a portion of the results were repeated for two random seeds to ensure no issues with statistical representation. The 1000 tile datasets were split for training, validation, and test sets with a 72%, 8%, and 20% split, respectively. We held the images designated to each category to be fixed for all training and evaluation combinations, which ensured that all models were tested on the same data.

We conducted a manual subjective inspection of the 1000 tiles used for each dataset in order to provide some representative description of their context.¹⁷ We manually counted images that fit into five

TABLE III. Contextual differences by dataset (approximate). 17

Dataset	Large/Flat	Open spaces	Ag.	Water	Util. PV	# Bldg/tile
CA-F	70	140	40	10	0	20-40
CA-S	70	80	10	40	0	20-40
FR-G	10	20	0	0	0	2-5
FR-I	20	90	20	0	0	5-10
DE-G	60	80	10	10	10	10-20
NY-Q	130	10	0	10	0	10-20

bins based on their characteristics: large structures/flat roofs (usually commercial buildings), large open spaces (making up 50% of the image), patterned or row-based agricultural, bodies of water, and utility scale PV. Images not containing one of these features were primarily residential housing. Counts, rounded to the nearest 10, of these images are listed in Table III. For the residential imagery, we also include a rough count of the number of structures that were observed in a typical tile to give an indication of the building density.

These observations are inherently qualitative, but they serve to help describe contextual differences between the datasets. The predominance of residential dwellings was common across all datasets. NY-Q was the most urban of the datasets, with the smallest number of open spaces and the largest number of flat-roofed structures (which were often commercial-scale buildings). NY-Q's urban character was also qualitatively indicated by fewer observable trees within its residential areas as compared to the other datasets. CA-F had the highest incidence of open areas and uniquely contained a significant number of tiles that appeared to indicate agricultural activity in the form of rowor pattern-based vegetative activity. As previously mentioned, the FR-G and FR-I datasets both uniquely centered the images on positively identified PV systems,²³ which along with the resolution and tile size differences explains the difference in building count. This may reduce the probability of PV systems potentially spanning a tile boundary for the FR-G and FR-I sets.16

D. Models trained using the datasets

In order to assess the generalizability of neural network models, an exhaustive characterization of models trained utilizing the six data sources was performed. To establish baseline performance, we first trained six dataset-specific models (one corresponding to each dataset) using the sets of 800 training and validation images taken only from a single dataset. Each of these six models were evaluated against the 200 images making up the test data associated with each of the six datasets, providing results that showed how well each custom trained model generalized outside of its training data.

In addition to the six original datasets, training was also performed using combinations of training data from multiple datasets. Combination datasets always maintained the total size of 800 tiles for training and validation. These tiles were pulled from the previously identified training subsets associated with each dataset. Models trained on these combination datasets were used to assess how incorporating more diverse data influenced the performance of a model. All possible combinations of the datasets were considered, including composite training datasets made by selecting from 2, 3, 4, 5, and all 6 datasets. All combination datasets used equal numbers of tiles from their

constituent components to the extent possible, with any tiles required to reach 800 selected from the final dataset. For example, a dataset made up of CA-F, CA-S, and FR-G would be composed of 266 images from CA-F, 266 images from CA-S, and 268 images from FR-G, totaling 800. The individual tiles used were chosen randomly from among the training and validation tiles belonging to that dataset. When considering all possible combinations, a total of 57 additional models were trained. Each was evaluated individually against the test data associated with each dataset.

Finally, we conducted tests that show performance results from including small fractions of training data from the same data source as the test data in the training set. These evaluations were conducted only for models using test data for the NY-Q dataset as the target. For three of the datasets (CA-F, CA-S, and FR-I), we trained models that replaced a fraction of the training data with varying levels of data from NY-Q (1%, 2%, 3%, 4%, 5%, 10%, 20%, 30%, 40%, and 50%). As with the other conditions evaluated, these models were all trained on a fixed number of tiles (800 total for training and validation). In conjunction with the combination dataset that includes for example both CA-F and NY-Q data (which represents 50% data from NY-Q), these allow us to determine exactly how small amounts of data from a target test set can improve the performance of a model.

IV. RESULTS AND DISCUSSION

A. Models trained on a single dataset

First, we describe results for the baseline of models trained on a single dataset. The results for the IoU are given in Table IV. The results of precision and recall for the models are presented in Tables V and VI, respectively. Averages shown in these tables exclude tests on the data corresponding to a model's training data, in order to show the overall generalized performance without being skewed by differences in the absolute predictability of a set of test data.

We can make some inferences about the model performance based on the conjunction between these metrics. For example, when FR-I predicts on the FR-G dataset, it is often correct but very selective. It has a high precision (95%) indicating that it is usually correct when making predictions, by a low recall (36%) indicating that it does not

TABLE IV. IoU values by dataset.¹⁷ Train dataset in rows. Test dataset in columns. Averages exclude the diagonal to highlight the results for unseen data.

	CA-F	\mathbf{CA} - \mathbf{S}	FR-G	FR-I	DE-G	NY-Q	\mathbf{Avg}
CA-F	0.71	0.35	0.11	0.36	0.06	0.16	0.21
CA-S	0.55	0.61	0.11	0.22	0.17	0.19	0.25
FR-G	0.03	0.00	0.81	0.45	0.13	0.26	0.17
FR-I	0.13	0.19	0.35	0.69	0.31	0.56	0.31
$\mathbf{DE}\text{-}\mathbf{G}$	0.18	0.29	0.11	0.29	0.63	0.44	0.26
NY-Q	0.07	0.22	0.15	0.47	0.40	0.81	0.26
\mathbf{Avg}	0.19	0.21	0.17	0.36	0.21	0.32	
FR-I DE-G NY-Q	0.13 0.18 0.07	0.19 0.29 0.22	0.35 0.11 0.15	0.69 0.29 0.47	0.31 0.63 0.40	0.56 0.44 0.81	0.31 0.26

TABLE V. Precision values by dataset.¹⁷ Train dataset in rows. Test dataset in columns. Averages exclude the diagonal to highlight the results for unseen data.

	CA-F	CA-S	FR-G	FR-I	DE-G	NY-Q	\mathbf{Avg}
CA-F	0.87	0.46	0.36	0.48	0.07	0.25	0.33
CA-S	0.82	0.79	0.51	0.31	0.22	0.24	0.42
FR-G	0.10	0.03	0.91	0.76	0.41	0.52	0.36
FR-I	0.63	0.64	0.95	0.79	0.67	0.77	0.73
DE-G	0.70	0.65	0.83	0.91	0.77	0.82	0.78
NY-Q	0.59	0.66	0.90	0.87	0.75	0.90	0.75
\mathbf{Avg}	0.57	0.49	0.71	0.67	0.42	0.52	

TABLE VI. Recall values by dataset.¹⁷ Train dataset in rows. Test dataset in columns. Averages exclude the diagonal to highlight the results for unseen data.

	CA-F	CA-S	FR-G	FR-I	DE-G	NY-Q	\mathbf{Avg}
CA-F	0.79	0.59	0.15	0.58	0.59	0.35	0.45
CA-S	0.62	0.72	0.13	0.47	0.59	0.37	0.44
FR-G	0.06	0.01	0.88	0.52	0.15	0.29	0.20
FR-I	0.15	0.23	0.36	0.84	0.37	0.67	0.35
$\mathbf{DE}\text{-}\mathbf{G}$	0.19	0.33	0.11	0.30	0.79	0.48	0.28
NY-Q	0.07	0.24	0.15	0.50	0.47	0.89	0.28
\mathbf{Avg}	0.22	0.28	0.18	0.47	0.43	0.43	

identify a large share of the ground truth pixels. An example of the converse is available for CA-F predicting DE-G, where performance is achieved by erroneous overprediction of the incidence of PV. In this case, modest recall is observed (59%), which means that many ground truth pixels are identified, but at the cost of predicting a significant number of false positives, indicated by the 7% score in recall.

It is unsurprising to observe that models generally performed best when predicting their corresponding test data, where the average IoU score across all models was 0.71. From the tables above, we can also observe that with a few exceptions in the precision metric, generalization was relatively poor; a model trained on a given dataset was the best performer on test data for that dataset. A few examples of moderate skill at generalization was observed. The best examples occurred with FR-I predicting NY-Q test data and the model trained on CA-S predicting CA-F. In the case of California, this may arise somewhat from the shared data source, but it is likely that confounding factors



FIG. 1. Example of discretization of the individual array modules in an FR-G image when predicted by the NY-Q trained model.

are at play, because no performance boost to CA-F was seen when predicting CA-S.

The FR-I trained model had the most generalizable performance to other test sets with an average IoU of 0.31. The FR-G trained model showed the worst individual example of generalization, especially on CA-F and CA-S where it showed virtually no predictive skill. FR-G compared to the California sets had the greatest discrepancy in resolution, which may suggest that models do not adapt well to lower resolution imagery (i.e., lower zoom levels). We can also consider the difficulty of the task for an arbitrary model but averaging across models for a given test dataset. The test sets with the highest average IoU scores across all models were FR-I (IoU = 0.36) and NY-Q (IoU = 0.32), showing greatest ease for prediction by a general model. For all these cases, it is important to note that none of these examples of generalization achieved the performance of the model trained on the corresponding dataset.

The difficulty of predicting across multiple resolutions may also been inferred via the fact that the FR-G test data were most difficult to predict by other models, with an average IoU of 0.17. Investigating the precision and recall shows that models were usually correct when predicting positive values, but were hesitant to do so, as indicated by the low recall. When observing the predictions on a detailed level, it is possible to notice that some models tended to discretize the individual panels on FR-G, indicating that they apparently interpreted the frames of the modules as gaps in the array, which was not true for FR-G's own predictions. This may be an indicator that when training models at lower zoom levels (for which the frames are generally not resolvable), a degree of confusion arises in the predictions when applied at higher zoom, because additional physical features can be resolved. An example of this effect is shown in Fig. 1. In this case, the frames of the panels (which were not always visible in the NY-Q images) resolve with a width of multiple pixels in the FR-G images. We note that this occurred despite the zoom augmentation in the training methodology.

B. Models trained on combined data

Since no individual models generalized well across other datasets, we investigated how training models on data from multiple sources affects their performance at predictions. We will refer to these as models trained on combination datasets. Tests were made considering two

modalities. First, we trained and tested combination models on data they had seen, that is, using a fraction of training data corresponding to the target test dataset, paired with images from additional data sources. This investigation answers the question "Compared to training on exclusively the target data source, can exposure to more diverse data improve the performance of a model?" Second, we looked at combination models tested on completely unseen data, which is to say that no data from the test data's data source were used in training. In this case, a three data source combination trying to predict NY-Q would never contain training data from NY-Q (e.g., could be trained on CA-F, FR-I, and DE-G). This framing attempts to answer the question, "Does exposure to more diverse data improve the generalizability of a model for data from an unknown source?" In either case, we tested all possible combinations of training data sources that met the modality criteria. As stated previously, for combination models, the total number of 800 training and validation images was maintained, and splits between the training data sources were as even as possible. The results for both seen and unseen combination tests are discussed in the following.

1. Combination models for predicting data from a seen data source

Combination models for predicting seen data were trained using training data from the target test data source combined with data from an additional *n* number of data sources. That is to say, these combination models always contained some data from the same data source as the corresponding test dataset. So a three data source combination model attempting to predict NY-Q test data might be trained on CA-F, FR-G, and NY-Q data. Combinations were trained making use of data from 2, 3, 4, 5, or 6 total datasets (corresponding to 50%, 67%, 75%, 80%, and 83% training data from sources other than the test data source, respectively). The results on IoU score, precision, and recall as a function of number of data sources are shown in Figs. 2–4. The results shown are normalized to performance of a model trained solely on data from the corresponding test data source (i.e., from Table IV) to better indicate trends when accounting for performance offsets. A tabulated form of Fig. 2 is shown for two source combinations only in Table VII.

The results show that adding additional diverse data to a model on average worsens its IoU score performance as compared to models

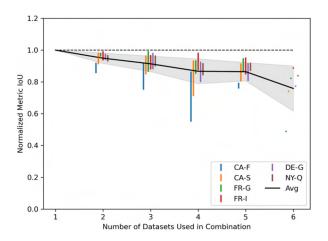


FIG. 2. IoU score performance on combination models tested on seen data by test dataset. Horizontal axis shows the number of individual datasets used in making up the training data (always including the test data in this case). Markers indicate range of individual combination model performance. Line shows average performance at this combination size, while area shows first standard deviation range across all models.

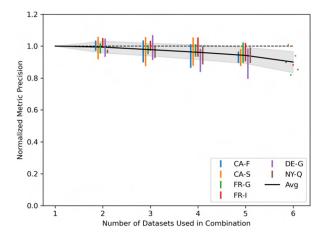


FIG. 3. Precision performance on combination models tested on seen data by test dataset. Horizontal axis shows the number of individual datasets used in making up the training data (always including the test data in this case). Markers indicate range of individual combination model performance. Line shows average performance at this combination size, while area shows first standard deviation range across all models.

trained specifically on a given data source. This performance degradation is greater as more diverse data are included in the training set (i.e., less of the target data are used). This trend is universal across all test data sources, though some cases (e.g., CA-F) experience a greater degree of performance loss. Simply put, this result indicates that diversifying the fixed-size training dataset never increased its performance over a model trained exclusively on the target data source, and thus simply diversifying the training data could not be recommended as a strategy for creating a more generalizable model. While the data do not allow a definitive conclusion to be drawn for this phenomenon, we hypothesize that it occurs due to displacement of the target data in the

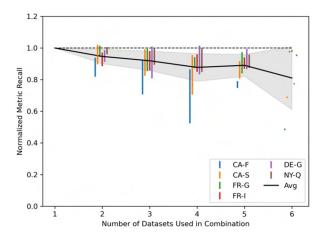


FIG. 4. Recall score performance on combination models tested on seen data by test dataset. Horizontal axis shows the number of individual datasets used in making up the training data (always including the test data in this case). Markers indicate the range of individual combination model performance. Line shows average performance at this combination size, while area shows first standard deviation range across all models.

TABLE VII. Two set seen combination normalized IoU performance by test dataset.

	CA-F	CA-S	FR-G	FR-I	DE-G	NY-Q
CA-F & CA-S	0.92	0.95				
CA-F & FR-G	0.86		0.99			
CA-F & FR-I	0.89			0.99		
CA-F & DE-G	0.89				0.96	
CA-F & NY-Q	0.92					0.97
CA-S & FR-G		0.92	0.96			
CA-S & FR-I		0.93		0.96		
CA-S & DE-G		0.98			0.96	
CA-S & NY-Q		0.97				0.97
FR-G & FR-I			0.98	0.94		
FR-G & DE-G			0.96		0.93	
FR-G & NY-Q			0.98			0.93
FR-I & DE-G				0.99	0.98	
FR-I & NY-Q				0.93		0.97
DE-G & NY-Q					0.95	0.95

training dataset (i.e., a combination of two data sources contains only half as many images from a given data source as each would individually). That is, the raw number of images from the target data appears to be more important than the diversity of the training data.

The results may be investigated in more detail by considering the effects on precision and recall. In the case of precision, we observed that introducing more diverse data may for some cases lead to an increase in the precision of models (i.e., make them less likely to make false positive predictions), by up to 7% relative to the baseline for the highest precision models, but did not reach the level of statistical significance based on the repeatability described previously. These are indicated by bars with values above 1.0 in Fig. 3. For cases where the

precision was negatively impacted, performance reductions did not exceed more than 20% from the baseline. In the case of recall, very slight improvements in performance were observed when training on diverse data in a limited number of cases, but the potential negative impacts were quite significant (up to 40% reduction in performance). As in the case of IoU, negative impacts were more likely when including data from a greater number of different data sources. So we could conclude that creating combination datasets on seen data may make models more precise in predictions, but any benefits are outweighed by reductions in the recall leading to an overall degradation of performance.

In sum, these results indicate that as compared to custom-training for a model to make predictions on a given data source, adding a more diverse set of data does not improve the overall model performance. Conversely, the IoU score performance was always reduced as compared to a baseline trained exclusively on data from the test data source. Reductions in performance seemed to be dominated by loss of recall, as a few cases actually exhibited increases in precision resulting from increased diversity in the training data. These models would be less likely to predict false positives, but always at the cost of predicting an increased number of false negatives. However, because there was no discernible pattern to the likelihood of improving precision, it would be difficult to deliberately produce a model with these characteristics on an *a priori* basis. These results indicate that to get the best performing model on a given test dataset, one should favor training on as much data from that data source as possible.

2. Performance of combination models on unseen test data

We also tested a suite of combination models whose constituents never included data from the test data's source. These models were trained using 2, 3, 4, or 5 data sources, representing all combinations that did not include the test set. Data for a single unseen source correspond to those described in Sec. IV A, but are included with these results as a baseline. Combination results for six data sources necessarily include the test data source and thus do not fully meet the unseen criteria, but those results are also included here for comparison purpose. The results are shown for IoU in Fig. 5, for precision in Fig. 6 and recall in Fig. 7. A tabulated version of Fig. 5 for two source combinations only is given in Table VIII (note that this is essentially the complementary values to Table VIII).

The results on IoU in Fig. 5 show that no combination models performed nearly as well as the custom trained models; however, on average, performance in all three metrics did improve by diversifying the training data. A much higher degree of vertical spread was observed, indicating a much greater degree of variability in the performance of individual combinations. Inspecting results for the other metrics, we see a similar result to that for the seen models, in that it was common for combination models to exceed the precision of custom-trained models, and in this case, did so at statistically significant levels in the extreme cases. This increase in precision is never accompanied by improvement in the IoU score as compared to the custom trained models. We also may observe that the case of testing on FR-G data appears to be an outlier, for which no combination of data resulted in substantial performance improvements.

These results indicate that on average, including more diverse training data tends to improve the performance of models at

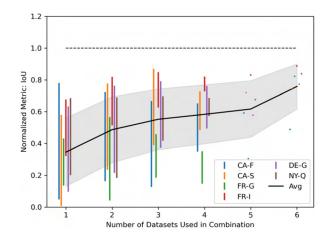


FIG. 5. IoU score performance on combination models tested on never seen data by test dataset. Horizontal axis shows the number of individual datasets used in making up the training data. Note that "6" case always includes seen data. Markers indicate range of individual combination model performance. Line shows average performance at this combination size, while area shows first standard deviation range across all models.

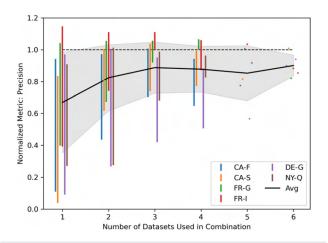


FIG. 6. Precision performance on combination models tested on never seen data by test dataset. Horizontal axis shows the number of individual datasets used in making up the training data. Note that "6" case always includes seen data. Markers indicate range of individual combination model performance. Line shows average performance at this combination size, while area shows first standard deviation range across all models.

identifying PV arrays. However, when considering the best individually performing model for any given test set, no universal pattern emerged. That is, some test sets experienced highest IoU score performance in a model using 2 or 3 datasets, while one case's best performing model used only a single dataset. Thus, utilizing data from as many datasets as possible increases the probability of achieving moderately accurate performance from a generalized model, but might not lead to the best model performance overall. The best way to ensure high performance is to include data from the target data source model in the training data, as seen by comparing the absolute values of IoU score between Figs. 2 and 5.

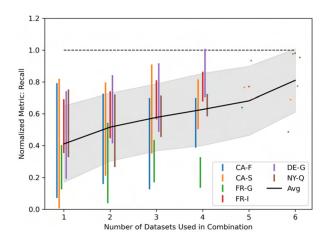


FIG. 7. Recall score performance on combination models tested on never seen data by test dataset. Horizontal axis shows the number of individual datasets used in making up the training data. Note that "6" case always includes seen data. Markers indicate the range of individual combination model performance. Line shows average performance at this combination size, while area shows first standard deviation range across all models.

TABLE VIII. Two set seen combination normalized IoU performance by test dataset.

	CA-F	CA-S	FR-G	FR-I	DE-G	NY-Q
CA-F & CA-S			0.13	0.53	0.21	0.18
CA-F & FR-G		0.69		0.82	0.46	0.38
CA-F & FR-I		0.70	0.35		0.41	0.63
CA-F & DE-G		0.74	0.06	0.65		0.53
CA-F & NY-Q		0.78	0.19	0.79	0.76	
CA-S & FR-G	0.63			0.66	0.44	0.50
CA-S & FR-I	0.68		0.31		0.55	0.58
CA-S & DE-G	0.55		0.04	0.51		0.64
CA-S & NY-Q	0.72		0.30	0.77	0.74	
FR-G & FR-I	0.16	0.24			0.43	0.63
FR-G & DE-G	0.31	0.45		0.66		0.53
FR-G & NY-Q	0.17	0.41		0.74	0.61	
FR-I & DE-G	0.41	0.49	0.57			0.69
FR-I & NY-Q	0.16	0.41	0.26		0.62	
DE-G & NY-Q	0.31	0.45	0.24	0.65	•••	• • •

It is worth emphasizing that Fig. 5 clearly shows that no combination model performed better (or even nearly as well) on IoU score as a model trained on data from the target data source. This suggests that seeking to produce truly generalized models may not yield the most satisfactory results regardless of the care taken in the selection of their makeup for training.

C. Image-wise performance

To better understand some of the performance of the models, we visualized the individual images with the best- and worst-IoU score on an image-wise basis, shown in Figs. 8 and 9, respectively. In these cases,

best and worst IoU scores were determined by averaging across the performance from the models trained on a single dataset.

While the representations of best images are inherently anecdotal, a few comments can be made about their shared characteristics. In the images representing the best average predictions, PV systems tended to be large and rectilinear. In the case of NY-Q test data in particular, all five images show large commercial rooftop systems. CA-F is the possible outlier to these observations, because four of the five best performing images appear to show small rooftop arrays. Additionally, the solar arrays in these images appear to be similarly colored. To attempt to quantify the preference for identifying large systems, we computed the Pearson correlation coefficient between the number of positive pixels in the labeled image (related to the overall array size) and the average IoU score for the image across all unseen test sets. All datasets except FR-G showed a small, albeit statistically significant image-wise relationship between the number of pixels and IoU score (p < 0.005), with the level of association varying from $\rho = 0.21 - 0.49$. This indicates that most of these models do tend to perform better on larger systems. The lack of a relationship in the FR-G data may result from the relative scarcity of larger systems in that dataset (as indicated in

The worst performing images were predominantly of residential housing. Again, despite the anecdotal nature of these data, a few observations can be made. Many of these images across all datasets contain examples where there is very little contrast between the roof and the array. In some cases from FR-G, we observe instances where the camera sensor seems to have saturated due to solar reflection, and these were also difficult to predict. The difficult to predict images from NY-Q are all examples of very small segments that are cropped by the edges of the frame. One of the poorly performing images from CA-F contains examples of agricultural rows (present in several other images from that dataset as well). It was common for models not trained on CA-F data to predict false positives on the regularly spaced rows in this and similar images, which we hypothesize is due to their regular patterned structure that may resemble the rows of large-scale PV installations. An example is shown in Fig. 10.

D. How much target data are needed for good performance?

Given that no generalized model performed as well as the custom trained models, we investigated what quantity of training data corresponding to the test set could result in improvements to performance. Given the large number of possible combinations, these investigations were conducted only for test data corresponding to the NY-Q dataset. Models were trained by combining each of the datasets with a fraction of data from NY-Q. Fractions of 1%, 2%, 3%, 4%, 5%, 10%, 20%, 30%, 40%, and 50% were investigated. The results for testing on NY-Q data are shown in Fig. 11. As evident, including data from the target data source quickly improves the performance of the model. While there is a degree of subjectivity to interpretation, diminishing returns are reached around 20% of the NY-Q data.

We also looked at the extent to which incorporating the small quantities of NY-Q data affected their ability to predict their corresponding test data. Those results are depicted in Fig. 12. Overall, models remain at or above about 90% of their baseline IoU value. The degree of impact varies by data source, with CA-F being most affected. A few models obtain IoU score performance that exceeds the baseline



FIG. 8. Five images for each test set with best averaged IoU score across all models trained on a single dataset.

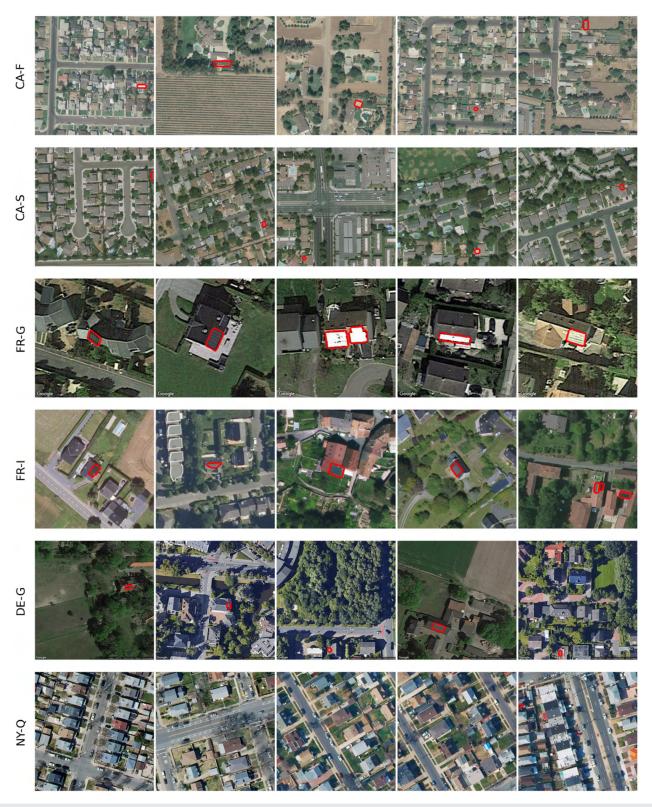


FIG. 9. Five images for each test set with worst averaged IoU score across all models trained on a single dataset.

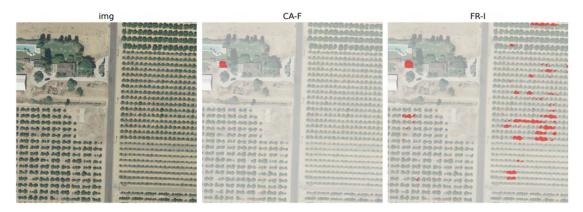


FIG. 10. Example of false predictions of PV by the FR-I trained model on the rows of agricultural activity seen in CA-F.

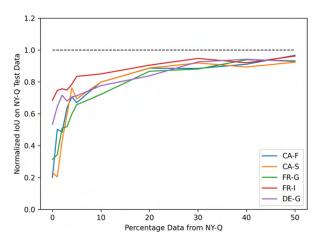


FIG. 11. IoU score results on NY-Q for inclusion of incremental amounts of NY-Q data to improve performance. Colored label corresponds to the data source paired with NY-Q in the combination.

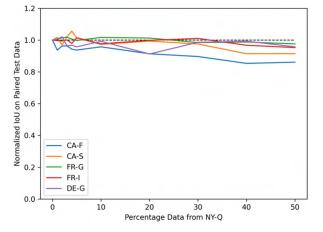


FIG. 12. IoU score results on corresponding test data for the inclusion of incremental amounts of NY-Q data to improve performance. Colored label corresponds to the data source paired with NY-Q in the combination.

with small amounts of NY-Q data. While this does suggest the possibility of introducing very small amounts of diverse data to improve the performance of a model, it is important to note that these increases are very small and none reached the level of statistical significance relative to average IoU standard deviation of 0.04 described in Sec. III A. In any event, the improvements seen are not universally beneficial, nor does introducing the data produce a consistent trend that could be used to try to produce a more effective model.

Coupled with the previous results on combination models, these data suggest that there is no reliable method to produce a generalizable neural network model for segmentation of PV within images simply by diversification of the training data. Rather, the best method for producing reliable neural network models for this task is inclusion of some labeled data from the target data source in training. Fractions of at least 20% produced models that reached performance around 90% of the normalized level produced with full labeling of training data from the target, regardless of the initial quality of the model without NY-Q data. The choice of training effort ultimately requires a balancing decision between desired model quality and labeling effort.

V. CONCLUSION

The use of trained neural networks remains an attractive option for remote identification of PV systems for a variety of research and decision making tasks. We conducted a comprehensive study of training a ResNet-based neural network for this purpose and whether the possibility exists to generalize such a model based on diversification of the training data. The experimental design used a fixed size and architecture to control for the impact of those effects on the results. Our study may aid researchers in planning training approaches for the development of models for identification of PV from aerial images, especially when considering the breadth of data sources currently available.

We obtained a negative result for the ability to improve performance of a custom trained model by diversifying its training data, while using a fixed total number of training images. We did not observe any combination models where incorporating training data from additional sources increased a model's ability to predict the location of PV in images relative to a model trained exclusively on the target data. We did observe very slight (1%–2%) increases in the IoU score corresponding to introduction of less than 10% NY-Q data that

were not statistically significant relative to the repeatability of the IoU metric. This implies that when preparing to utilize a model with new data sources, achieving the best performance will require some degree of labeling of the new source, and researchers should plan to make balanced decisions regarding desired model performance against the invested labeling effort.

Our results on predicting unseen data showed agreement with previous studies that were based on fewer data sources. When investigating models that are tested on completely unseen data, it was not possible to create truly generalized models, regardless of the combinations of training data used at the fixed size of 1000 training images. While incorporating data from many data sources into training data had the potential to yield a more general model on average, these models did not approach the performance of models trained specifically on data from the target data source. When predicting unseen data, the average model trained on maximally diverse training data produced IoU score results around 60% as effective as models custom trained on the test data's source. As before, this result indicates to researchers planning to apply models for PV identification purpose on a new data source that it is necessary to include some labeled data on the new source to achieve successful models.

Achieving the best performance therefore necessitates the incorporation of some degree of labeled data from the target for the purpose of training. We investigated the degree to which small amounts of labeled data could improve performance, with the intention of allowing investigators to minimize the labeling effort. Our investigation indicates that the greatest gains come during the addition of up to 20% data from the target dataset, after which the magnitude of returns diminishes. Future work may consider more advanced methodologies for training to reduce the labeling effort required to gain these benefits.

The results of this study are limited by the experimental methodology employed in this study, which utilized a fixed model architecture commonly used by many other investigators and was limited to a fixed training dataset size of 1000 images. Further research may be necessary to conclusively determine whether more sophisticated model architectures could overcome the limitations on generalizability seen here, or whether models trained on a substantially larger dataset would produce more favorable results. However, the results obtained from this study provide insight to researchers who are hoping to apply neural networks for PV identification utilizing close to "off-the-shelf" approaches. When using publicly available datasets, architectures accessible through common open source packages and desktop hardware, researchers should plan for some labeling effort to apply PV identification models to unseen data sources.

We look forward to the opportunities that neural network based PV identification models offer to help answer questions related to growth, access, and affordability of distributed solar generation.

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AUTHOR DECLARATIONS Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Joseph Ranalli: Conceptualization (equal); Investigation (lead); Software (equal); Writing – original draft (lead); Writing – review & editing (equal). Matthias Zech: Conceptualization (equal); Investigation (supporting); Software (equal); Writing – review & editing (equal). Hendrik-Pieter Tetens: Conceptualization (equal); Investigation (supporting); Writing – review & editing (equal).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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