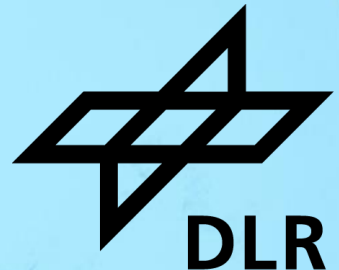
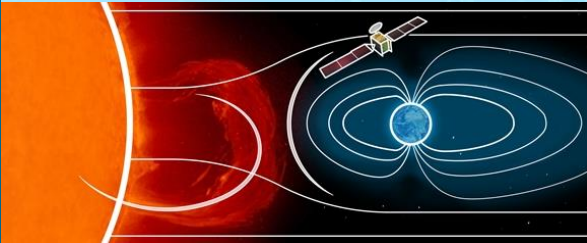


# IONOSPHERIC INDICES FOR CHARACTERIZING IONOSPHERIC PERTURBATIONS AND WARNING USERS OF TRANS-IONOSPHERIC RADIO SYSTEMS

NORBERT JAKOWSKI, M. MAINUL HOQUE, JUAN ANDRÉS CAHUASQUÍ,  
GRZEGORZ NYKIEL

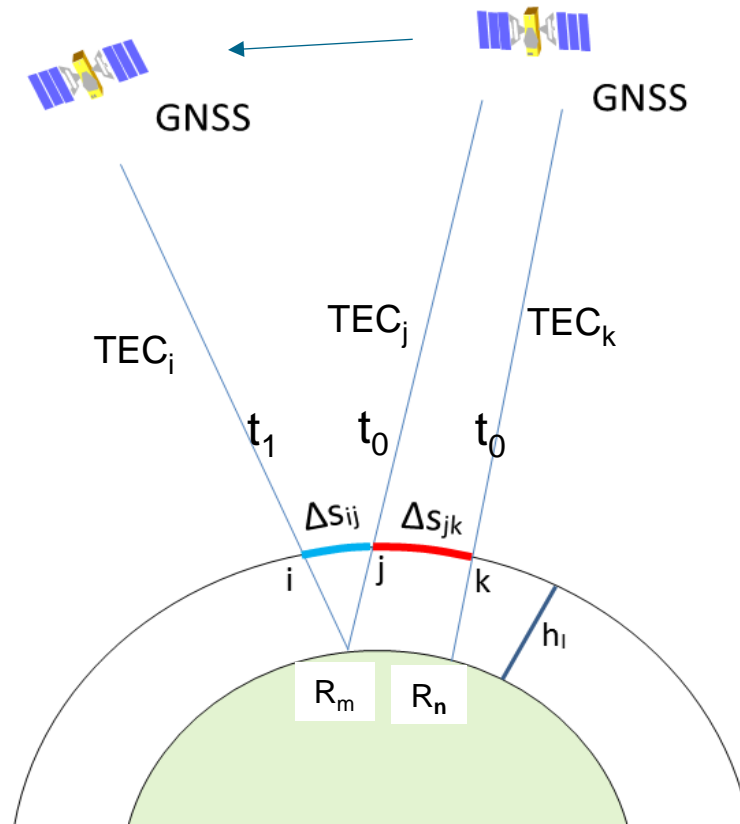
GERMAN AEROSPACE CENTER DLR, NEUSTRELITZ, GERMANY



- Introduction
- Ionospheric index approaches GIX and SIDX
- Use of indices in GNSS positioning
- Discussion of application related scales
- Summary and Conclusions

- Ionospheric research and space based technologies such as telecommunication, navigation and remote sensing require an objective measure of the ionospheric perturbation degree on global scale.
- Developing indices and related scales must consider the following criteria:
  - Objective measure, free from instrumental impact
  - Global data coverage around the clock
  - Characterization of the state of the ionosphere in near real time
  - Robust approach, nevertheless, reliable and sufficiently accurate
  - Easy and fast computation and interpretation
  - Pragmatic scale, accepted by customers
  - Forecast capability
- Indices and related scales require international acceptance, efforts to standardize well accepted approaches (ISWAT group G2B-04 - <https://iswat-cospar.org/G2B-04>)

# Gradient Ionosphere indexX (GIX) and Sudden Ionosphere Disturbance indexX (SIDX)



- Attempt to separate temporal and spatial perturbations by GIX and SIDX
- Index approaches based on GNSS\* data
  - Good data coverage over main application areas
  - High temporal resolution ( $\approx 1$ s) possible
  - Data close to user needs
- Fast computation, low latency of products
- GIX:  $\Delta\text{TEC}/\Delta s$      $\Delta s$ : distance between piercing points at  $t_0$
- SIDX:  $\Delta\text{TEC}/\Delta t$      $\Delta t = t_1 - t_0$  at satellite tracks

GNSS\*: Global Navigation Satellite System

Jakowski, N. and M. M. Hoque (2019), Estimation of spatial gradients and temporal variations of the total electron content using ground based GNSS measurements, Space Weather, doi: 10.1029/2018SW002119

# Sudden Ionosphere Disturbance Index (SIDX)

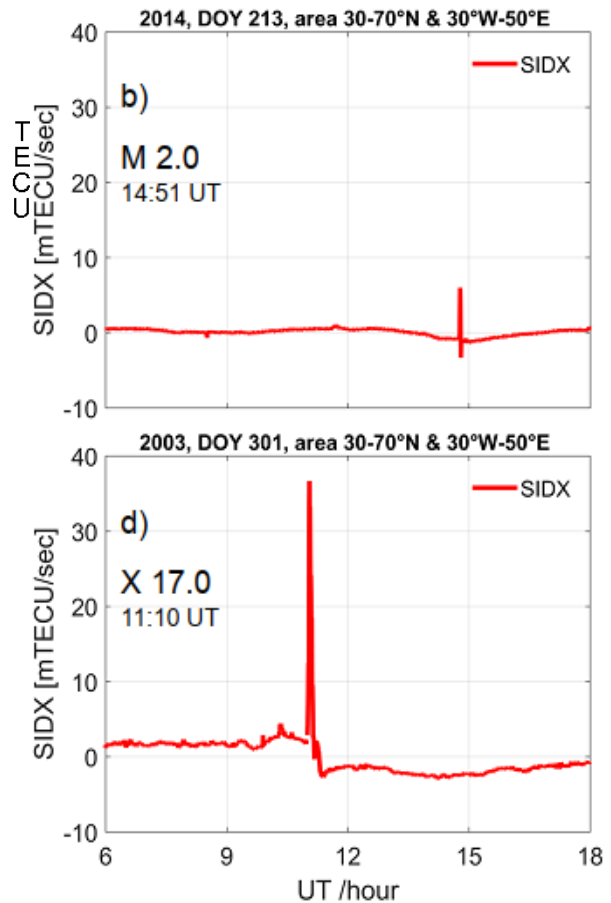
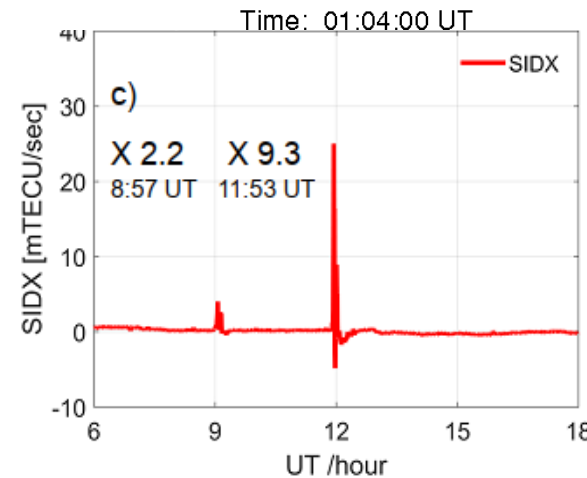
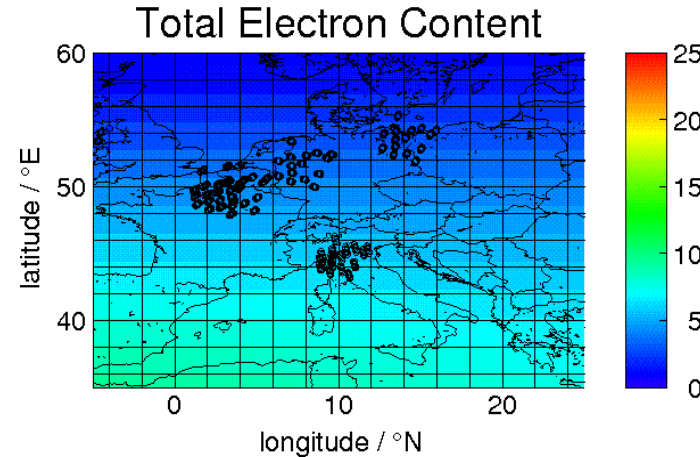
- SIDX - basic approach:  
average rate of TEC rate of change  
at all PPs in a selected area

$$\frac{\partial TEC}{\partial t} = \frac{\Delta STEC}{M \Delta t} - \frac{\partial TEC}{\partial u} v$$

$$\left\langle \frac{\partial TEC}{\partial t} \right\rangle \approx \frac{1}{N} \sum_{i=1}^N \left( \frac{\Delta STEC}{M \Delta t} \right)_i$$

$$SIDX = \left\langle \frac{\partial TEC}{\partial t} \right\rangle$$

$$SIDXS = \sqrt{2 \left( \left\langle \frac{\partial TEC^2}{\partial t} \right\rangle - \left\langle \frac{\partial TEC}{\partial t} \right\rangle^2 \right)}$$





# Sudden Ionosphere Disturbance Index (SIDX)

- SIDX - basic approach:  
average rate of TEC rate of change  
at all PPs in a selected area

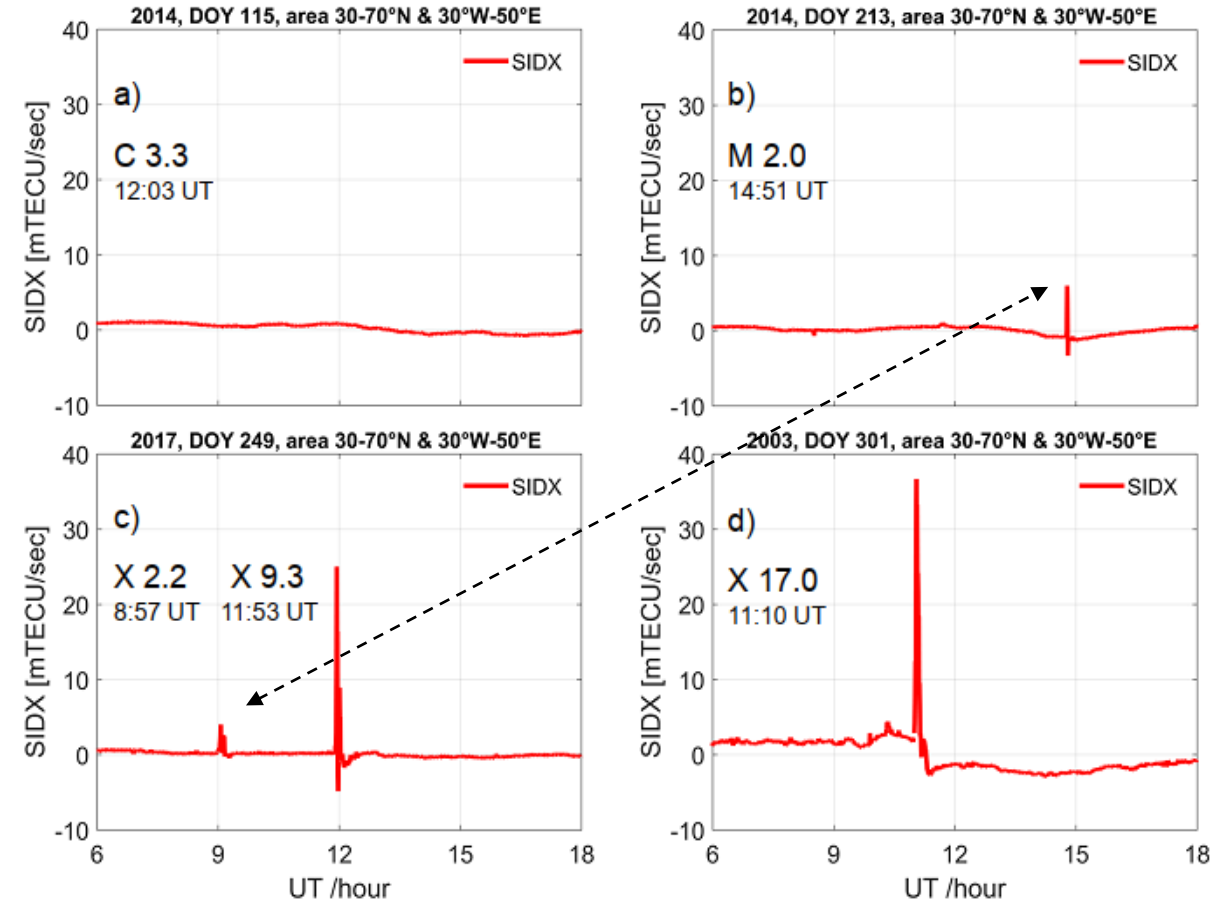
$$\frac{\partial TEC}{\partial t} = \frac{\Delta STEC}{M \Delta t} - \frac{\partial TEC}{\partial u} v$$

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$$SIDX = \left\langle \frac{\partial TEC}{\partial t} \right\rangle$$

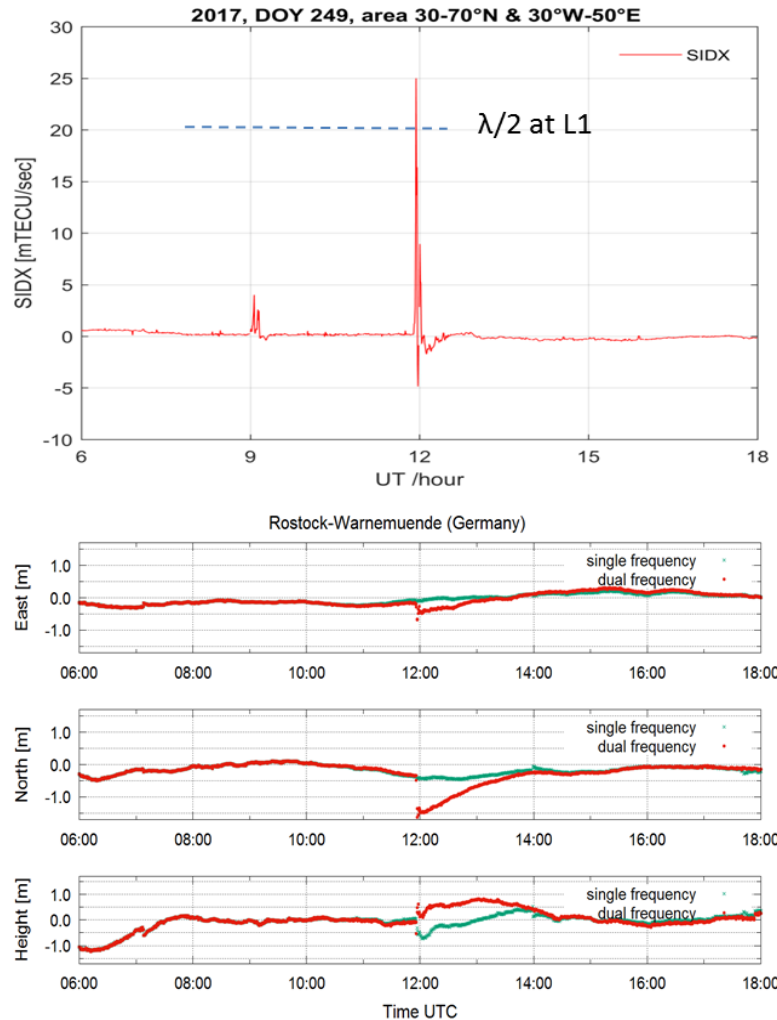
$$SIDXS = \sqrt{2 \left( \left\langle \frac{\partial TEC^2}{\partial t} \right\rangle - \left\langle \frac{\partial TEC}{\partial t} \right\rangle^2 \right)}$$

SIDX response to solar flares may differ from X ray classification due to spectral dependence of ionization



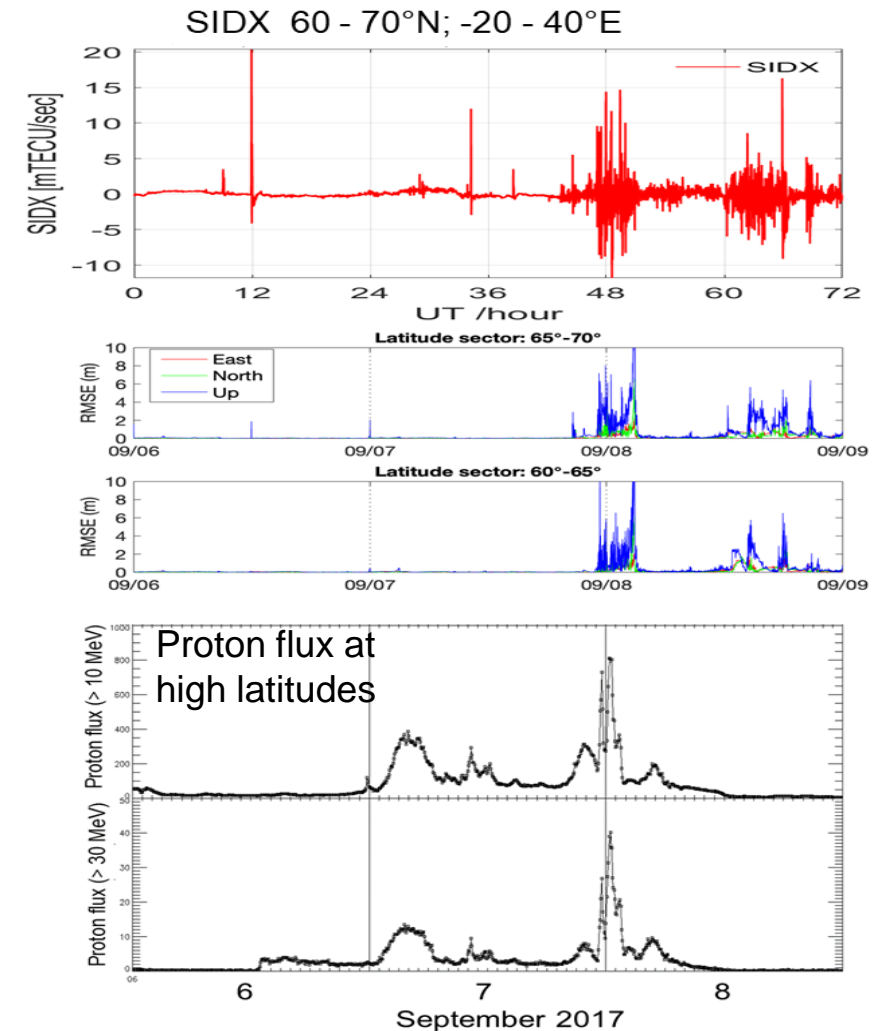
# Application of SIDX in positioning

SIDX Sept 6, 2017 – solar flare impact



- Enhanced SIDX values due to rapid changes of ionospheric ionization correlate with GNSS positioning errors
  - Rapid changes of ionospheric ionization may be caused by solar flares and precipitation of energetic particles
- detectable by SIDX
- Definition of a scale useful for customers needs numerous measurement samples.

SIDX Sept 7, 2017 – particle precipitation



# Spatial perturbation degree by the **Gradient Ionosphere index** **GIX**

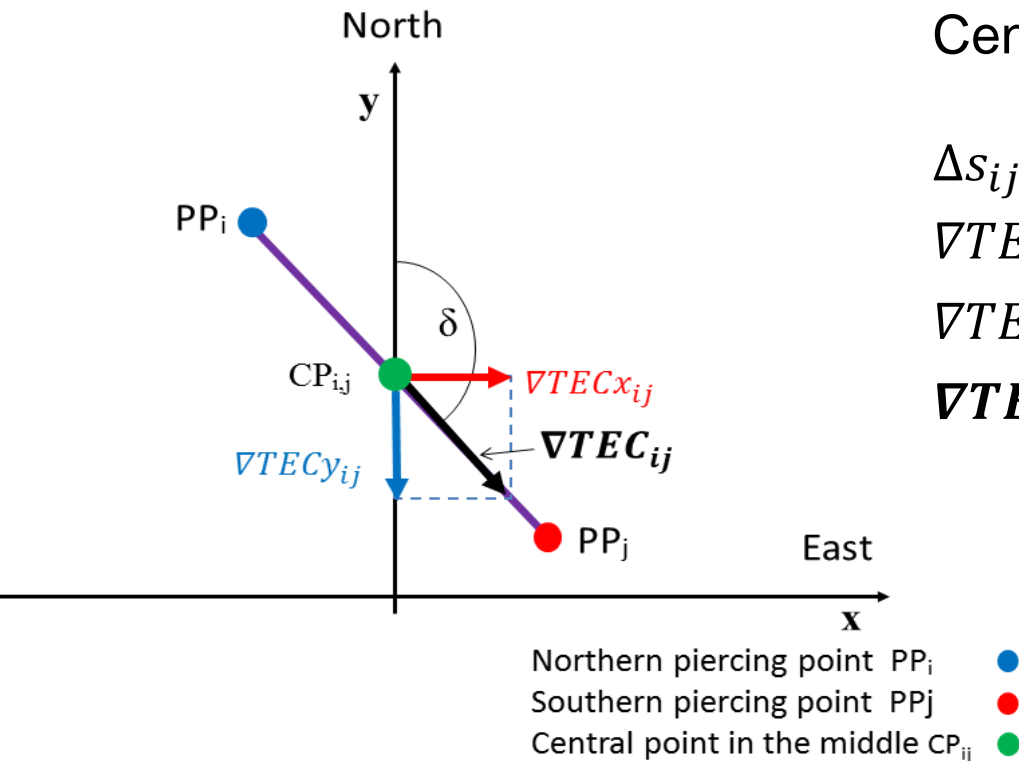
N: number of piercing points  $PP_i$  and  $PP_j$   
Central point  $CP_{ij}$

$\Delta s_{ij}$ : distance between piercing points

$\nabla TEC x_{ij}$ : gradient East direction

$\nabla TEC y_{ij}$ : gradient in North direction

$\nabla TEC_{ij}$ : total gradient between  $PP_i$  and  $PP_j$



Data base:

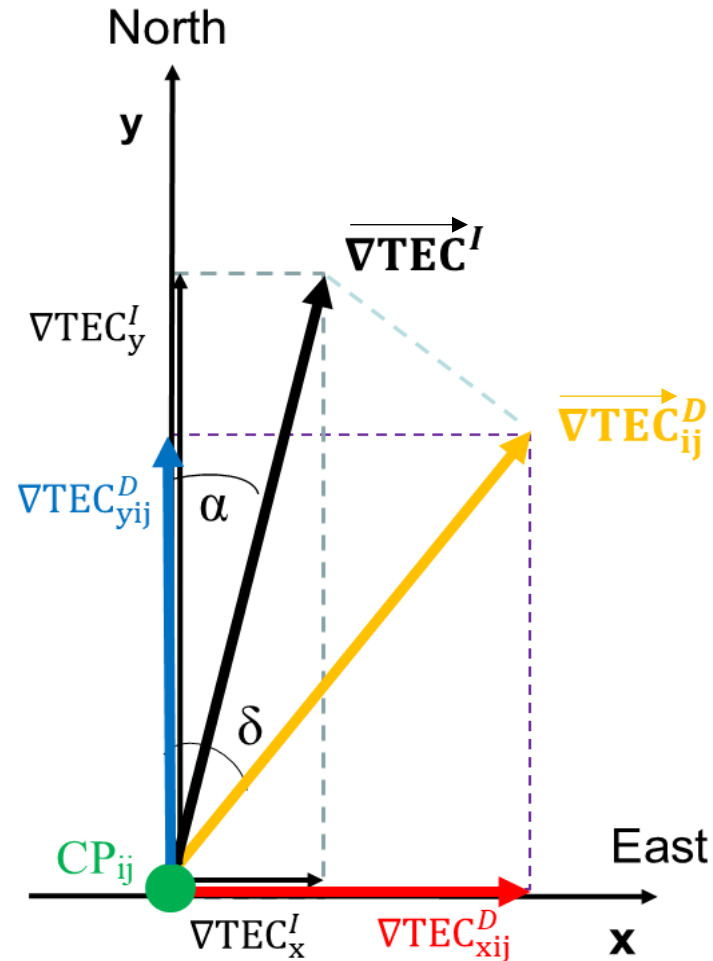
**Vertical TEC data** at N piercing points  $PP_{i,j}$ .

$ND = N(N-1)/2$     maximal number of different PPs  
usable for gradient computation

**Gradient Ionosphere index**



# Gradient Ionosphere Index (GIX) → GIXM + GIXV



Vertical TEC data at N ionospheric piercing points (IPPs)

$N_D \leq N(N-1) / 2$  Number of different IPP links (dipoles)

N: number of piercing points  $PP_i$  and  $PP_j$

$CP_{ij}$  : Central point of dipole, location of the measured gradient vector  $\vec{\nabla TEC}_{ij}^D$

$\Delta s_{ij}$ : distance between piercing points

$$GIXM = \langle \nabla TEC^D \rangle = \frac{1}{N_D} \sum_{k=1}^{N_D} |\nabla TEC_k^D|$$

$\nabla TEC_{ij}^D$ : measured gradient value between  $PP_i$  and  $PP_j$

$\nabla TEC x_{ij}^D$ : measured gradient component in East direction

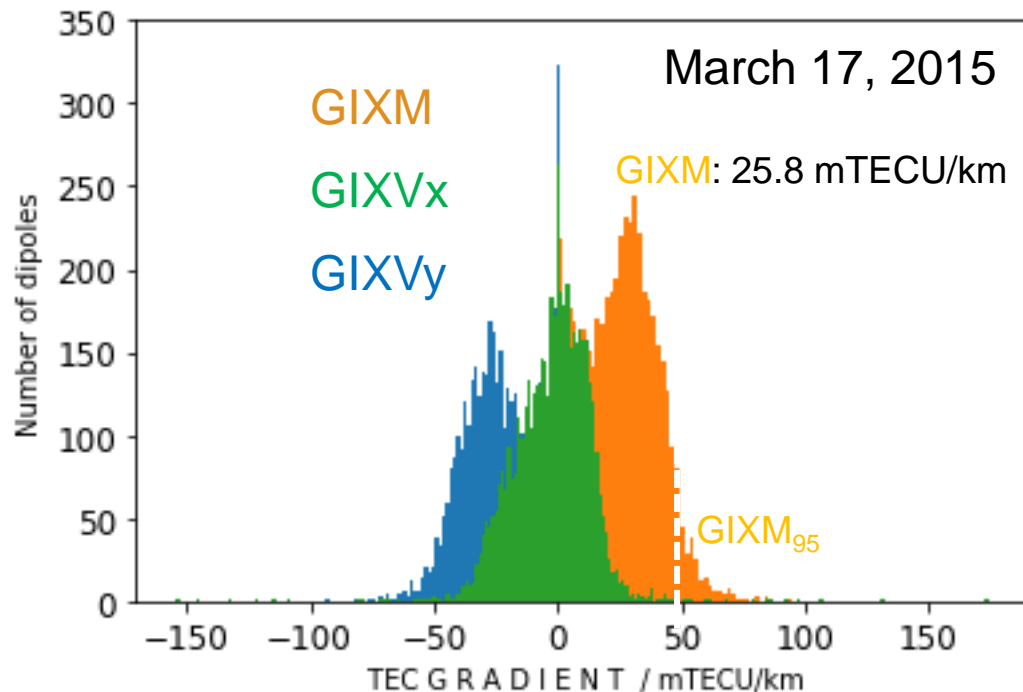
$\nabla TEC y_{ij}^D$ : measured gradient component in North direction

$$GIXV = \langle \nabla TEC^I \rangle = \sqrt{\langle \nabla TEC x^D \rangle^2 + \langle \nabla TEC y^D \rangle^2}$$

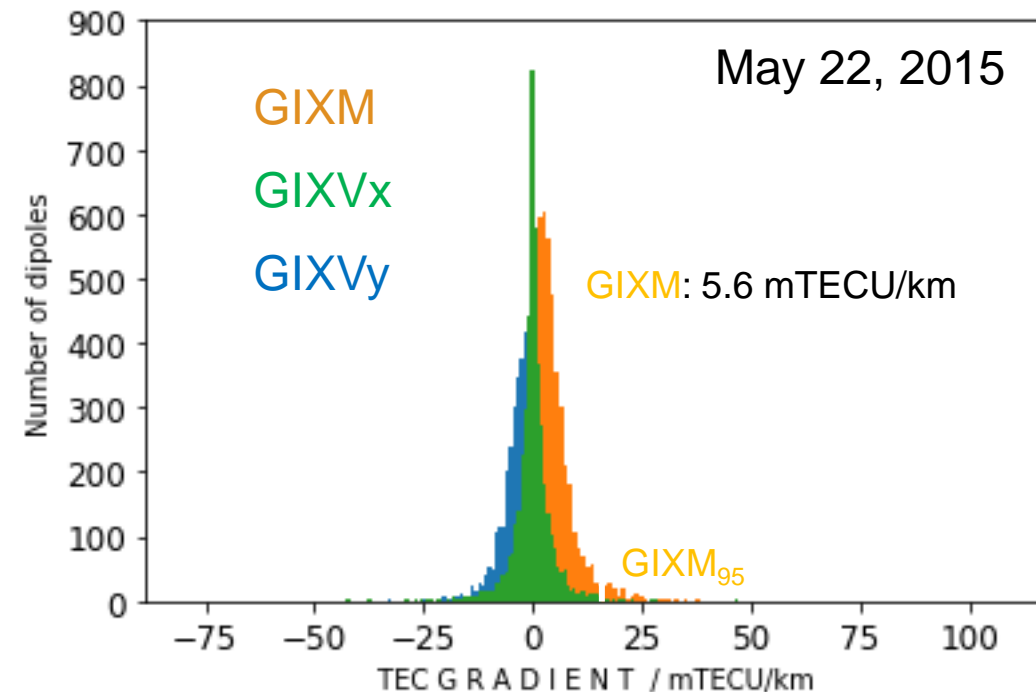
$$\alpha = \text{atan} ( \langle \nabla TEC x^D \rangle / \langle \nabla TEC y^D \rangle )$$

# Distribution functions of GIXVx, GIXVy and GIXM on March 17, 2015 and May 22, 2015 at 18:00 UT

Ionospheric gradient vector: 38.6 mTECU/km  
Azimuth of ionospheric gradient vector: 187.3°



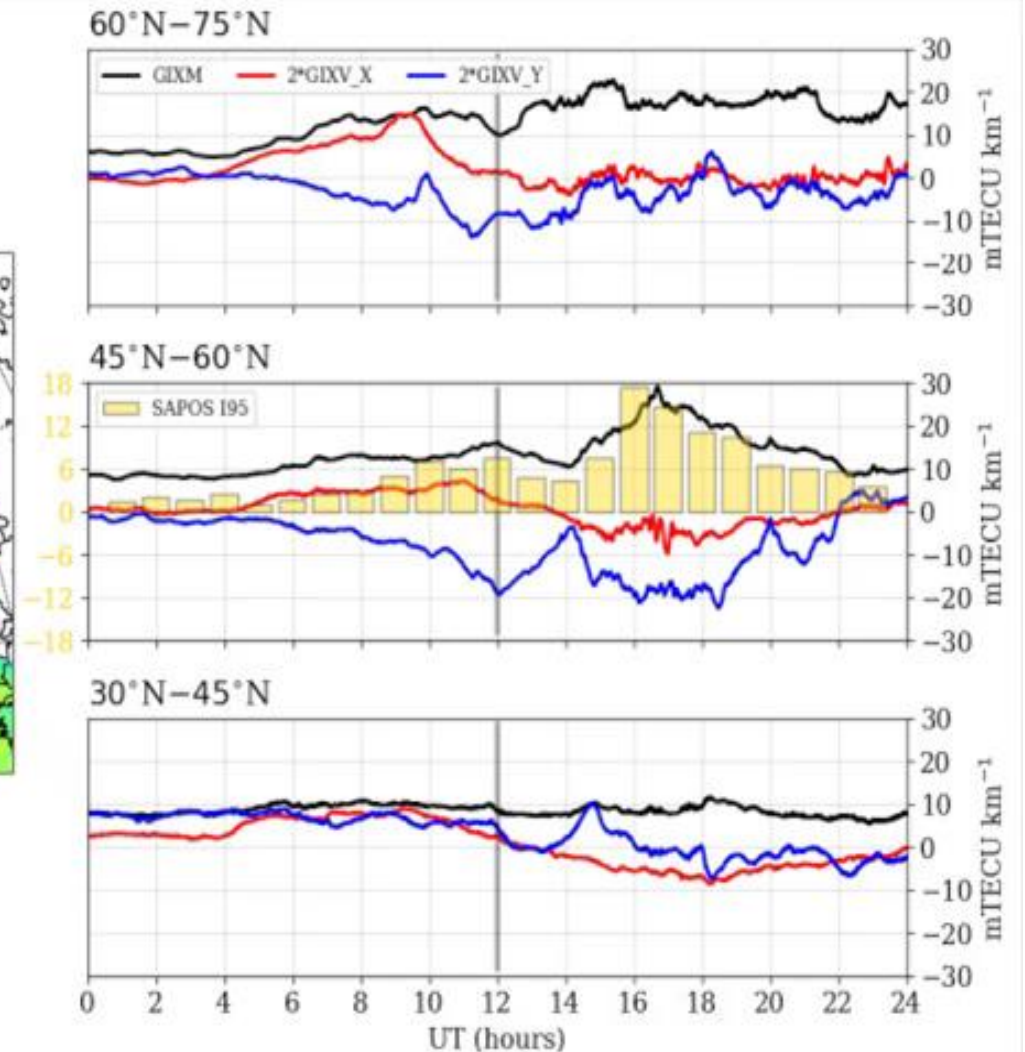
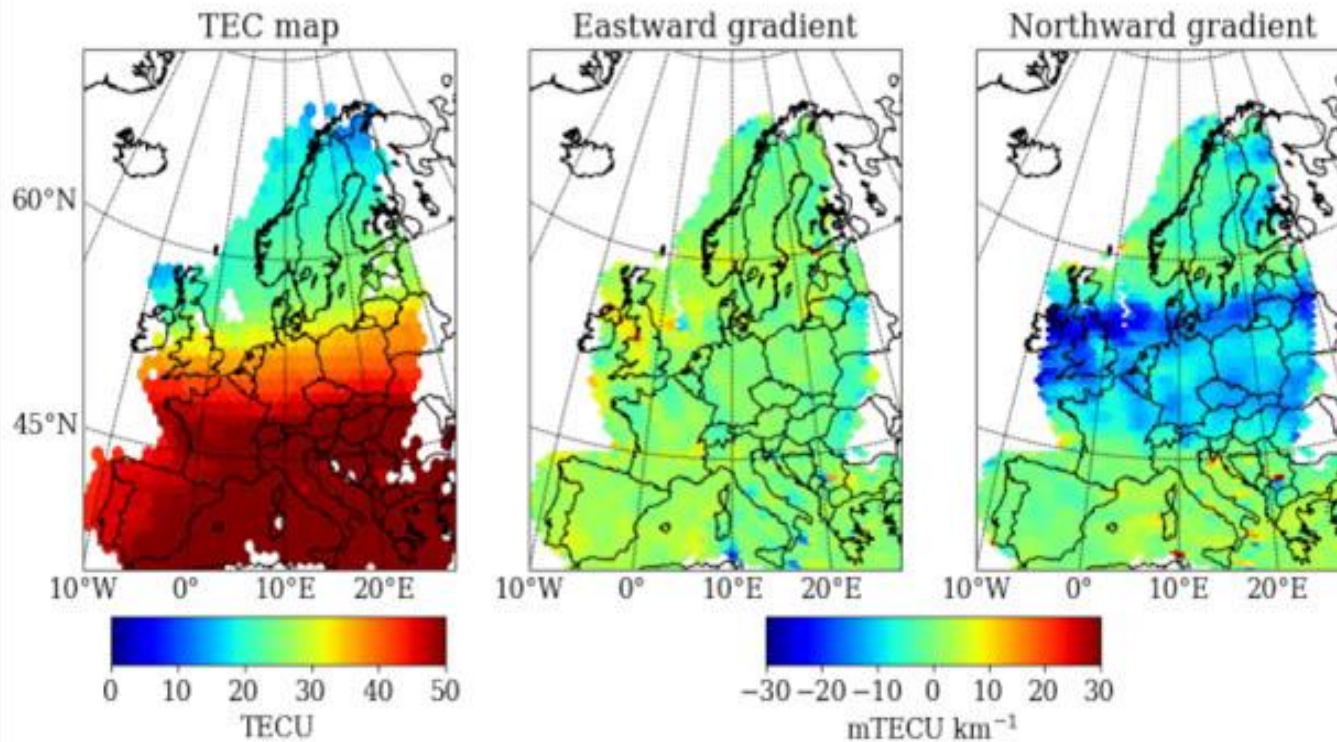
Ionospheric gradient vector: 4.8 mTECU/km  
Azimuth of ionospheric gradient vector: 181.1°



- ISWAT G2B-04 initiated a „Coordinated Ionosphere Study on Scales and Indices” (CISSI)
- Goal: comparison of different index approaches at disturbed and quiet periods (reference)

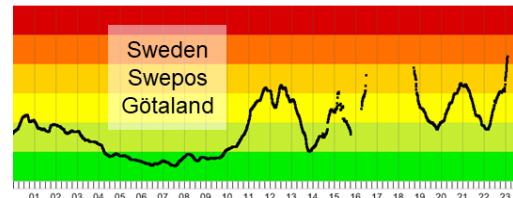
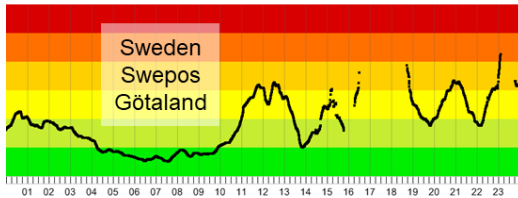
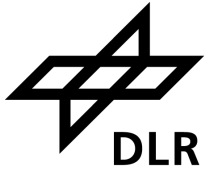
# Propagation of perturbations on St. Patrick's Day storm at March 17, 2015

2015-03-17 12:00:00 UT



# GIXM /GIXM95 scaling for GNSS positioning

Sample day: March 17, 2015



- Comparison of index approaches with user estimates of residual errors

## Top: SWEPOS

- Service for high accurate GNSS positioning in Sweden
- Operates Swedish national reference system
- <https://www.l5navigation.se/jonofarsmonitor/>

<https://www.l5navigation.se/jonofarsmonitor/>

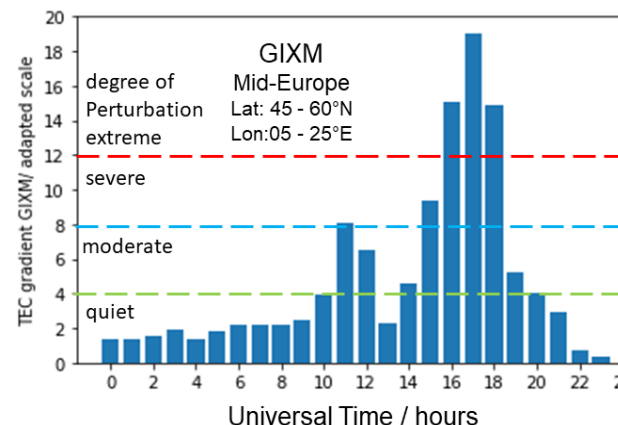
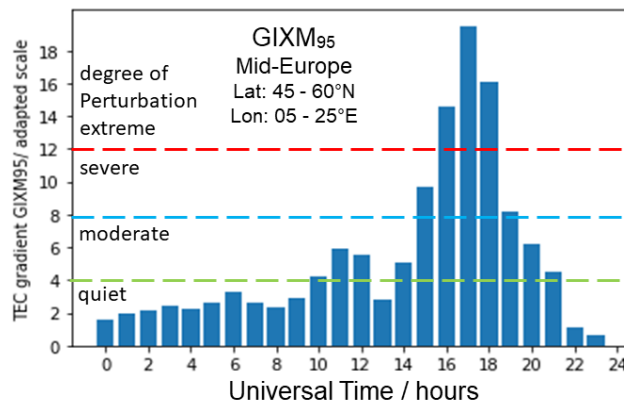
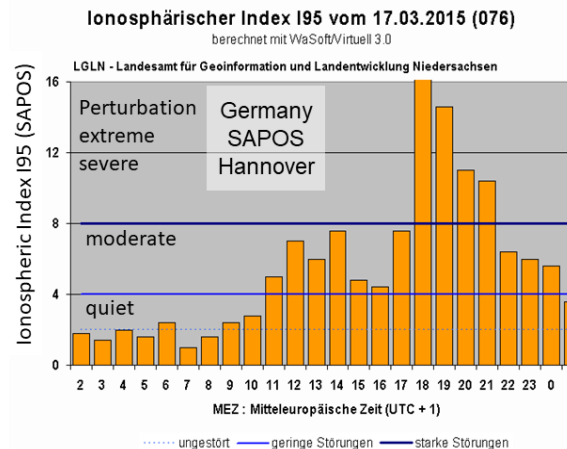
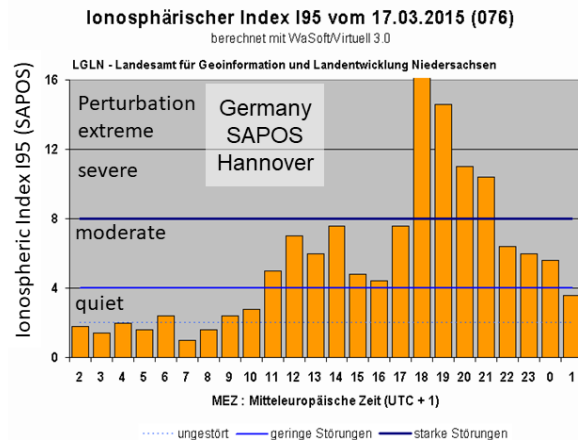
## Middle: SAPOS

- Service for high-accurate GNSS measurements in Germany
- Operates German GNSS reference network
- <https://www.lgln.niedersachsen.de/sapos/ionospheric-index-i95-51389.html>

## Comparison GIXM95 and GIXM

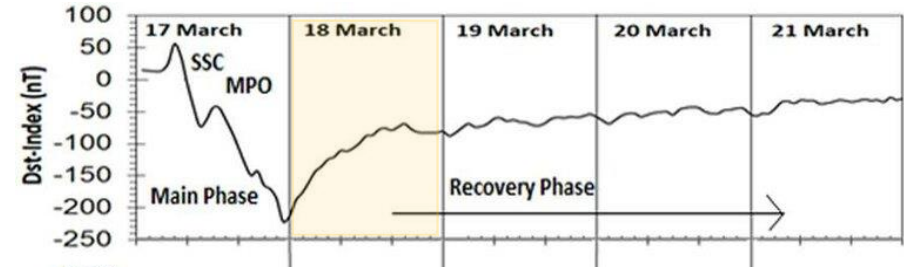
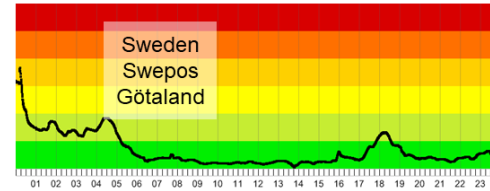
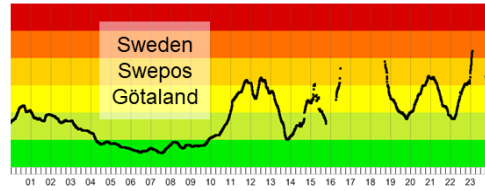
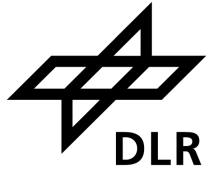
- Bottom left: adapted GIXM95 scale
- Bottom right: adapted GIXM scale

- Adapted indices GIXM95 and GIXM behave similarly, GIXM somewhat better

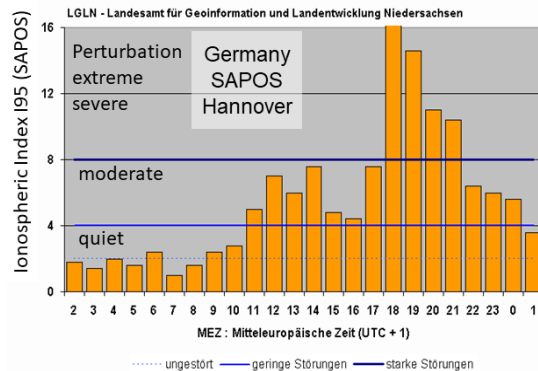


# GIXM scaling adapted to GNSS positioning approach (I95)

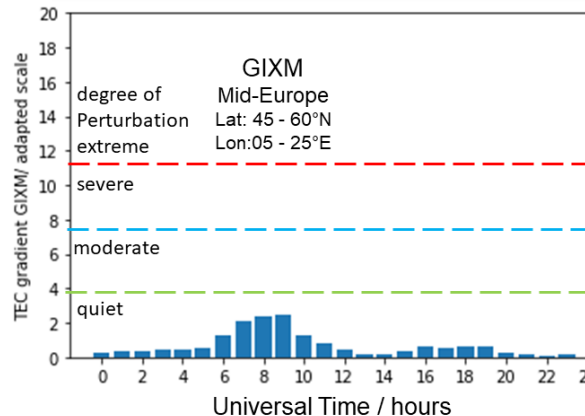
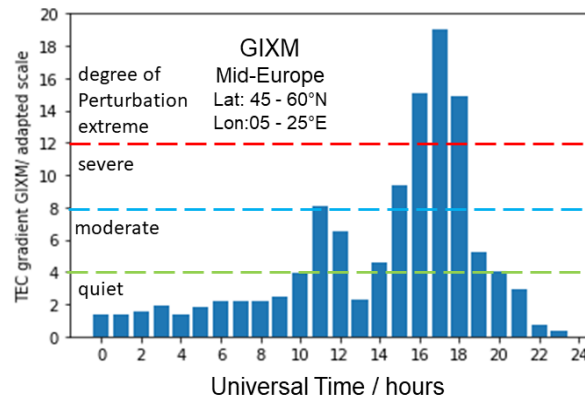
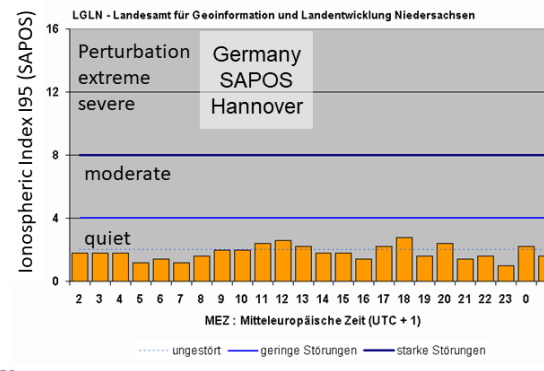
## Sample days: March 17 and 18, 2015



Ionosphärischer Index I95 vom 17.03.2015 (076)  
berechnet mit WaSoft/Virtuell 3.0



Ionosphärischer Index I95 vom 18.03.2015 (077)  
berechnet mit WaSoft/Virtuell 3.0



GIXM on March 17 and 18, 2015

Bottom left: March 17, 2015

Bottom right: March 18, 2015

Ionospheric storm effects disappear on March 18, 2015 at all scales

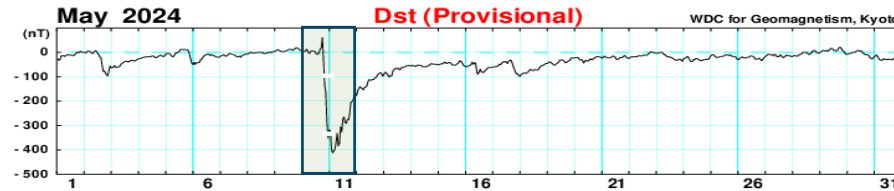
Dst mostly < -100 nT on March 18, 2015 during the recovery phase of the geomagnetic storm

Dst values not suited to estimate the perturbation degree of the ionosphere



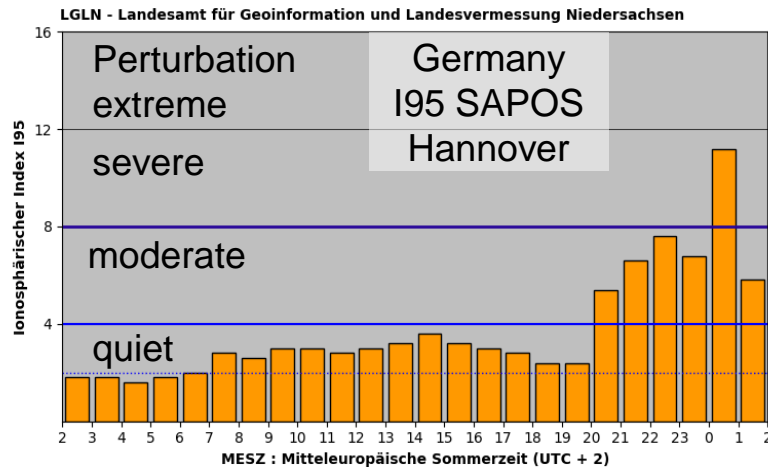
# GIXM comparison with I95 from SAPOS

## Sample days: May 10 and 11, 2024



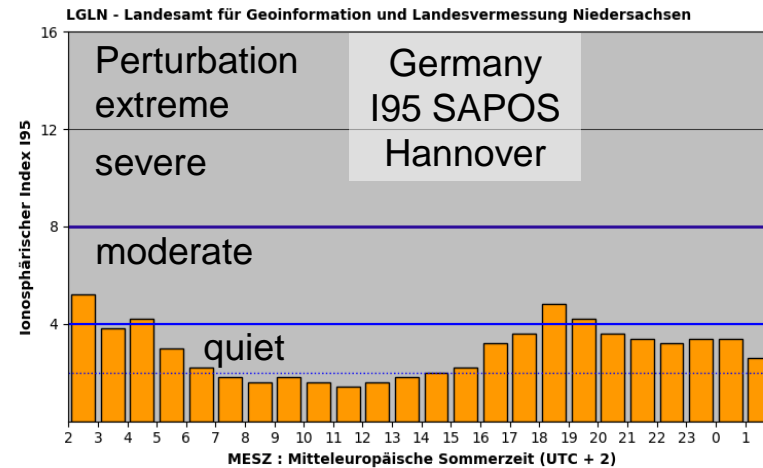
**Ionosphärischer Index I95 vom 10.05.2024 (131)**

berechnet mit WaSoft/WaV2



**Ionosphärischer Index I95 vom 11.05.2024 (132)**

berechnet mit WaSoft/WaV2

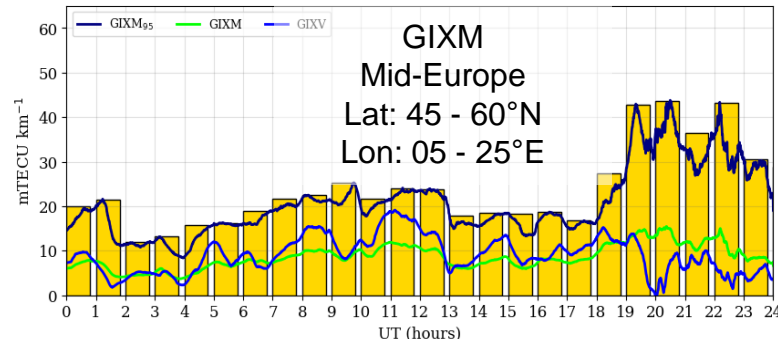


- GIXM and I95 from SAPOS/Germany show similar behaviour over recent storm days on May 10 and 11, 2024.

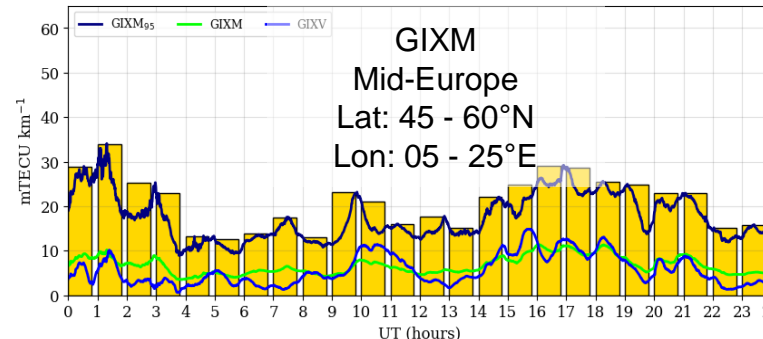
- Two main options for defining a trans-ionospheric SW scale:

- user adapted scale  
(seen in the previous slide)

Date: 2024-05-10

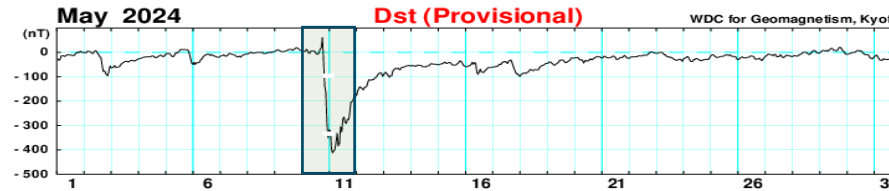


Date: 2024-05-11

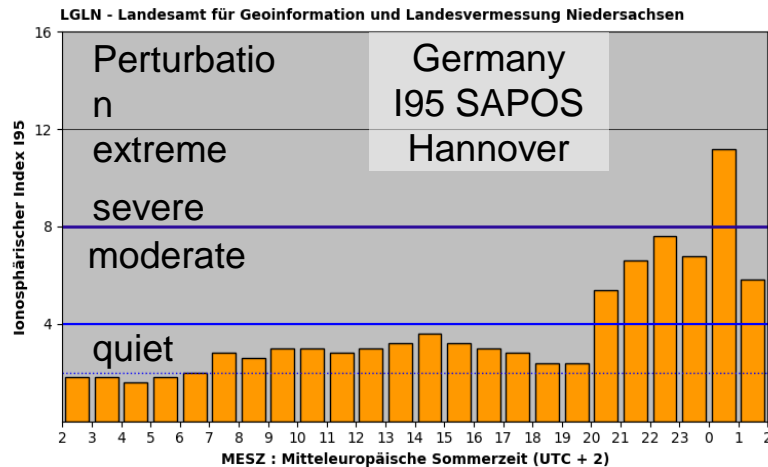


# GIXM comparison with I95 from SAPOS

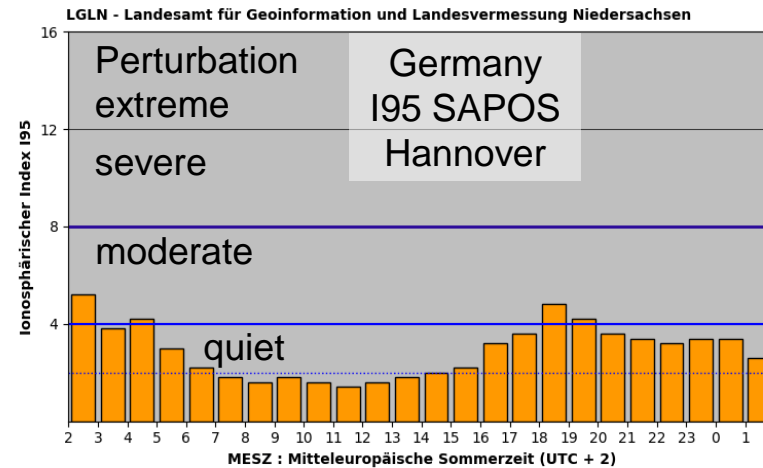
## Sample days: May 10 and 11, 2024



**Ionosphärischer Index I95 vom 10.05.2024 (131)**  
berechnet mit WaSoft/WaV2



**Ionosphärischer Index I95 vom 11.05.2024 (132)**  
berechnet mit WaSoft/WaV2

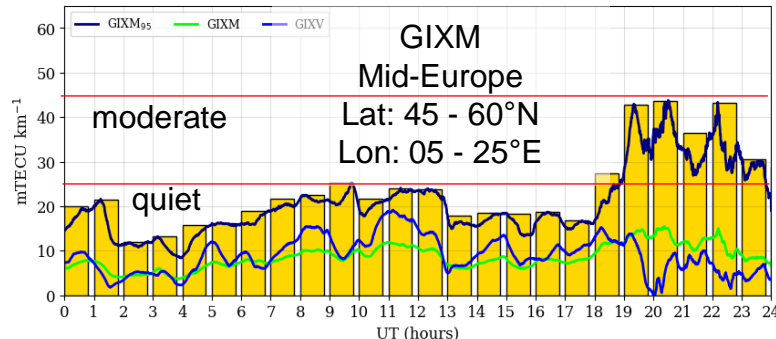


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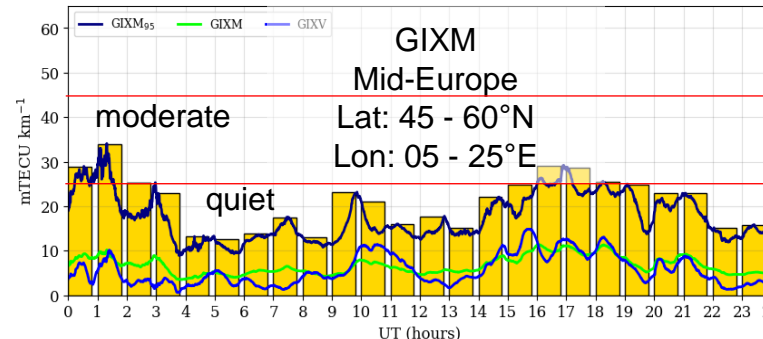
- Two main options for defining a trans-ionospheric SW scale:

- user adapted scale  
(seen in the previous slide)
- physics based definition including units  
Thresholds defined from users point of view

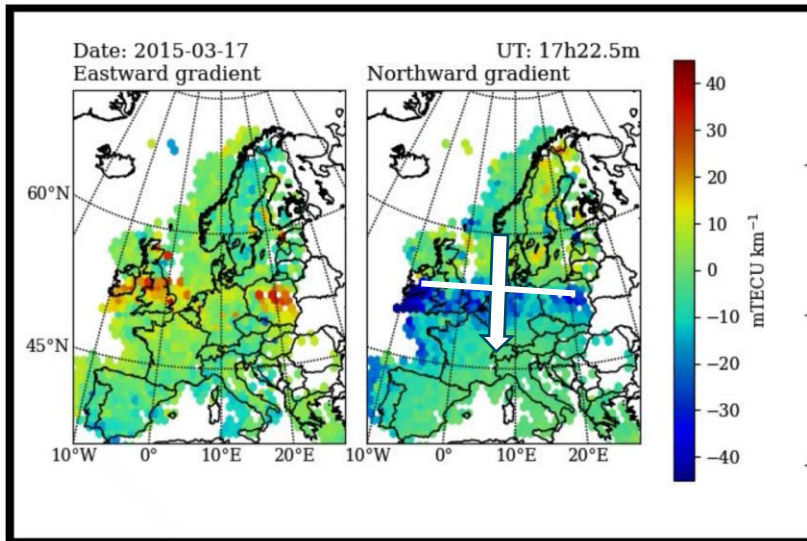
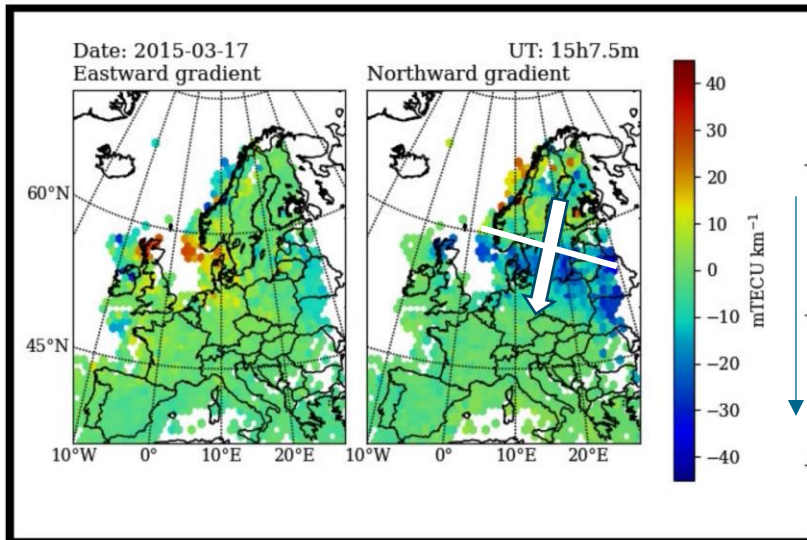
Date: 2024-05-10



Date: 2024-05-11



# Forecast of perturbation propagation using GIXV



Early detection of the propagating ionization front  
strength see color scale  
velocity  $\approx 55$  m/s \*  
direction  $\approx 188^\circ$

Forecast for lower latitudes

Permanent control of the ionization front parameters  
corresponding correction  
forecast for lower latitudes based on the estimation of  
the direction and velocity of the ionisation front.

Control of ionization front parameters at application area  
Forecast for lower latitudes  
Comparison of gradient values with positioning results at  
application areas, conclusions to further improve the  
prediction algorithms

\* Propagation velocity estimated between 15:08 and 17:23 UT

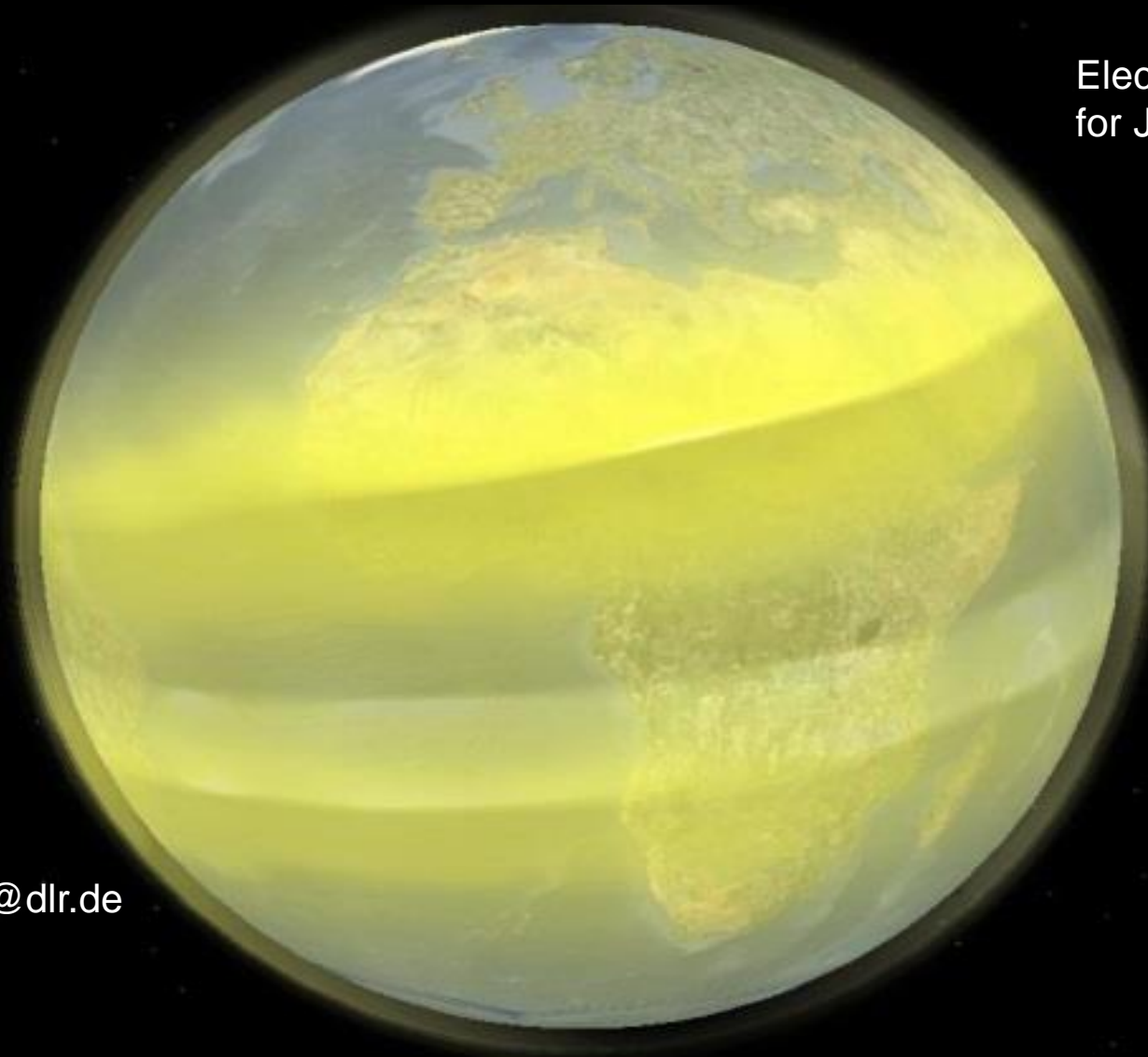
# Summary and conclusions



- GIX indicates spatial TEC structures over a selected area in near real time with high temporal resolution ( $\Delta t \geq 1\text{s}$ )
- SIDX indicates rapid change rates of TEC over a selected area with a time resolution  $\Delta t$  depending on the sampling rate of measurements
- Two different perturbation scales suggested
  - Academic based (use ionospheric parameters, solar wind relationships, comparative studies)
  - Application based (adapted to customer needs, easy and understandable use by customers)
- Customers are mainly interested in forecasts – two options to warn users:
  - Ionospheric observations at high latitudes used to estimate strength and dynamics of perturbations
  - Relationships between solar wind and indices are used to estimate dynamics of perturbation
- Close dialogue with users of space based radio systems (e.g. GNSS, remote sensing radars, radio astronomy) required to improve algorithms and scales.

# Ionosphere from space

Electron density reconstruction at DLR  
for July 23, 2011, 14:00 UT



Contact:  
Dr. Norbert Jakowski  
Kalkhorstweg 53  
D-17235 Neustrelitz  
Germany  
Email: [Norbert.Jakowski@dlr.de](mailto:Norbert.Jakowski@dlr.de)  
Web: <http://impc.dlr.de>

# Thank you !



Data SIO, NOAA, U.S. Navy, NGA, GEBCO  
Image IBCAO  
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