

# Prolonging a discrete time crystal by quantum-classical feedback

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Advancing  
Physics

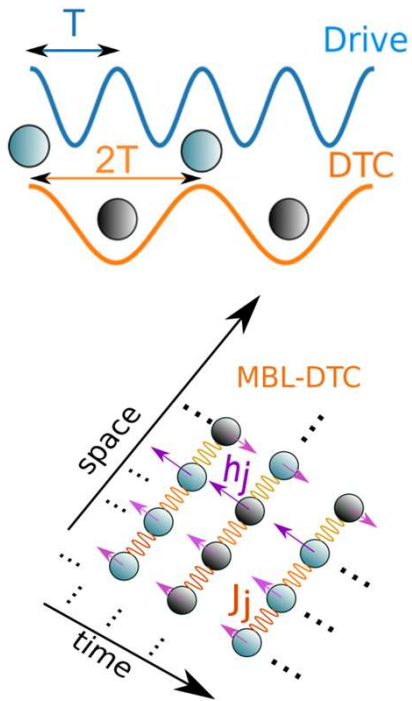


# Motivation



## 👉 DTC Concept

F. Wilczek,  
Phys. Rev. Lett. 109, 160401  
(2012)



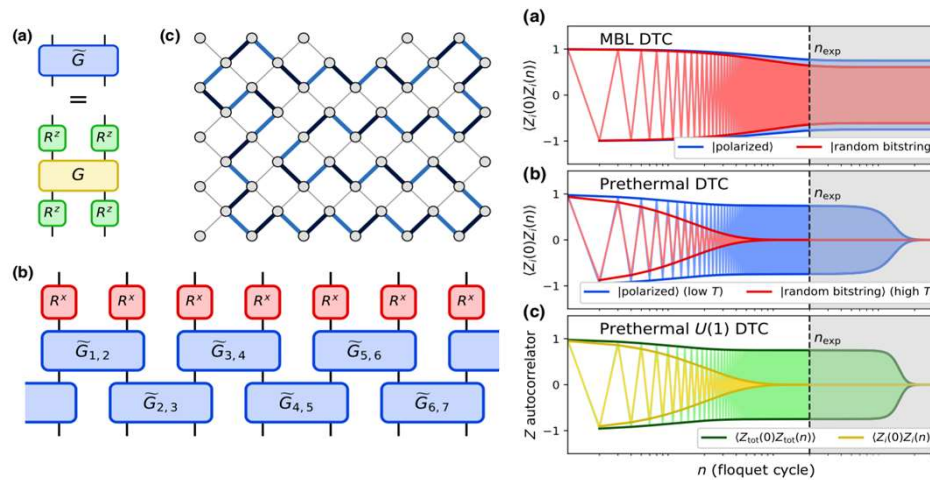
## 🔧 Proposal: DTC on a quantum computer

PRX QUANTUM 2, 030346 (2021)

Featured in Physics

### Many-Body Physics in the NISQ Era: Quantum Programming a Discrete Time Crystal

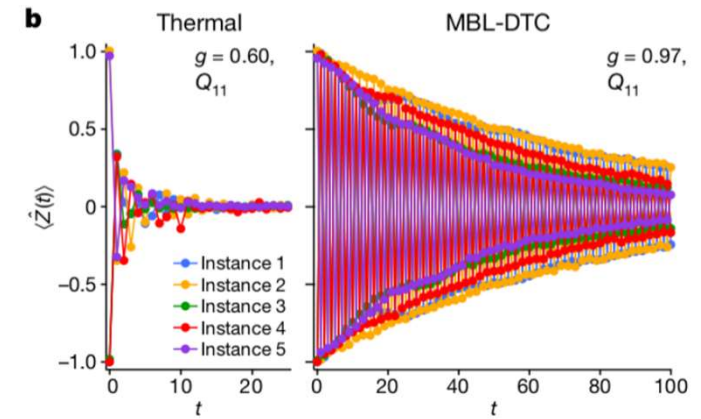
Matteo Ippoliti<sup>1,\*</sup>, Kostyantyn Kechedzhi<sup>2</sup>, Roderich Moessner<sup>3</sup>, S.L. Sondhi<sup>4</sup>, and Vedika Khemani<sup>1</sup>



## ✳️ DTC quantum experiment

✅ Realized on NISQ devices

❌ Problem: Decoherence noise



X. Mi et.al. Nature, 601, 531–536  
(2022)

# Approach

Overcoming noise effects employing in-circuit measurements

Hybrid computation quantum+classical

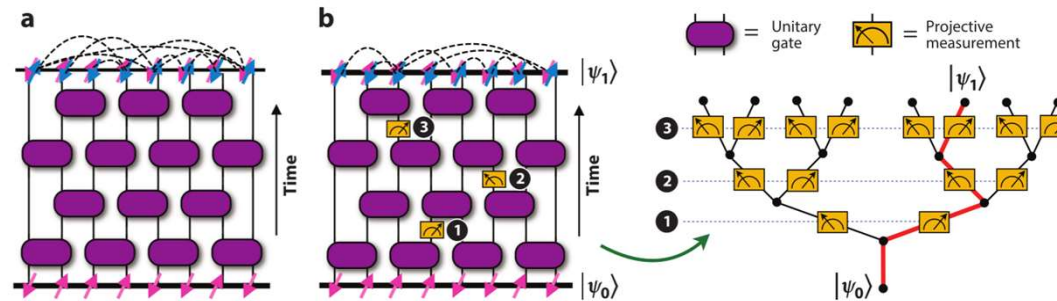
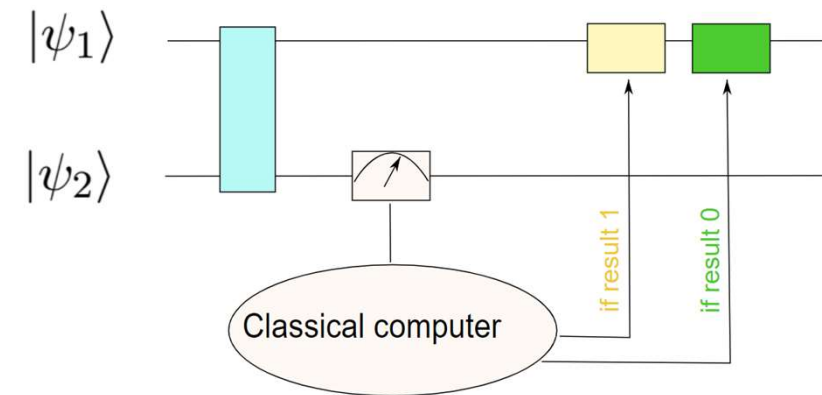
Near-to-classical quantum states  $\longrightarrow$  Low entanglement

$$|\Psi\rangle \text{ DTC states} \\ \cos(n\Omega) |\uparrow\uparrow\uparrow\uparrow\rangle + i \sin(n\Omega) |\downarrow\downarrow\downarrow\downarrow\rangle$$

Employ information on partial measurements to exert action over the state.

Context: Monitored quantum circuits (non-unitary operations)

Simplest quantum-classical feedback



# Model

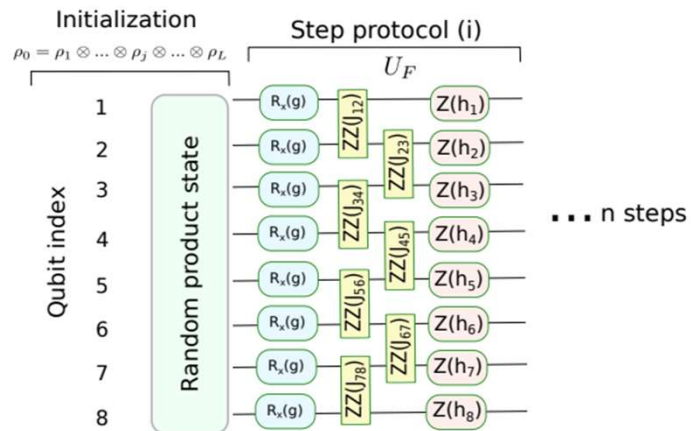
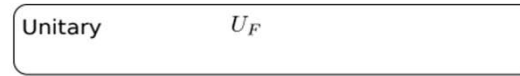
## Floquet unitary

$$U_F = e^{-i\frac{T}{4} \sum_j (J_j \sigma_j^z \sigma_{j+1}^z + 2h_j \sigma_j^z)} e^{-i\frac{\pi g}{2} T \sum_j \sigma_j^x}$$

X. Mi et.al. Nature, 601, 531–536 (2022)

## Quantum circuit realization

G.Camacho, B.Fauseweh, arXiv:2309.02151



# Model

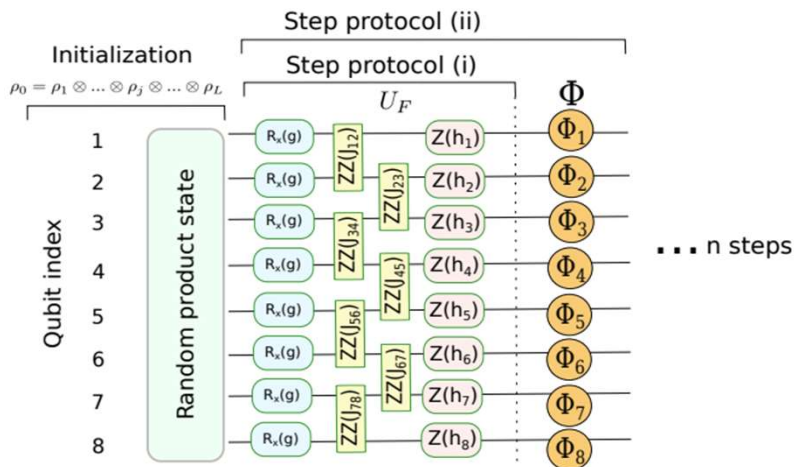
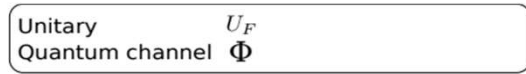
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X. Mi et.al. Nature, 601, 531–536 (2022)

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X. Mi et.al. Nature, 601, 531–536 (2022)

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G. Camacho, B. Fauseweh, arXiv:2309.02151

## Bit-flip noise model

$$\Phi(\rho) = \sum_{i=0}^{Q-1} K_i \rho K_i^\dagger, \quad \sum_i K_i^\dagger K_i = I$$

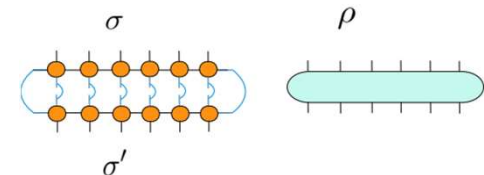
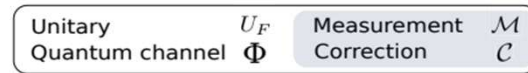
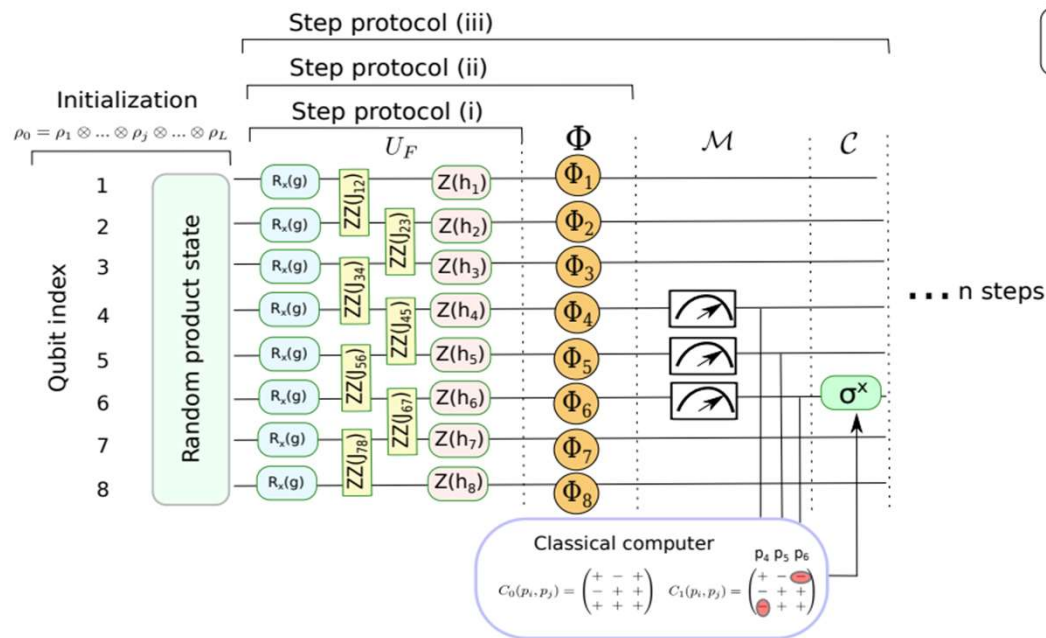
## Kraus operators

$$K_0 = \sqrt{1-p}I, \quad K_1 = \sqrt{p}\sigma^x$$

Represent state  $\rho$  as  
Matrix Product Density Operator  
(MPDO)

F. Verstraete, et.al. Phys. Rev. Lett. 93, 207204 (2004)

A. H. Werner et.al. Phys. Rev. Lett. 116, 237201 (2016)



Protocol (i)  $\rho_n = U_F^n \rho_0 (U_F^\dagger)^n$

Protocol (ii)  $\rho_n = \Phi \left( U_F \rho_{n-1} U_F^\dagger \right)$

Protocol (iii)  $\rho_n = \mathcal{C} \circ \mathcal{M} \circ \Phi \left( U_F \rho_{n-1} U_F^\dagger \right)$

# Correction scheme for protocol (iii)

At step “n”...

(1) Measure M adjacent qubits at random location

$$\mathcal{S}^{(n)} = \{x_0^{(n)}, x_0^{(n)} + 1, \dots, x_0^{(n)} + M - 1\}$$

Set of indices

(2) Store result into classical register (bits)

$$\vec{\sigma}_n(\mathcal{S}^{(n)}) \Big|_{\sigma_j \in \{+1, -1\}}$$

Initialization values

$$\vec{\sigma}_0(\mathcal{S}^{(n)})$$

(3) Compute classical correlations for that specific domain wall

$$C_n(i, j) = \vec{\sigma}_n^T \otimes \vec{\sigma}_n \quad i, j \in \mathcal{S}^{(n)}$$

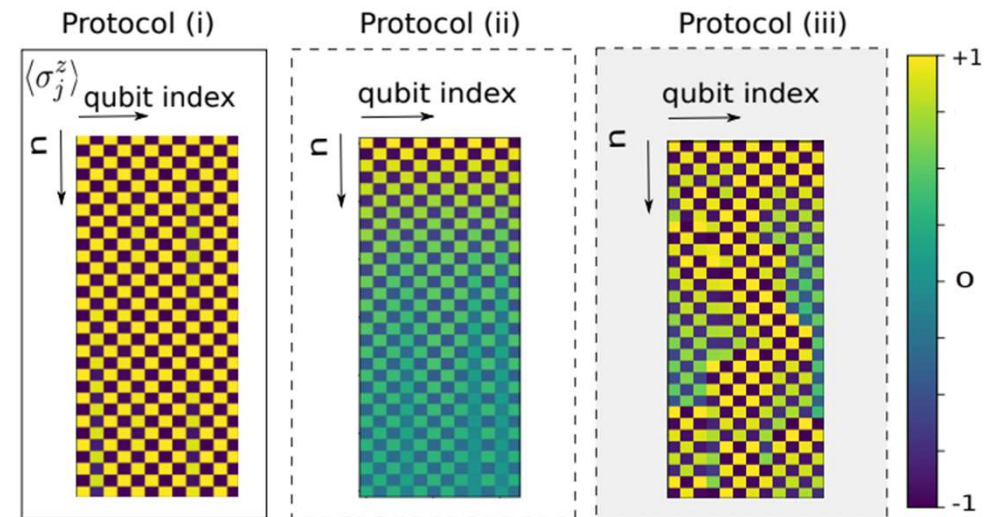
Comparison matrix

$$C_0(i, j) = \vec{\sigma}_0^T \otimes \vec{\sigma}_0 \quad \delta_{ij}(n) = \text{int} \left( \frac{1}{2} (J_{ij} - C_0(i, j) * C_n(i, j)) \right)$$

(4) Identify index  $i(n)$  and correct

$$i(n) = \max \left( \sum_j \delta_{ij}(n) \right) \quad \dots \text{continue to step } n+1$$

Protocol instances



### Key remarks for DTC correction

- ✓ T-periodic scheme
- ✓ Local regions correction
- ✓ Error qubit identification improves with number of qubits

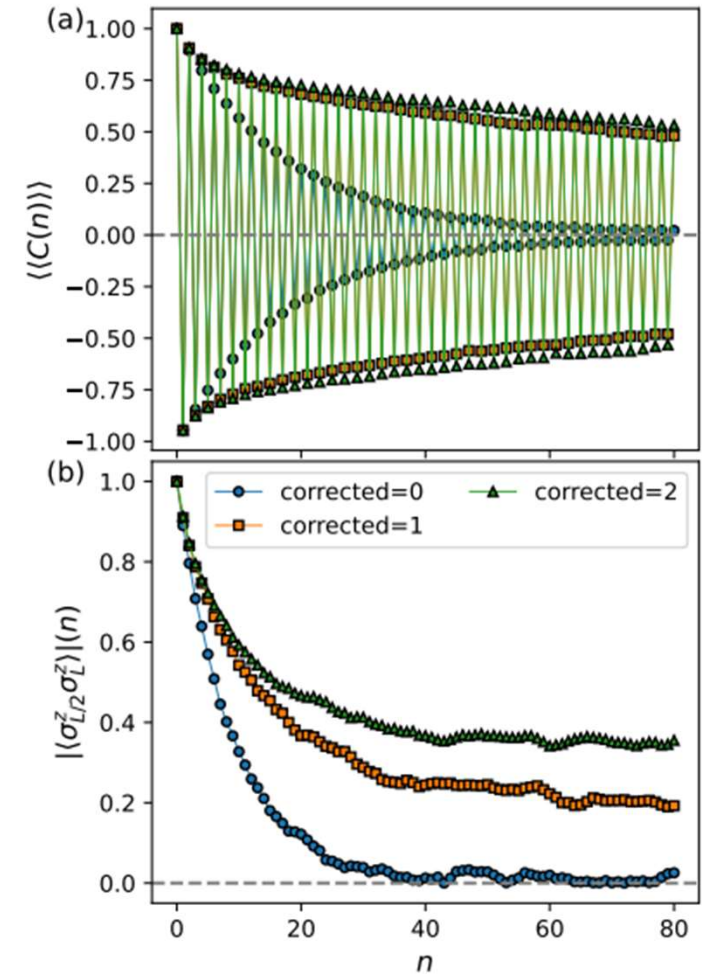
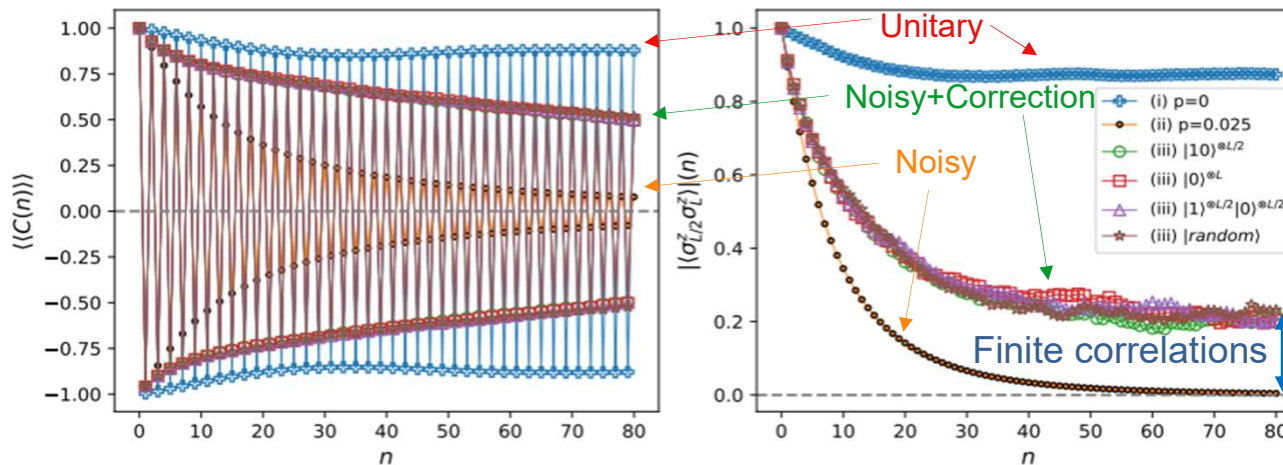
# Results

- Initial state independence
- DTC correlations beyond intrinsic decoherence times employing feedback

Correction scheme verification:

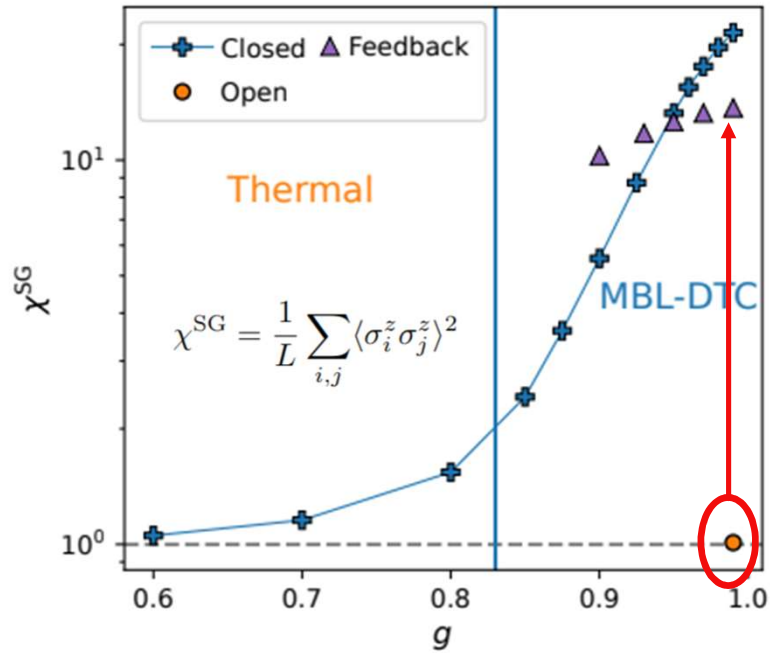
- Site and disorder averaged autocorrelation
- Bulk-edge spin correlations

Chain  $L=24$ ,  $g=0.97$ ,  $M=6$ ,  $N_{\text{dis}}=1280$



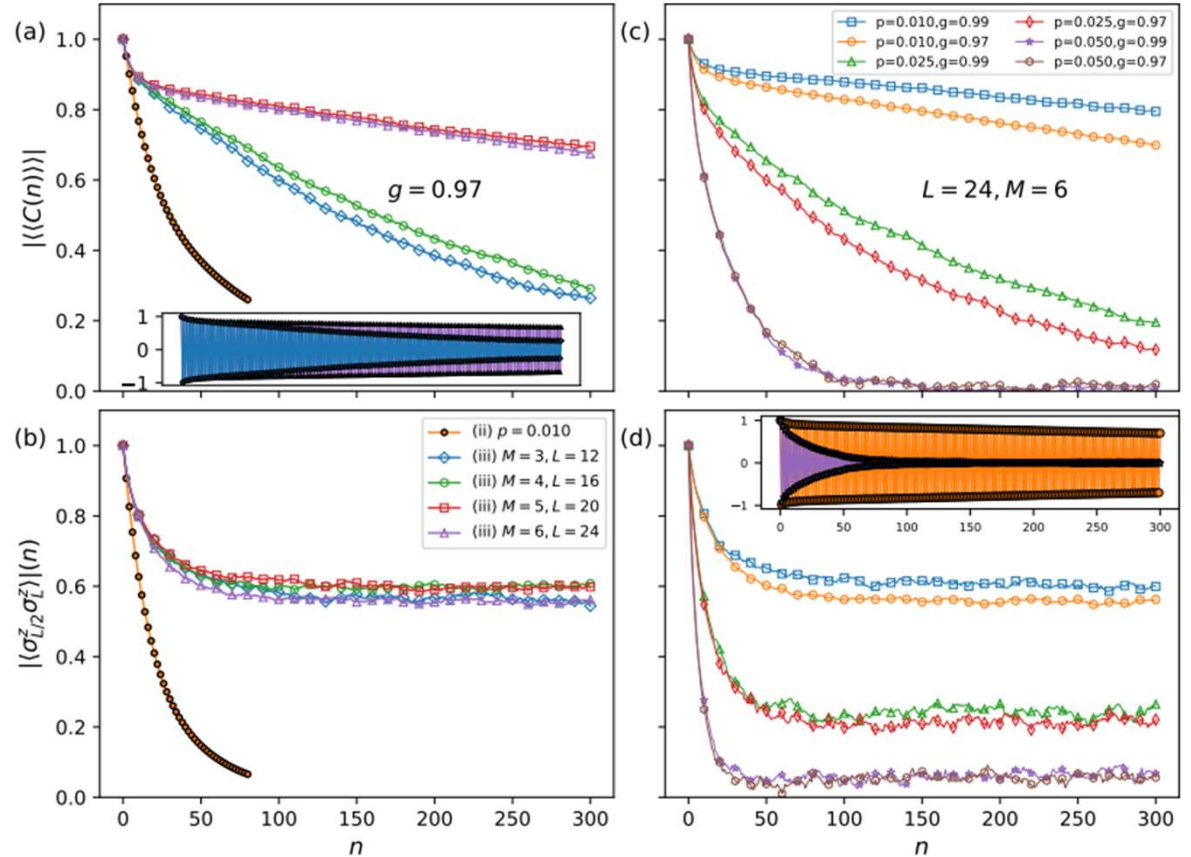


# Results



- Enhanced glassy spatial order employing feedback (protocol (iii))

G.Camacho, B.Fauseweh, arXiv:2309.02151



- Favourable scaling with system size
- Noise parameter is dominant over kick parameter

# Summary and outlook



## Main results

- ▣ Feedback scheme based on mid-circuit measurements enhances DTC response on a noisy environment
- ▣ Correction from feedback is essential: Beyond pure Zeno effect
- ▣ Protocol independent of state preparation, and periodic with period  $T$
- ▣ Good scaling with increasing system size and domain wall size

## Outlook

- ▣ Implementation of feedback scheme on current hardware employing dynamic circuits functionalities
- ▣ Alternative noise models, measurement protocols, generalization to qudit systems
- ▣ Monitored quantum dynamics affected by feedback schemes