Relativistic effects in macroscopically delocalized quantum superpositions

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Dr. Albert Roura, Institute of Quantum Technologies, 01.02.2024

Macroscopically delocalized quantum superpositions:

coherent superposition of spatially separated atomic wave packets.



- Differences in dynamics of superposition components entirely Newtonian.
- Same relativistic effects on superposition components (e.g. atomic clocks).
 STANFORD UNIVERSITY
- <u>Goal (QM + GR)</u>: experiment with general relativistic effects acting non-trivially on the quantum superposition.





Proper time as which-way information

 Quantum superposition of clocks (COM + internal state)

experiencing different proper times

reduced visibility of interference signal

Zych et al., Nat. Commun. 2, 505 (2011)

Sinha & Samuel, Class. Quantum Grav. 28, 145018 (2011)





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Outline



- 1. Key elements of quantum-clock interferometry
- 2. Major challenges in quantum-clock interferometry
- 3. Doubly differential gravitational-redshift measurement
- 4. Spacetime curvature and proper-time difference
- 5. Conclusions



Key elements of quantum-clock interferometry

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Quantum clock model





• *Initialization* pulse:

$$|\mathbf{g}
angle \rightarrow |\Phi(0)
angle = \frac{1}{\sqrt{2}} \Big(|\mathbf{g}
angle + i \, e^{i\varphi} |\mathbf{e}
angle \Big)$$

• Evolution:

$$|\Phi(\tau)\rangle \propto \frac{1}{\sqrt{2}} \Big(|\mathbf{g}\rangle + i \, e^{i\varphi} e^{-i\Delta E \, \tau/\hbar} |\mathbf{e}\rangle\Big)$$

$$\left| \langle \Phi(\tau_b) | \Phi(\tau_a) \rangle \right| = \cos\left(\frac{\Delta E}{2\hbar} \left(\tau_b - \tau_a\right)\right)$$



• Comparison of independent clocks (after read-out pulse):





$$\Delta \tau_b - \Delta \tau_a \approx \left(g L_z/c^2\right) \Delta t$$

for optical atomic clocks

$$\Delta E \sim 1 \,\mathrm{eV}$$
 $L_z \sim 1 \,\mathrm{cm}$



Comparison of independent clocks (after read-out pulse):



$$\Delta \tau_b - \Delta \tau_a \approx \left(g L_z/c^2\right) \Delta t$$



 L_z



- Theoretical description of the clock:
 - two-level atom (internal state):

 $\hat{H} = \hat{H}_1 \otimes |\mathbf{g}\rangle \langle \mathbf{g}| + \hat{H}_2 \otimes |\mathbf{e}\rangle \langle \mathbf{e}|$

$$m_1 = m_g$$

 $m_2 = m_g + \Delta m$
 $\Delta m = \Delta E/c^2$

classical action for COM motion:

$$S_n[x^{\mu}(\lambda)] = -m_n c^2 \int d\tau = -m_n c \int d\lambda \sqrt{-g_{\mu\nu}} \frac{dx^{\mu}}{d\lambda} \frac{dx^{\nu}}{d\lambda} \qquad (n = 1, 2)$$

free fall



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$$m_1 = m_g$$

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classical action for COM motion:

$$S_n\left[x^{\mu}(\lambda)\right] = -m_n c^2 \int d\tau \approx \int_{t_0}^t dt' \left(-m_n c^2 + \frac{1}{2}m_n \dot{\mathbf{x}}^2 - m_n U(t', \mathbf{x})\right)$$

free fall

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$$m_1 = m_g$$

 $m_2 = m_g + \Delta m$
 $\Delta m = \Delta E/c^2$

classical action for COM motion:

$$S_n \left[x^{\mu}(\lambda) \right] = -m_n c^2 \int d\tau - \int d\tau \, V_n(x^{\mu}) \qquad (n = 1, 2)$$

including external forces



Atom interferometry in curved spacetime (including relativistic effects)

- Wave-packet evolution in terms of
 - central trajectory (satisfies classical e.o.m.) $X^{\mu}(\lambda)$
 - centered wave packet $\left|\psi_{\mathrm{c}}^{(n)}(au_{\mathrm{c}})\right\rangle$



• Metric in *Fermi-Walker* coordinates:





$$ds^{2} = g_{\mu\nu}dx^{\mu}dx^{\nu} = g_{00} c^{2}d\tau_{c}^{2} + 2 g_{0i} c d\tau_{c} dx^{i} + g_{ij} dx^{i}dx^{j}$$

$$g_{00} = -(1 + \delta_{ij} a^{i}(\tau_{c}) x^{j}/c^{2})^{2} - R_{0i0j}(\tau_{c}, \mathbf{0}) x^{i}x^{j} + O(|\mathbf{x}|^{3})$$

$$g_{0i} = -\frac{2}{3}R_{0jik}(\tau_{c}, \mathbf{0}) x^{j}x^{k} + O(|\mathbf{x}|^{3})$$

$$g_{ij} = \delta_{ij} - \frac{1}{3}R_{ikjl}(\tau_{c}, \mathbf{0}) x^{k}x^{l} + O(|\mathbf{x}|^{3})$$

• Expanding the action for the *centered wave packet*:

$$X^{\mu}(\tau_{\rm c}) = \left(c \,\tau_{\rm c} , \mathbf{0}\right)$$
$$\hat{H}_n = m_n c^2 + V_n(\tau_{\rm c}, \mathbf{0}) + \hat{H}_{\rm c}^{(n)}$$



- Wave-packet evolution: $|\psi^{(n)}(\tau_{\rm c})\rangle = e^{iS_n/\hbar} |\psi^{(n)}_{\rm c}(\tau_{\rm c})\rangle$
 - propagation phase

$$\mathcal{S}_n = -\int_{\tau_1}^{\tau_2} d\tau_{\rm c} \left(m_n c^2 + V_n(\tau_{\rm c}, \mathbf{0}) \right)$$

centered wave packet

$$i\hbar \frac{d}{d\tau_{\rm c}} \left| \psi_{\rm c}^{(n)}(\tau_{\rm c}) \right\rangle = \hat{H}_{\rm c}^{(n)} \left| \psi_{\rm c}^{(n)}(\tau_{\rm c}) \right\rangle$$

$$\hat{H}_{c}^{(n)} = \frac{1}{2m_{n}} \hat{\mathbf{p}}^{2} + \frac{1}{2} \hat{\mathbf{x}}^{T} \left(\mathcal{V}^{(n)}(\tau_{c}) - m_{n} \Gamma(\tau_{c}) \right) \hat{\mathbf{x}}$$
gravity-gradient tensor

 $\mathcal{V}_{ij}^{(n)}(\tau_{\rm c}) = \left. \partial_i \partial_j V_n(\tau_{\rm c}, \mathbf{x}) \right|_{\mathbf{x} = \mathbf{0}}$

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• Full interferometer (including *laser kicks*):



propagation + laser phases

$$|\psi_{
m I}
angle = rac{1}{2} \left(e^{i\phi_a} + e^{i\phi_b}
ight) |\psi_{
m c}
angle$$

• Detection *probability* at the *exit port(s)*:

 $\langle \psi_{\mathrm{I}} | \psi_{\mathrm{I}} \rangle = \frac{1}{2} \left(1 + \cos \delta \phi \right)$

• Phase shift: $\delta \phi = \phi_b - \phi_a + \delta \phi_{sep}$

For further details:



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Gravitational Redshift in Quantum-Clock Interferometry

Albert Roura

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- Relativistic description of atom interferometry in curved spacetime.
- Including *external forces* and even *guiding potentials*.
- *Relativistic* interpretation of the *separation phase* in open interferometers.



Major challenges in quantum-clock interferometry

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Insensitivity to gravitational redshift (in a uniform field)

• Consider a freely falling frame:



• Proper-time difference between the two interferometer branches independent of *g*.

(small dependence due to pulse timing suppressed by $(v_{
m rec}/c) \sim 10^{-10}$)



Insensitivity to gravitational redshift (in a uniform field)

• Consider a freely falling frame:



Proper-time difference between the two interferometer branches independent of g.

(small dependence due to pulse timing suppressed by $(v_{
m rec}/c) \sim 10^{-10}$)

Differential recoil





Implied changes of proper-time difference are comparable to signal of interest.

Small visibility changes



• Reduced interference visibility due to deceasing quantum overlap of clock states:

$$\left\langle \Psi_{\mathrm{I}} | \Psi_{\mathrm{I}} \right\rangle = \frac{1}{2} + \frac{1}{2} \left| \left\langle \Phi(\tau_{b}) | \Phi(\tau_{a}) \right\rangle \right| \cos \delta \phi \qquad \left| \left\langle \Phi(\tau_{b}) | \Phi(\tau_{a}) \right\rangle \right| = \cos \left(\frac{\Delta E}{2\hbar} \left(\tau_{b} - \tau_{a} \right) \right)$$

• Small effect for feasible parameter range:

 $\Delta E/\hbar = \omega_0 \approx 2\pi \times 4 \times 10^2 \,\mathrm{THz}$

$$\langle \Phi(\tau_b) | \Phi(\tau_a) \rangle \Big| = \cos\left(\frac{\omega_0}{2} \frac{g \,\Delta z}{c^2} \,\Delta t\right) \approx 1 - (10^{-3})^2/2 \qquad \Delta z = 1 \,\mathrm{cm} \qquad \Delta t = 1 \,\mathrm{s}$$

 Extremely difficult to measure such small changes of visibility, which are masked by other effects leading also to loss of visibility.

Small visibility changes



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 Extremely difficult to measure such small changes of visibility, which are masked by other effects leading also to loss of visibility.



Doubly differential gravitational-redshift measurement

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Gravitational Redshift in Quantum-Clock Interferometry

Albert Roura

Quantum superposition of a single clock at two different heights

- Initialization pulse after the spatial superposition has been generated.
- Doubly differential measurement:
 - state-selective detection
 - compare different initialization times





Differential phase-shift measurement

Detection probability at first exit port (independent of internal state):

$$\begin{split} \Psi_{\mathrm{I}}|\Psi_{\mathrm{I}}\rangle &= \frac{1}{2} \left(\left\langle \Psi_{\mathrm{I}}^{(1)} \middle| \Psi_{\mathrm{I}}^{(1)} \right\rangle + \left\langle \Psi_{\mathrm{I}}^{(2)} \middle| \Psi_{\mathrm{I}}^{(2)} \right\rangle \right) \\ &= \frac{1}{4} \left(1 + \cos \delta \phi^{(1)} + 1 + \cos \delta \phi^{(2)} \right) \\ &= \frac{1}{2} + \frac{1}{2} \cos \left(\frac{\delta \phi^{(2)} - \delta \phi^{(1)}}{2} \right) \cos \left(\frac{\delta \phi^{(1)} + \delta \phi^{(2)}}{2} \right) \\ & \overbrace{\text{visibility}} \end{split}$$

- Phase-shift difference directly related to visibility reduction.
- Precise differential phase-shift measurement with state-selective detection much more viable (immune to spurious loss of contrast + common-mode rejection of phase noise)

Two-photon pulse for clock initialization



• Level structure for group-II-type atoms (e.g. Sr, Yb) employed in optical atomic clocks:



- Two-photon process resonantly connecting the two clock states.
- Equal-frequency counter-propagating laser beams in lab frame $e^{i\omega t}e^{i\mathbf{k}\cdot\mathbf{x}} \times e^{i\omega t}e^{-i\mathbf{k}\cdot\mathbf{x}} = e^{i2\omega t}$
 - → constant effective-phase simultaneity hypersurfaces in lab frame.

Laboratory frame



• Compare differential phase-shift measurements for different initialization times:



$$\left(\delta\phi^{(2)}(t_{i}') - \delta\phi^{(1)}(t_{i}')\right) - \left(\delta\phi^{(2)}(t_{i}) - \delta\phi^{(1)}(t_{i})\right) = \frac{\Delta E}{2\hbar} \left(\Delta\tau_{b} - \Delta\tau_{a}\right) = \Delta m g \,\Delta z \,(t_{i}' - t_{i})/\hbar$$

Laboratory frame



• Compare differential phase-shift measurements for different initialization times:



$$\left(\delta\phi^{(2)}(t_{i}') - \delta\phi^{(1)}(t_{i}')\right) - \left(\delta\phi^{(2)}(t_{i}) - \delta\phi^{(1)}(t_{i})\right) = \frac{\Delta E}{2\hbar} \left(\Delta\tau_{b} - \Delta\tau_{a}\right) = \Delta m g \,\Delta z \,(t_{i}' - t_{i})/\hbar$$

Laboratory frame



• Compare differential phase-shift measurements for different initialization times:



Freely falling frame



• Relativity of simultaneity: $\Delta \tau_{\rm c} \approx -v(t) \Delta z/c^2 = g \left(t - t_{\rm ap}\right) \Delta z/c^2$



Challenges addressed



- Comparing measurements with *different initialization times*

→ sensitive to gravitational redshift + further immunity

Almost no recoil from initialization pulse:

small residual recoil with no impact on gravitational redshift measurement.

Effect of differential recoil from second pair of Bragg pulses cancels out in doubly differential measurement.



• Residual recoil with no influence on the phase-shift for the excited state:



Feasible implementation



- 10-m atomic fountains operating with Sr, Yb in Stanford & Hannover respectively.
- More than 2 s of free evolution time.
- Doubly differential phase shift of $3 \operatorname{mrad}$ for

 $\Delta E/\hbar = \omega_0 \approx 2\pi \times 4 \times 10^2 \,\mathrm{THz}$ $\Delta z = 1 \,\mathrm{cm}$ $\Delta t_\mathrm{i} = 1 \,\mathrm{s}$

resolvable in a single shot for $N = 10^5$ (shot-noise limited).

VLBAI (Hannover)





Alternative implementation

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Demanding requirements on the atom optics



- <u>Main challenge</u>: last pair of laser pulses should <u>diffract both internal states</u> efficiently.
- Two possibilities:
 - ▶ Bragg diffraction at the magic wavelength → very demanding requirements on laser power
 - Combination of single-photon transitions

 higher complexity, fermionic isotopes
 far from maturity
- Look for an alternative scheme involving simple atom optics with milder requirements on laser power that could be implemented at the VLBAI facility.



Quantum-clock interferometry



$$\left(\delta\phi^{(2)}(t'_{i}) - \delta\phi^{(1)}(t'_{i})\right) - \left(\delta\phi^{(2)}(t_{i}) - \delta\phi^{(1)}(t_{i})\right) = \frac{\Delta E}{2\hbar} \left(\Delta\tau_{b} - \Delta\tau_{a}\right) = \Delta m g \,\Delta z \,(t'_{i} - t_{i})/\hbar$$

doubly differential measurement



Quantum-clock interferometry



$$\left(\delta\phi^{(2)}(t'_{i}) - \delta\phi^{(1)}(t'_{i})\right) - \left(\delta\phi^{(2)}(t_{i}) - \delta\phi^{(1)}(t_{i})\right) = \frac{\Delta E}{2\hbar} \left(\Delta\tau_{b} - \Delta\tau_{a}\right) = \Delta m g \,\Delta z \,(t'_{i} - t_{i})/\hbar$$

doubly differential measurement



Alternative interferometry scheme



 Differential phase shift between the two shots directly sensitive to gravitational time dilation:

$$\delta\phi_A - \delta\phi_B = -\Delta m \, c^2 \, (\Delta\tau_b - \Delta\tau_a)/\hbar = -\Delta m \, g \, \Delta z \, (t_{\rm f} - t_{\rm i})/\hbar$$



Alternative interferometry scheme



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$$\delta\phi_A - \delta\phi_B = -\Delta m \, c^2 \, (\Delta\tau_b - \Delta\tau_a)/\hbar = -\Delta m \, g \, \Delta z \, (t_{\rm f} - t_{\rm i})/\hbar$$



Alternative interferometry scheme



• Test of UGR with a delocalized quantum superposition (*dilaton* model):

$$\delta\phi_A - \delta\phi_B = -\Delta m c^2 \left(\Delta \bar{\tau}_b - \Delta \bar{\tau}_a\right)/\hbar = -\Delta m \left(1 + \alpha_{\text{e-g}}\right) g \,\Delta z \,(t_{\text{f}} - t_{\text{i}})/\hbar$$

$$\alpha_{\text{e-g}} = \frac{m_1}{\Delta m} \left(\beta_2 - \beta_1\right)$$



Inversion and Bragg diffraction pulses





Suppression of vibration noise



• Suppress *vibration noise* through the *simultaneous* operation of a Rb interferometer:

$$\delta\phi_{\text{laser}} = \delta\bar{\varphi} + \mathbf{k}_{\text{eff}} \cdot \mathbf{g} \left(1 + \beta_1\right) T'(T + T') + \mathbf{k}_{\text{eff}} \cdot \Delta \mathbf{g} \, T'(T + T') - \sum_j \delta \mathbf{k}_{\text{eff}}^{(j)} \cdot \mathbf{X}_{\text{mirror}}(t_j)$$



Suppression of vibration noise



• Suppress *vibration noise* through the *simultaneous* operation of a Rb interferometer:

$$\left(\delta\phi_{A} - \left(\frac{k_{\rm eff}}{k_{\rm eff}^{\rm Rb}}\right)\delta\phi_{\rm Rb}\right) - \left(\delta\phi_{B} - \left(\frac{k_{\rm eff}}{k_{\rm eff}^{\rm Rb}}\right)\delta\phi_{\rm Rb}'\right) = -\Delta m \, c^{2} \left(\Delta\bar{\tau}_{b} - \Delta\bar{\tau}_{a}\right)/\hbar = -\Delta m \left(1 + \alpha_{\rm e-g}\right)g \, \Delta z \, (t_{\rm f} - t_{\rm i})/\hbar$$



Feasible experimental implementation

- Simple atom optics with mild requirements on laser power.
- Suppression of vibration noise through simultaneous Rb interferometer.
- Feasible implementation with VLBAI facility in Hannover.

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Measuring gravitational time dilation with delocalized quantum superpositions

Albert Roura^(D),¹ Christian Schubert,^{2,3} Dennis Schlippert,² and Ernst M. Rasel²



Spacetime curvature and proper-time difference

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- Effect of spacetime curvature on a delocalized wave function.
- Proper-time time difference between the two atom interferometer arms.
- Gravitational analog of the scalar Aharonov-Bohm effect.







Conclusions

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 Measurement of *relativistic effects* in *macroscopically delocalized quantum superpositions* with quantum-clock interferometry.

 Important challenges in *quantum-clock interferometry* and its application to *gravitational-redshift* measurement.

• Promising <u>doubly differential scheme</u> that overcomes them.

• Feasible implementation in facilities soon to become operational.



 If one considers a consistent framework for *parameterizing violations* of Einstein's *equivalence principle*, (e.g. dilaton models)

both for comparison of *independent clocks* and for the above *quantum-clock interferometry* scheme one obtains

$$\frac{\Delta \bar{\tau}_b - \Delta \bar{\tau}_a}{\Delta \bar{\tau}_a} \approx (1 + \alpha_{\text{e-g}}) \Big(U(\mathbf{x}_b) - U(\mathbf{x}_a) \Big) / c^2 \qquad \alpha_{\text{e-g}} = \frac{m_1}{\Delta m} \big(\beta_2 - \beta_1 \big)$$

test of universality of gravitational redshift with delocalized quantum superpositions



SCIENCE ADVANCES | RESEARCH ARTICLE

PHYSICS

Interference of clocks: A quantum twin paradox

Sina Loriani¹*, Alexander Friedrich²*[†], Christian Ufrecht², Fabio Di Pumpo², Stephan Kleinert², Sven Abend¹, Naceur Gaaloul¹, Christian Meiners¹, Christian Schubert¹, Dorothee Tell¹, Étienne Wodey¹, Magdalena Zych³, Wolfgang Ertmer¹, Albert Roura², Dennis Schlippert¹, Wolfgang P. Schleich^{2,4,5}, Ernst M. Rasel¹, Enno Giese²

Loriani et al., Sci. Adv. 2019; 5: eaax8966 4 October 2019





Other current activities

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Q-GRAV Project



Interface of Quantum Mechanics and Gravitation

• Main Topics:

- 1. Atom interferometry
- 2. Matter-wave lensing for cold atoms
- 3. Relativistic quantum information

Team members:







Nico Schwersenz



Albert Roura

Q-GRAV Project



Interface of Quantum Mechanics and Gravitation

- Main Topics:
- 1. Atom interferometry
- 2. Matter-wave lensing for cold atoms
- 3. Relativistic quantum information
- Highlighted international collaborations:
 - Atom interferometry experiments on the ISS with NASA's Cold Atom Lab (CAL)
 NASA JPL + Consortium for Ultracold Atoms in Space
 - NASA's Science Definition Team for DSQL Mission Concept and follow-up activities Recognized with a NASA Group Achievement Award

ESA-related activities



- ACES Mission (launch in 01/2025)
 - high-precision measurements with cold atoms in space
 - tests of general relativity, relativistic geodesy, intercontinental time / frequency distribution
 - ACES Workshop 2023 organized in Ulm.

AIRBUS CONSISTENT OF CONSISTE

• Co-Chair of ESA's *Physical Sciences Working Group* (PSWG).

Member of ESA's Space Science Advisory Committee (SSAC).





Thank you for your attention.

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Q-SENSE European Union H2020 RISE Project







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Atom interferometry

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Atom interferometers as accelerometers

