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Key Points:
• The injection of N2O by sprites seems to be not enough to account for the disagreement between satellite observations and simulations.
• We have calculated the radial dependence of the production of NO and N2O by a single sprite streamer in the mesosphere.
• The characteristics of the LBH band emitted by sprites prevent the estimation of the event altitude from space-based photometric recordings.

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Citation:

Abstract
Sprites are mesospheric filamentary discharges that liberate and accelerate large quantities of electrons. They produce local enhancements of some chemical species and fast (milliseconds) optical emissions. In this work, we couple a self-consistent 2-D model of sprites with an extensive chemical scheme to calculate the injection of chemical species by one sprite streamer in the mesosphere 0.85 ms after its onset. The N, NO, and N2O injections per streamer are about 10^{21} atoms, 6 \times 10^{19} molecules, and 10^{18} molecules, respectively. According to our results, longer simulations are necessary to determine the role of sprites in the concentration of N2O in the mesosphere. We also calculate the contribution of sprite glows to space-based photometers of the Atmosphere-Space Interactions Monitor and the Tool for the Analysis of RAdiations from lightNIngs and Sprites.

1. Introduction
Sprites are a type of transient luminous event (TLE) with a characteristic time of few milliseconds taking place in the range of altitudes between 40 and 90 km above thunderstorms (e.g., Franz et al., 1990; Pasko et al., 1997, 2012; Stenbaek-Nielsen et al., 2009, 3829). They are formed by fast-propagating bright plasma filaments known as streamers (Pasko et al., 1998; Raizer et al., 1998) followed by long-standing (1–100 ms) luminous structures called beads and glows (Liu, 2010; Luque & Gordillo-Vázquez, 2011; Luque et al., 2016). Since their discovery in 1989, several authors have investigated the chemical influence of sprites in the mesosphere using zero- and one-dimensional models (e.g., Evtushenko et al., 2013; Gordillo-Vázquez, 2008, 2010, 2012; Parra-Rojas et al., 2015; Sentman et al., 2008; Winkler & Nothold, 2014). They reported a significant production of NO in the center of sprite streamers due to the oxidation of atomic nitrogen produced by electron-impact processes. Sentman et al. (2008) assumed a streamer nominal diameter of 25 m and a vertical length of 10 km to estimate a production of 5 \times 10^{19} molecules of NO per streamer between altitudes 65 and 75 km. In the stratosphere, NO_x produced by lightning contributes to ozone depletion (Cruzen, 1979; Schumann & Huntrieser, 2007), while its concentration in the mesosphere is very low. Enell et al. (2008) estimated a production of 3 \times 10^{22}–3 \times 10^{23} molecules of NO per sprite. Armone et al. (2014) used these estimated NO_x production to calculate, using the Whole Atmosphere Community Climate Model version 4 (WACCM4), the global and regional sprite-induced variations in the concentration of NO_x. They found that the perturbation in the tropical concentration of nitrogen oxide by sprite streamers could lie between 0.015 and 0.15 ppbv. These quantities correspond to a perturbation of the background concentration of NO_x between less than 1% and up to 20%. Rodger et al. (2008), Armone et al. (2008), Armone et al. (2009), and Armone and Dinelli (2016) reported NO_{x} over thunderstorms through satellite observations. They concluded that sprite-NO_{x} is at the edge of detectability with current instruments.

The third strongest greenhouse gas after CO_{2} and CH_{4} is N_{2}O, having a global-warming potential (GWP) of almost 300 over 100 years and being an important ozone depleting species (Davidson, 2009). The most important source of N_{2}O in the atmosphere is from surface emissions (Davidson, 2009). However, Sheese et al. (2016) reported the existence of an atmospheric source of N_{2}O based on observations from the satellite instrument “Atmospheric Chemistry Experiment-Fourier Transform Spectrometer” (ACE-FTS). They proposed energetic particle precipitation in the lower thermosphere as the main N_{2}O atmospheric source. Kelly et al. (2018) included the production of N_{2}O via N_{2}(A^{3}Σ_u^{+}) + O_{2} in the mesosphere-lower thermosphere (MLT) in...
Blue Jets could contribute to about 38% of the N2O between 20 and 40 km. Previously, Gordillo et al. suggested the lower stratosphere. Based on results by Winkler and Nothold (2015), Pérez-Invernón et al. (2008) and Parra et al. (2015) had found an important production of N2O in sprites due to the chemical reaction N2 + O→ e + N2O with the concentration of O− being previously increased, with respect to background values, due to the action of sprite streamers (Luque & Gordillo-Vázquez, 2012). According to Parra-Rojas et al. (2015), the production of NO and N2O could spread down to 50 km altitude (Parra-Rojas et al., 2015). In particular, the density enhancement of N2O molecules due to the streamer channel (scale of seconds) between 50 and 60 km altitudes could be up to 2 orders of magnitude above the background value. There are no global measurements nor estimations on the global chemical impact of sprites in the concentration of N2O in the mesosphere. However, modeling results by Gordillo-Vázquez (2008) and Parra-Rojas et al. (2015) suggest that sprites could contribute to the global concentration of N2O in the mesosphere, specially over middle and low latitudes where sprites are more frequent (Chen et al., 2008).

According to computational models of streamers, laboratory experiments, and optical measurements, sprites emit light predominantly in the first and second positive systems of the molecular neutral nitrogen (1PS N₂ and the 2PS N₂, or simply FPS and SPS), the first negative system of the molecular nitrogen ion (N²⁻: 1NS or simply FNS), the Meinel band of the molecular nitrogen ion (Meinel N²⁻), and the Lyman-Birge-Hopfield (LBH) band of the molecular neutral nitrogen (e.g., Armstrong et al., 1998; Gordillo-Vázquez et al., 2018; Kanmae et al., 2007; Kuo et al., 2005b; Sato et al., 2015; Stenbaek-Nielsen et al., 2007). Some authors have proposed the use of the ratios FNS to SPS and FPS to SPS to estimate the peak electric field in air discharges (Adachi et al., 2006; Bonaventura et al., 2011; Celestin & Pasko, 2010; Hoder, 2016; Hoder et al., 2012; Kim et al., 2003; Kozlov et al., 2001; Kuo et al., 2005a, 2009, 2013; Liu et al., 2006; Morrill et al., 2002; Paris et al., 2004, 2005; Pasko, 2010; Pérez-Invernón et al., 2018; Shcherbakov & Sigmond, 2007; Šimek, 2014). Recently, Ihaddadene and Celestin (2017) proposed the measurement of the ratio of the SPS to the LBH band as a possible method to estimate the sprite streamer altitude from space-based photometers, such as the Atmosphere-Space Interactions Monitor (ASIM) (Chanrion et al., 2019; Neubert et al., 2019) and the Tool for the Analysis of RAdiations from lightNIngs and Sprites (TARANIS) (Lefeuvre et al., 2008). According to the spatial non-uniformity of streamers, Malagón-Romero et al. (2019) introduced two new methods to estimate the peak electric field in streamer heads.

Recently, Ono and Komuro (2019) validated the use of 2-D self-consistent streamer models to simulate the chemical influence of streamers in air. They compared the simulated enhancement of ozone produced by one streamer at atmospheric pressure with laser spectroscopy measurements. In this work we couple an extensive kinetic model of 131 species interacting through 952 chemical reactions with a 2-D self-consistent sprite streamer electrodynamical model. This 2-D approach allows us to self-consistently calculate the chemical influence of a single sprite streamer between the altitudes 68 and 75 km. The implemented vibrational and electronical kinetics of N₂ enable us to calculate the contribution of single sprite streamers to the photometers of ASIM and TARANIS. According to our results, optical emissions produced in the glow emerging in the streamer channel prevent the estimation of the sprite streamer head altitude from space-based photometers.

### 2. Streamer Model

To study the propagation of a sprite streamer and the latter evolution of the channel, we use a 2-D cylindrically symmetric model. We describe the time evolution of the electron density ne and ion densities ni with the drift-diffusion-reaction equations coupled to Poisson’s equation as follows:

\[
\frac{\partial n_e}{\partial t} = C_e + \nabla \cdot (n_e \mu_e F_e) + D_e \nabla n_e + S_{pb}, \tag{1a}
\]

\[
\frac{\partial n_i}{\partial t} = C_i + S_{pb} \delta_{O^{-},i}, \tag{1b}
\]
et al. (2018); that is, we set the air density properties of the atmosphere the chemical properties of the atmosphere as initial state of the atmosphere the chemical properties of the atmosphere. We use the software QtPlaskin, developed by Luque (2011), to analyze the main chemical processes that contribute to the concentration of each chemical species as a function of time in our simulation. We use the local field approximation, and, consequently, transport coefficients are derived from the electron energy distribution function (EEDF) that only depends on the local electric field. The symbol \( \delta \) is the Kronecker delta, and \( S_{ph} \) is the photoionization term that only applies to electrons and \( O_{2}^{+} \). As for Poisson’s Equation 1c, \( \phi \) is the electrostatic potential, the sum extends over all the charged species \( s \), \( q_{j} \) is the charge of the species \( s \), with \( s \) running over ions as well as electrons, and \( \epsilon_{0} \) is the vacuum permittivity.

Finite volume methods coupled to hyperbolic methods are suitable to solve the set of Equations 1a and 1b. To solve these equations we have used CLAWPACK/PETCLAW (Alghamdi et al., 2011; Clawpack Development Team, 2017; LeVeque, 2002). PETCLAW is built upon PETSc (Balay et al., 2016b, 2016a) and allows us to split the simulation domain into different subdomains (problems) that can be solved in parallel. Poisson’s equation is solved using the generalized minimal residual method and the geometric algebraic multigrid preconditioner, both from the PETSc numerical library.

We consider that the streamer is completely formed between altitudes 74.82 and 68 km, and we calculate its chemical influence and optical emissions in this range of altitudes. This approach allows us to ensure that the seed does not excessively influence our results.

### 2.1. Chemical Model

We use a modified version of the set of chemical reactions for halos and elves collected in the Appendix of Pérez-Invernón et al. (2016a), based on sprite and halo models developed by previous studies (Gordillo-Vázquez, 2008, 2010; Parra-Rojas et al., 2013, 2015). In addition, the chemical reactions of the 2-D model of streamers developed by Malagón-ROMERO and Luque (2018) are added to the model. As sprite streamers take place in the upper mesosphere where the concentration of water is negligible, we do not include chemical reactions involving water in our simulation. Vibrational chemistry of CO2 is not considered in this study. This vibrational and electronic chemical model allows us to calculate the temporal evolution of the density of \( N_{2}(\delta^{3} \Pi_{g}, v = 0, ..., 6) \), \( N_{2}(C^{3} \Pi_{u}, v = 0, ..., 4) \), and \( N_{2}(a^{1} \Pi_{g}, v = 0, ..., 15) \). Therefore, we can calculate the temporal evolution of the contribution of single sprite streamers to ASIM photometers (PH1: 337 ± 2.5 nm from the SPS, PH2: 180–230 nm from the LBH band) sampling at 100 kHz (Chanrion et al., 2019; Neubert et al., 2019) and TARANIS photometers (PH1: 337 ± 5 nm from the SPS, PH2: 145–280 nm from the LBH band, PH3: 757–765 nm from the FPS, PH4: 600–800 nm from the FPS) sampling at 20 kHz (Lefeuvre et al., 2008).

We use the software QtPlaskin, developed by Luque (2011), to analyze the main chemical processes that contribute to the concentration of each chemical species as a function of time in our simulation.

### 2.2. Initial and Boundary Conditions

Sprites are high-altitude discharges made of many streamers that propagate through a varying air density. In our model, we have set as initial state of the atmosphere the chemical profiles of Figure 1 of Pérez-Invernón et al. (2018); that is, we set the air density profile and composition at nighttime conditions in November from the Whole Atmosphere Community Climate Model (WACCM) (Marsh et al., 2013) for a latitude of 38° and a longitude of 0° relaxed for 6.5 s under the presence of cosmic ray ionization (Thomas, 1974). The concentration of N is negligible, and the humidity is set to zero (dry air conditions). We also set a background electron density following the Wait-Spies profile (Hu et al., 2007) that is neutralized by an identical density of positive ions:

\[
\begin{align*}
    n_{e, bg} &= (10^{4} \text{ m}^{-3}) \times e^{-\left(\frac{r}{2.86 \text{ km}}\right)},
\end{align*}
\]

In order to start the streamer we set a gaussian seed with an e-folding radius of 40 m and a peak density of \( 5 \times 10^{10} \text{ m}^{-3} \). This initial electron density is neutralized by an identical density of positive ions. In order to
solve Poisson’s equation we impose Dirichlet boundary conditions at $z = z_{\text{min}}$ and free boundary conditions at $r = r_{\text{max}} = 600$ m and $z = z_{\text{max}}$ according to the method described by Malagón-Romero and Luque (2018). These free boundary conditions are consistent with the density charge inside the domain and with a potential decaying far away from the source.

We have simulated a positive streamer propagating in a background electric field of 100 V/m, which correspond to 120 Td at 74.23 km. The simulated domain extends from 67 to 75 km in the vertical direction, and the grid resolution is 1 m.

3. Results and Discussion

3.1. Chemical Influence of Sprite Streamers in the MLT

Figures 1a–1g show the most significant density enhancements of the selected chemical species produced in the central axis of a simulated streamer. The species production is integrated during 0.85 ms, a time in which the streamer tip advances from 74.82 to 67 km of altitude. The streamer head reaches the altitude 73 km at time 0.45 ms. The density of the streamer tip advances from 74.82 to 67 km of altitude. Figure 1h shows the rates of production and losses of some species at 73 km of altitude. The streamer head reaches the altitude 73 km at time 0.45 ms. The density of the emitting species $N_2(C^3\Pi_m, v = 0)$ (Figure 1g) shows a glow emerging between $z = 74$ km and $z = 72$ km.

The main production of $N_2O$ takes place in the streamer channel region where the glow emerges (see Figure 1), while the densities of $e$, $O$, $N$, and $NO$ are significantly perturbed in both the streamer head and the streamer channel. The obtained perturbation in the concentration of $O_3$ is 7 orders of magnitude lower than the background value (Pérez-Invernón et al., 2018). The high electric field in the head and channel of the streamer accelerates electrons, producing a high concentration of $O\cdot$, $N_2(A^3\Sigma_u^+)$, and other chemical species due to direct electron-impact ionization, excitation, and dissociation and electron detachment processes (Luque & Gordillo-Vázquez, 2012).

The main production mechanism of $N_2O$ is the electron detachment process $N_2 + O \rightarrow e + N_2O$. The production rate of $N_2O$ by the chemical process $N_2(A^3\Sigma_u^+, v = 0) + O_2 \rightarrow O + N_2O$ is 1 order of magnitude lower than the production of $N_2O$ by electron detachment. The most significant removal of $N_2O$ occurs in the streamer head, through ionization of $N_2O$ by electron impact, while the $N_2O$ losses in the streamer channel are dominated by the chemical reactions $e + N_2O \rightarrow N_2 + O\cdot$, $O\cdot + N_2O \rightarrow NO^- + NO$, and $N_2(A^3\Sigma_u^+, v = 0) + N_2O \rightarrow N_2 + N + NO$. We have obtained an increase in the concentration of $N_2O$ between 75 and 68 km during 0.85 ms 1 order of magnitude lower than the increase reported by Parra-Rojas et al. (2015) for 1 ms using a 0-D model.

The production of NO is dominated by the chemical reactions $O_2 + N(^2D) \rightarrow NO + O$ and $O_2 + N(^2P) \rightarrow NO + O$. Main losses of NO are due to ionization by electron impact in the streamer head and by the chemical reactions $NO + N(^2D) \rightarrow N_2 + O$ and $NO + N_2(A^3\Sigma_u^+, v = 0) \rightarrow N_2 + NO(A^2\Sigma^+)$ in the streamer channel. Processes involving $N_2^+$ and $O_2^+$ represent secondary mechanisms for the loss of NO.

Dvorak et al. (2019) recently measured in laboratory experiments a density enhancement of $N$ inside the streamer channel. They proposed electron-ion dissociative recombination processes as the main mechanism producing an enhancement of $N$ in the streamer channel. According to our results, the production of $N$ by direct electron-impact dissociation of $N_2$ driven by the electric field in the streamer channel is 4 orders of magnitude above the production of $N$ by electron-ion dissociative recombination processes. This apparent disagreement could be due to a lower importance of recombination processes at low density than at atmospheric conditions. In addition, the characteristic time of recombination processes is larger than the time simulated. The density of $O_3$ is reduced in the streamer channel due to the electron attachment process $e^- + O_3 \rightarrow O^- + O_2$. For a more detailed discussion of the main chemical mechanisms involved in this simulation, we refer to Parra-Rojas et al. (2015) and Pérez-Invernón et al. (2018).

In Figure 2 we show the vertically and horizontally integrated radial density enhancement of some chemical species produced by a simulated sprite streamer 0.85 ms after its onset. This figure shows for the first time the radial dependence of the production of NO and $N_2O$ by a sprite streamer. The production of chemical species in the simulated streamer decays radially around 2 orders of magnitude between the center of the streamer and 400 m. The production of $N$, $NO$, and electrons increases during the downward propagation of the streamer head. The maximum production of $N_2O$ takes place in the glow (above 72 km).
Figure 1. (a–g) Density enhancement with respect to background of different chemical species produced by a simulated sprite streamer 0.85 ms after its onset between altitudes 68 and 74.82 km. (h) Temporal evolution of the rates of production (P) and losses (L) of the species plotted in panels (a)–(f) at the position $z = 73$ km, $r = 0$ km.
In Table 1 we show the most important productions of atoms and molecules in the mesosphere by a sprite streamer 0.85 ms after its onset in a cylindrical volume with a radius of 0.45 km and altitudes ranging from 67 up to 74.82 km. Computational limitations of this self-consistent electrodynamical model do not allow us to extend the simulation to longer times. We obtain streamer diameters of hundreds of meters, in agreement with previous observation (Cummer et al., 2006; Stenbaek-Nielsen et al., 2013) and modeling results (Luque & Ebert, 2009) of sprite streamers before bifurcation. We have obtained an injection of $5.9 \times 10^{19}$ NO molecules per sprite streamer, consistent with the production of $5 \times 10^{19}$ NO reported by Sentman et al. (2008) using a zero-dimensional model. The ratio of produced O atoms to NO molecules is about 5 in agreement with Sentman et al. (2008). According to our calculations, a sprite streamer could produce about $10^{18}$ N$_2$O molecules between 68 and 74.82 km.

Let us now estimate the chemical influence of a sprite composed by several streamers in the MLT using measured optical signatures of sprites. Armstrong et al. (1998) reported the maximum brightness of a complete sprite to be about 150 kR using a ground-based photometer covering 6° of field of view (FOV), centered at 399.4 nm, and sampling at 750 Hz. The wavelength of the SPS that contributes to this photometer is 399.7 nm (Gilmore, 1992). The maximum brightness is reached in the first millisecond. In addition, Figure 5 of Armstrong et al. (1998) shows that the FOV of the photometer covers a significant part of the sprite. Therefore, we can compare the maximum brightness reported by these authors with the maximum brightness of the complete sprite in the total simulated time 0.85 ms. We use the density of N$_2$(C$^3\Pi_u$, $\nu$=0) in our simulated single streamer, the atmospheric absorption calculated using the software MODTRANS 5 (Berk et al., 2005) between the sprite and the observer, and the system response of the photometer employed by Armstrong.

### Table 1

<table>
<thead>
<tr>
<th>Species</th>
<th>Total number of produced atoms/molecules</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>$9.7 \times 10^{20}$</td>
</tr>
<tr>
<td>O</td>
<td>$2.7 \times 10^{20}$</td>
</tr>
<tr>
<td>NO</td>
<td>$5.9 \times 10^{19}$</td>
</tr>
<tr>
<td>N$_2$O</td>
<td>$1.2 \times 10^{18}$</td>
</tr>
<tr>
<td>O$_3$</td>
<td>$-1.8 \times 10^{16}$</td>
</tr>
<tr>
<td>CO</td>
<td>$-3.1 \times 10^{15}$</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>$3.1 \times 10^{15}$</td>
</tr>
</tbody>
</table>

**Figure 2.** Vertically (upper panel) and horizontally (lower panel) integrated radial density enhancement of some chemical species produced by a simulated sprite streamer 0.85 ms after its onset between altitudes 68 and 74.82 km.
et al. (1998) to estimate the optical signature, obtaining a maximum brightness of 3 kR. Therefore, the simulated brightness of a streamer is about 50 times less than the reported optical emissions of a complete sprite.

On the other hand, the Global Lightning and Sprite Measurements on Japanese Experiment Module (JEM-GLIMS) reported absolute peak intensity of a complete sprite of about $3 \times 10^{-6} \text{ W/m}^2$ with a photometer sampling at 20 kHz in a range of wavelengths between 150 and 280 nm at 410 km altitude (Sato et al., 2016). We use the density of $N_2(a^1\Pi_g, v=0, \ldots, 5)$ in our simulated streamer to estimate the optical signature in the photometer of JEM-GLIMS, obtaining a peak intensity of $1.6 \times 10^{-7} \text{ W/m}^2$. Therefore, we can assume that a complete sprite would produce between 18 and 50 times more optical emissions and production of chemical species than the simulated single streamer. We will use factor 18, which is calculated from space-based measurements that are not significantly influenced by the absorption of the atmosphere.

Figure 3. Temporal evolution of (a) the altitude of the streamer head, (b) the maximum electric field in the streamer head, (c) the ratio of the contributions of the simulated sprite streamer optical emissions to the photometers of ASIM (PH1: 337 ± 2.5 nm, PH2: 180–230 nm) and TARANIS (PH1: 337 ± 5 nm, PH2: 145–280 nm, PH3: 757–765 nm, PH4: 600–800 nm), and (d) the VDF of $N_2(a^1\Pi_g, v=0, \ldots, 5)$. 

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We have compared the maximum brightness of simulated and reported sprites in the first millisecond after their onset to estimate the production of chemical species by a complete sprite in about 1 ms. During this time, the streamers travel about 7 km downward. According to this comparison, a complete sprite would produce about $2 \times 10^{19}$ molecules of N$_2$O and $10^{21}$ molecules of NO between about 68 and 75 km. Assuming a global sprite occurrence of 0.5 per minute (Chen et al., 2008), sprites could inject about $10^{25}$ N$_2$O and $10^{27}$ NO molecules in the MLT annually. Since the average concentration of N$_2$O in the MLT is about 1 ppbv (Kelly et al., 2018; Sheese et al., 2016), the total number of molecules of N$_2$O contained between 68 and 75 km is about $3 \times 10^{30}$. Therefore, the injection of N$_2$O molecules by sprites would contribute to the altitude-height profiles of N$_2$O measured by ACE-FTS (Kelly et al., 2018; Sheese et al., 2016) by less than 0.003% of the total population per year for a sprite simulation up to 0.85 ms. Hence, the chemical effect of sprite seems to be not enough to explain the disagreement between the concentration of N$_2$O in the MLT over middle and low latitudes measured by ACE-FTS (Sheese et al., 2016) and concentrations simulated by using WACCM4 (Kelly et al., 2018).

Our results correspond, however, to a simulation of 0.85 ms. The present computational capabilities do not allow more extensive spatiotemporal simulations with 2-D models. This means that we are only reporting the complete chemical influence of a sprite streamer head between altitudes 68 and 74.82 km and the influence of the first millisecond evolution of the streamer channel and the glow. The production of N$_2$O and NO in the glow is still active at the end of the simulation. However, the 0-D simulation by Parra-Rojas et al. (2015) shows that the chemical influence of one sprite between 68 and 74.82 km altitudes would not significantly change between 0.85 ms and 100 s after the onset of the sprite streamer (see Figures 8 and 15 of Parra-Rojas et al., 2015).

### 3.2. Optical Signature From Space-Based Photometers

Our chemical model incorporates all mechanisms that influence the population of excited species that emit observable radiation. Figure 3 shows an analysis of the contribution of a simulated sprite streamer optical signature to the photometers of ASIM and TARANIS. We plot in the first and second panels of Figure 3 the altitude and maximum electric field of the downward propagating streamer head, respectively. The third panel of Figure 3 shows the ratio of the contributions of the simulated sprite streamer optical emissions to the different photometers of ASIM and TARANIS. Comparison of the three uppermost panels of Figure 3 shows that the photometer ratios do not provide information about the altitude of the streamer head. This is due to the significant contribution of the glow discharge to the total optical emissions of the sprite streamer. In addition, the temporal evolution of the vibrational distribution function (VDF) of the most populated vibrational states of N$_2$(a$^1\Pi_g$, v) (Kirillov, 2011) showed in the fourth panel of Figure 3 is not constant during the temporal evolution of the simulated sprite streamer. The transient behavior of the N$_2$(a$^1\Pi_g$, v) VDF is influenced by the radiative decay of the electronically excited N$_2$(w$^3\Delta_u$, v) to N$_2$(a$^1\Pi_g$, v = 0)—with a characteristic time of 0.6 ms (Gilmore, 1992)—within the streamer channel. This cascading process breaks the assumption of a constant VDF of the N$_2$(a$^1\Pi_g$, v) levels, which is required to calculate the contribution of the LBH into the photometer band and to estimate the altitude of the streamer head (Pérez-Invernón et al., 2018).

### 4. Summary and Conclusions

We have calculated the chemical influence and optical emissions of a sprite streamer at altitudes between 68 and 74.82 km and during 0.85 ms using a self-consistent 2-D model coupled with a kinetic scheme of 131 species interacting through 952 chemical reactions. Our results suggest that the injection of N$_2$O by sprites in the MLT over midlatitudes and low latitudes is not enough to account for the disagreement between satellite observations and simulations. Future improvements in computational capabilities will allow more extensive spatiotemporal simulations to confirm this conclusion. The obtained injection of NO, N, and O molecules is in agreement with previous results based on 0-D and 1-D models. We have also estimated the contribution of the optical emissions of a simulated sprite streamer to the photometers of ASIM and TARANIS, concluding that the altitude of the streamer head cannot be estimated from space-based optical measurements operating at nadir.

The main conclusions of this work are as follows:
1. Single non-bifurcated sprite streams can inject $9.7 \times 10^{39}$ atoms of N, $5.9 \times 10^{19}$ molecules of NO, and $1.2 \times 10^{14}$ molecules of N$_2$O between the altitudes 68 and 74.82 km during 0.85 ms after its onset.

2. We have calculated for the first time the radial dependence of the production of NO and N$_2$O by a single sprite streamer.

3. We have estimated the contribution of the sprite streamer optical signature to the ratio between optical signals recorded by different photometric recordings of ASIM and TARANIS.

4. According to our model, the LBH band optical emissions from the glow and the transient $N_2(a^2\Pi_g, v)$ VDF influenced by the radiative decay of $N_2(w^2\Delta_u, v)$ to $N_2(a^2\Pi_g, v=0)$ prevent the estimation of the sprite streamer head altitude from space-based photometric recordings.

**Data Availability Statement**

Data presented here are available at the IAA repository (https://cloud.iaa.csic.es/public.php?service=file&c=c8t=cb269d94561e81c1cdd5066157fd86f0). The code developed for the simulation of sprite streamers is available at the repository (https://gitlab.com/amaro/streamer2d).

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