

Lidar Design Study for Turbulence Sensing from Ground into the Free Atmosphere Based on Angle-of-Arrival Fluctuation Analysis

Quantifying turbulent processes

- Exchange processes
- Gravity wave dissipation
- Clear Air Turbulence → aviation application
- Other applications: astronomy, laser comm., HEL

Requirements + boundary conditions:

- Parameters: ε (TKE, ε_{kin} , C_v^2), $u'/v'/w'$ or $\langle v'^2 \rangle = \sigma_v^2$, ε_{pot} (T' , C_T^2), scales L_0
- "Free atmosphere" → free troposphere + UTLS
- Temporal + local intermittency
- Blini: high spatial resolution ($< x \cdot 100m$), adv. over radar
- Advection: high temporal resolution ($< 1-3min$)
- Availability night/day

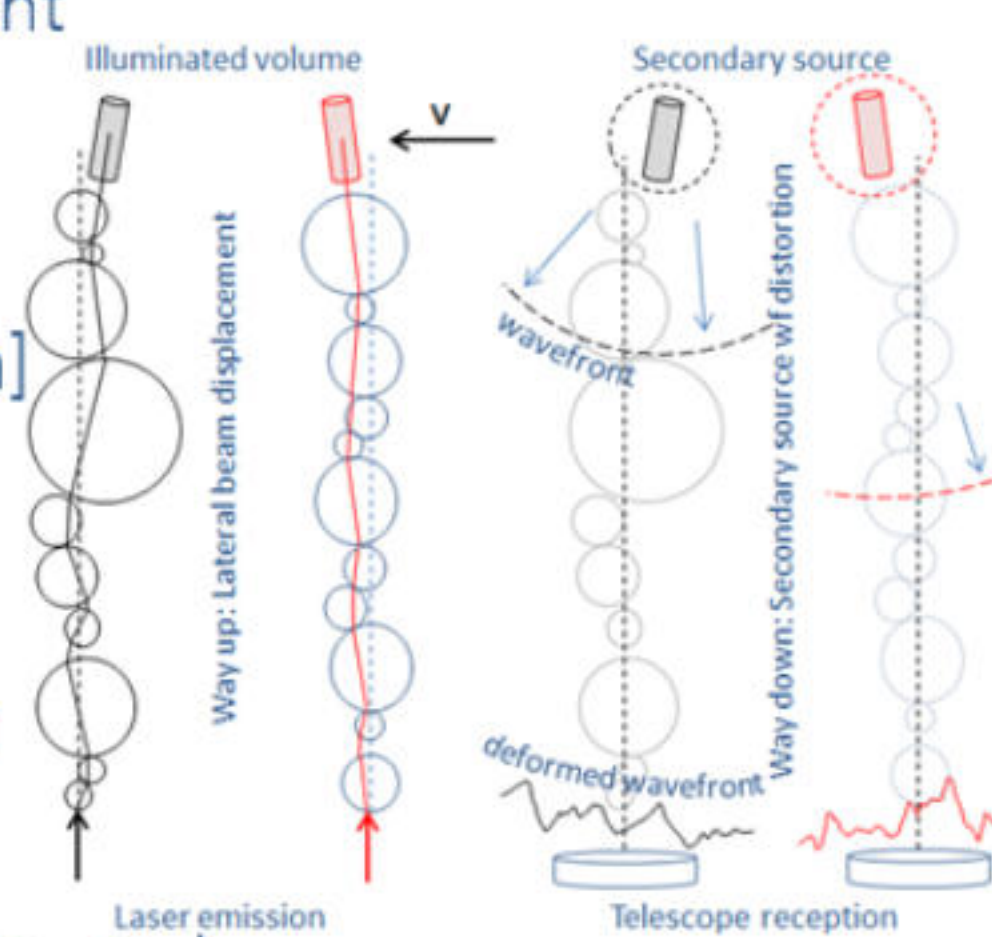
Cn² - Structure constant

Doppler Wind Lidar insufficient

→ take C_n^2 as proxy, use optical turbulence itself

- BSA backscatter amplif. [Banakh, Razenkov, Gurvich]
- Image jitter [Belen'kii, Gimmetstad]

- Angle-of-Arrival fluctuation [Zilberman, Kopeika]

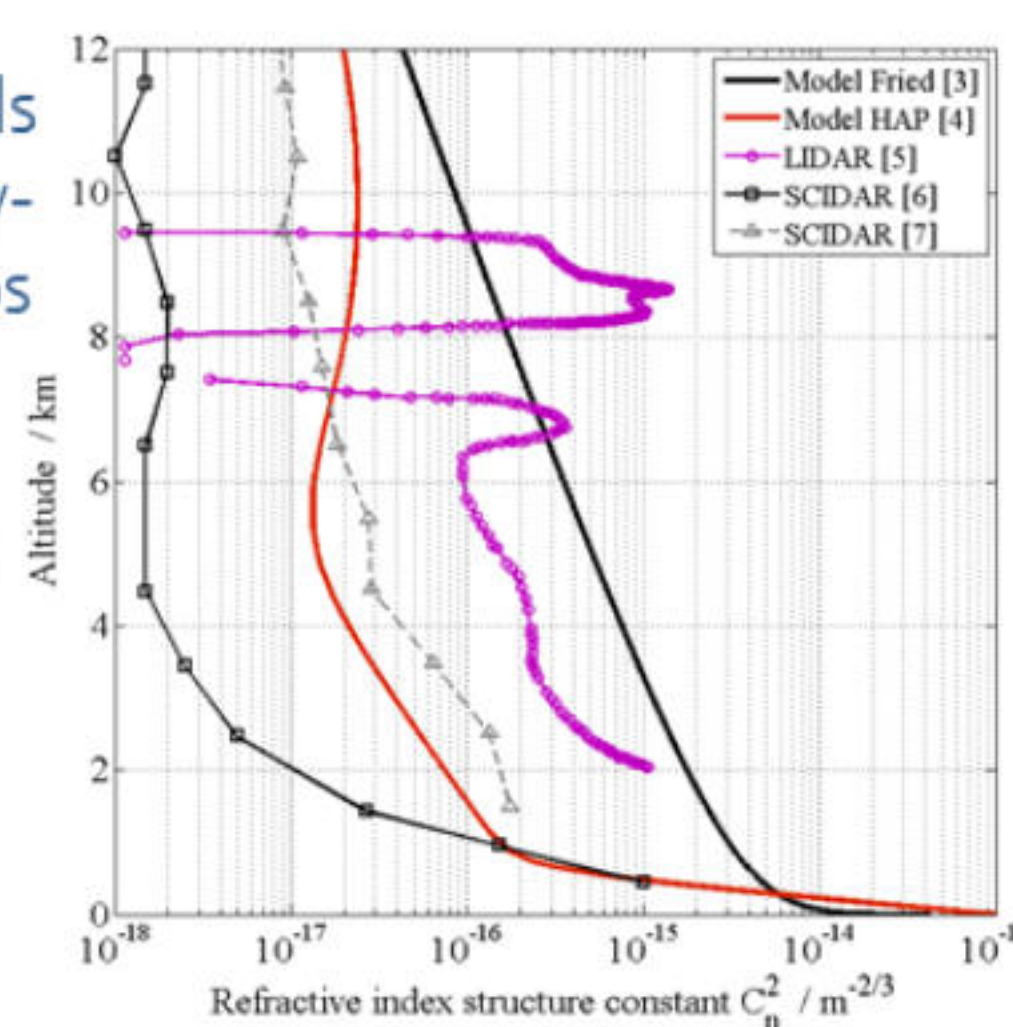


$$\langle \varphi_{AA}^2 \rangle = \langle \varphi_{LB}^2 \rangle + \langle \varphi_{SS}^2 \rangle - 2 \langle \varphi_{LB} \varphi_{SS} \rangle$$

AA = Angle of Arrival, LB = Lateral Beam centroid displacement, SS = Secondary Source, and mutual correlation

C_n² - magnitude: Models, measure

- Non-parametric models
- Fried, ...
- Parametric models
- Hufnagel-Valley-Andrews-Phillips
- Measurements
- Lidar
- SCIDAR (astro.)

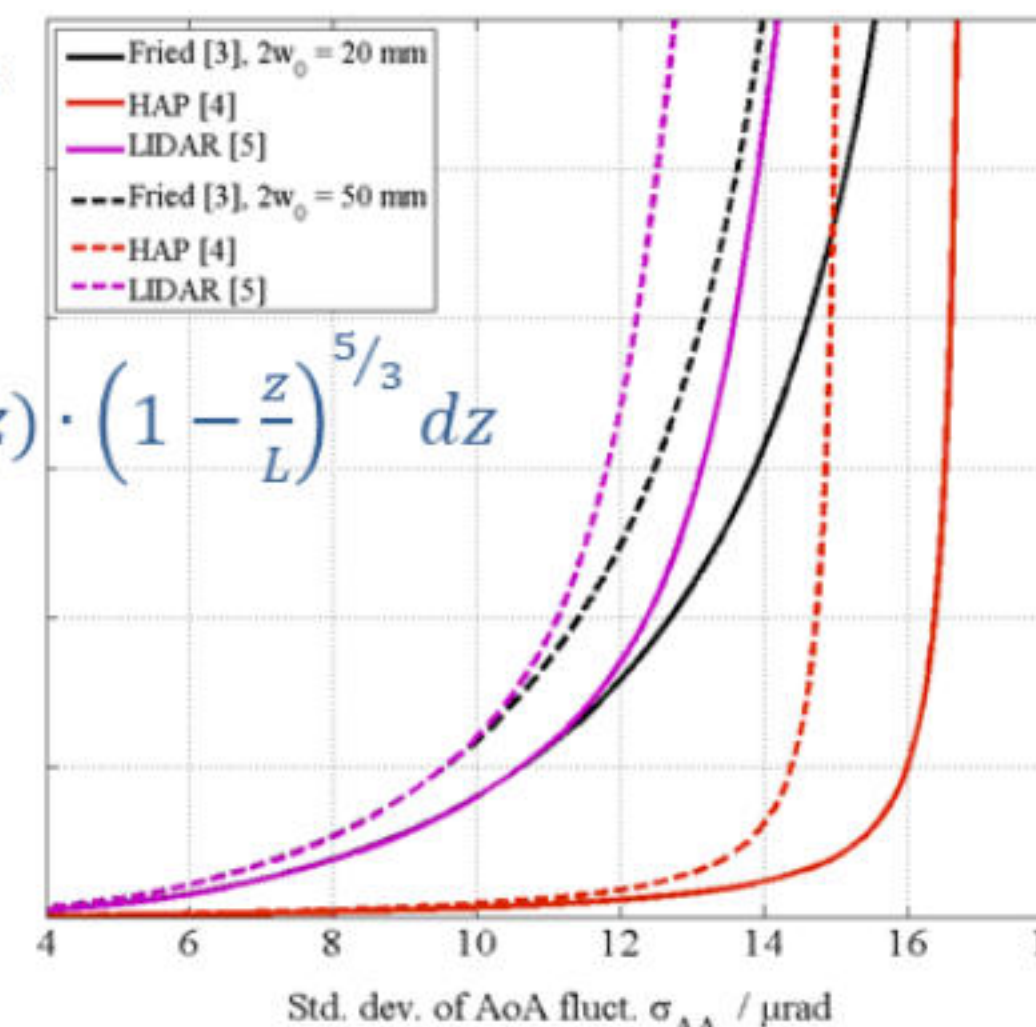


Expected AoA fluctuation $\langle \varphi_{AA}^2(h) \rangle$

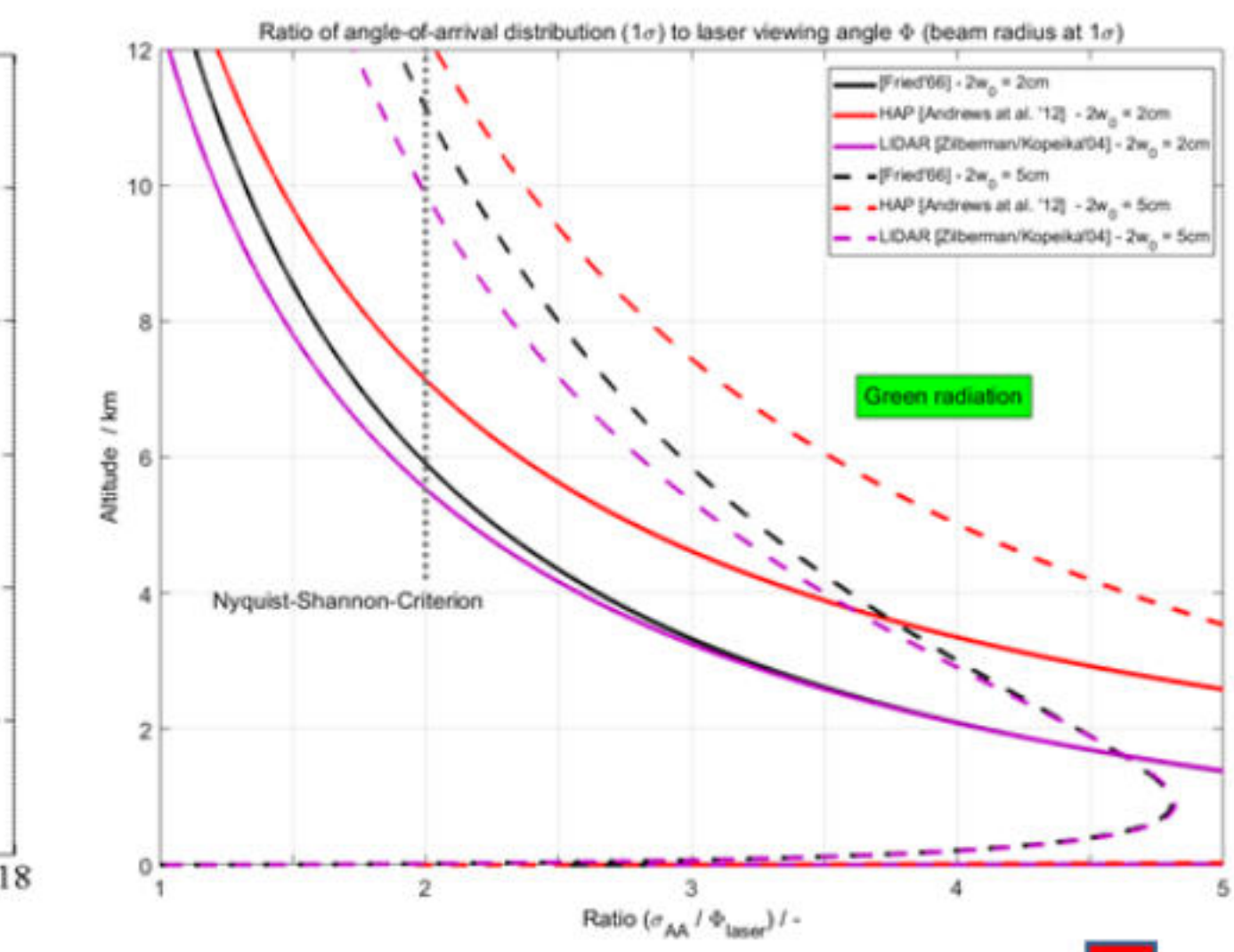
- Based on [ZK'08]
- C_n^2 -profiles
- Prefactor → optimisation / trade-off
- w_0 : Laser beam $\emptyset$
- D : telescope $\emptyset$

$$\langle \varphi_{AA}^2 \rangle = \left(\frac{4.07}{w_0^{1/3}} + \frac{5.65}{D^{1/3}} \right) \cdot \int_0^L C_n^2(z) \cdot \left(1 - \frac{z}{L} \right)^{5/3} dz$$

- Competing requirements
- $\langle \varphi_{AA}^2 \rangle \uparrow$ with $a_0 \downarrow$
- Diff. divergence: $\varphi(h) \uparrow$ with $a_0 \downarrow$
- Turb. beam spread: $\varphi(h) \downarrow$ with $a_0 \downarrow$



Laser spot viewing angle $\Phi(h)$

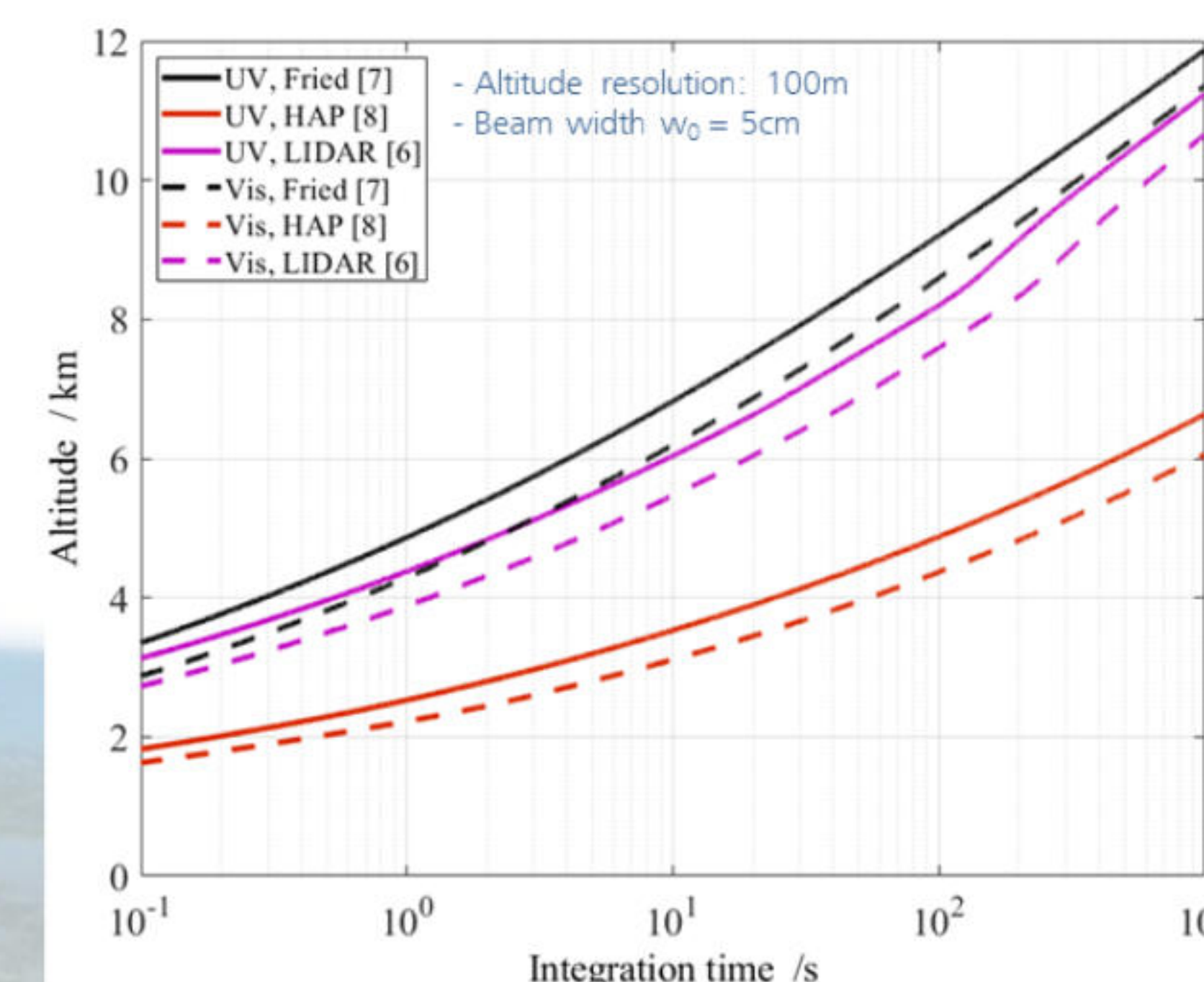


Possible performance in terms of resolution

- Averaging times with Poisson noise process $SNR_{\Sigma} \propto \sqrt{N_{\Sigma}}$

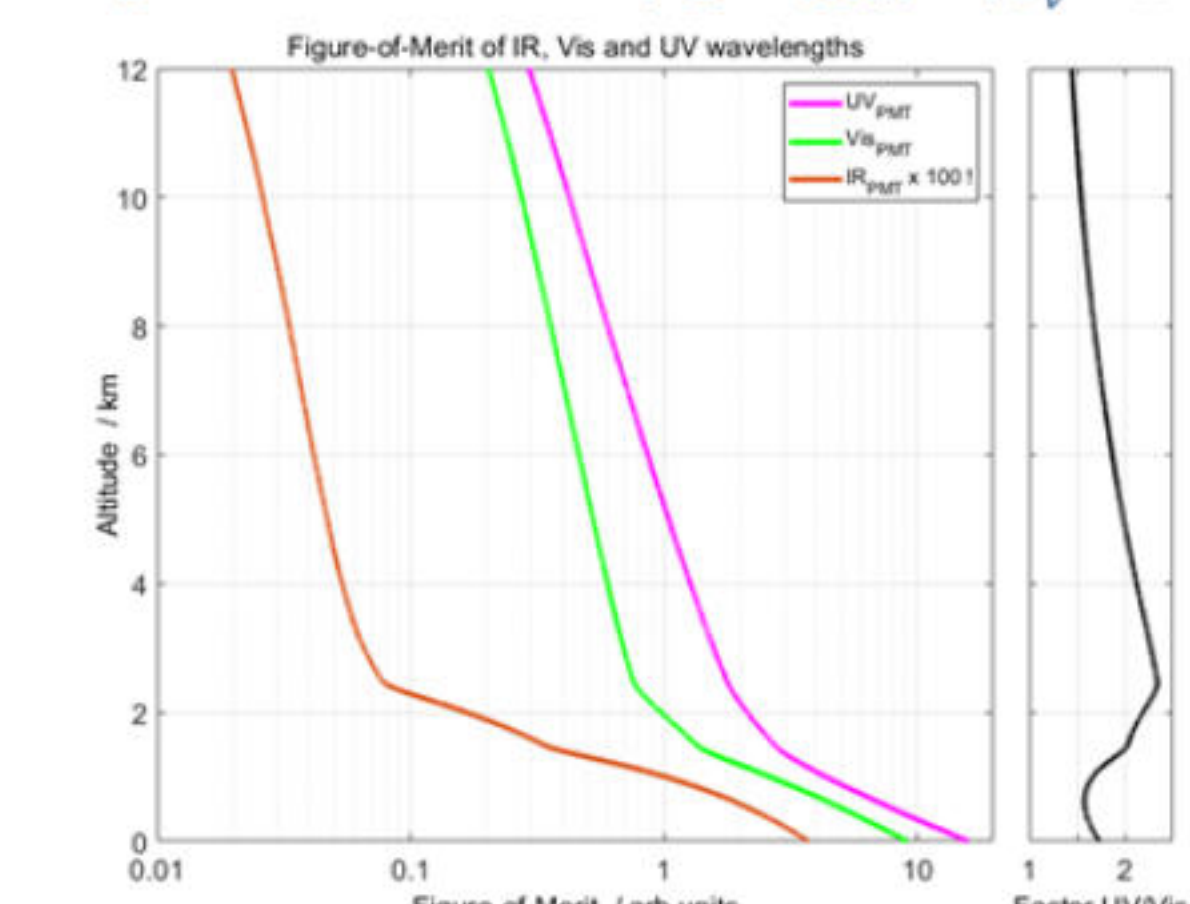
→ with Vis and UV: **spatial and temporal resolution of turbulent C_n² for detailed turb. structure studies**

- ! Conservative assessment (laser, signal recovery, ...)
- ! Many uncertainties and assumptions, in particular w.r.t.:
 - AoA theories spread [ZK04], further approximations
 - C_n^2 models spread
 - Boundary layer depth
 - Shannon-Nyquist criterion just fulfilled
 - Laser: pointing stability measurement, ...
 - Amplitude correction
 - Turbulence assumed fully frozen over measurement



Backscatter and detection

- No further req.'s on spectrum, purity
- Not sensitive on scattering process → molecular + aerosol backscatter
- Figure-of-merit = $\beta_{\Sigma} \cdot T_{Atm} \cdot \eta_{cv} \cdot Q \cdot E$

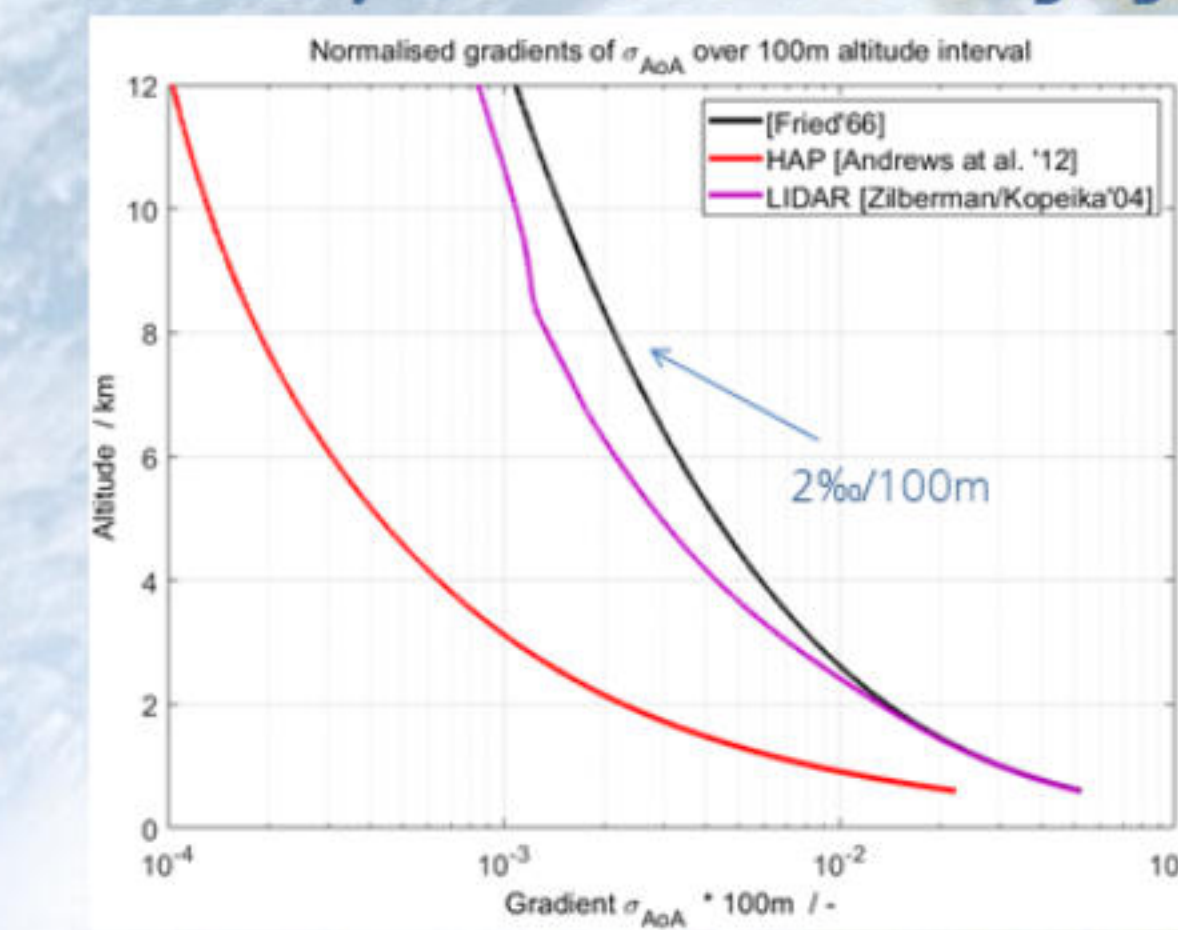


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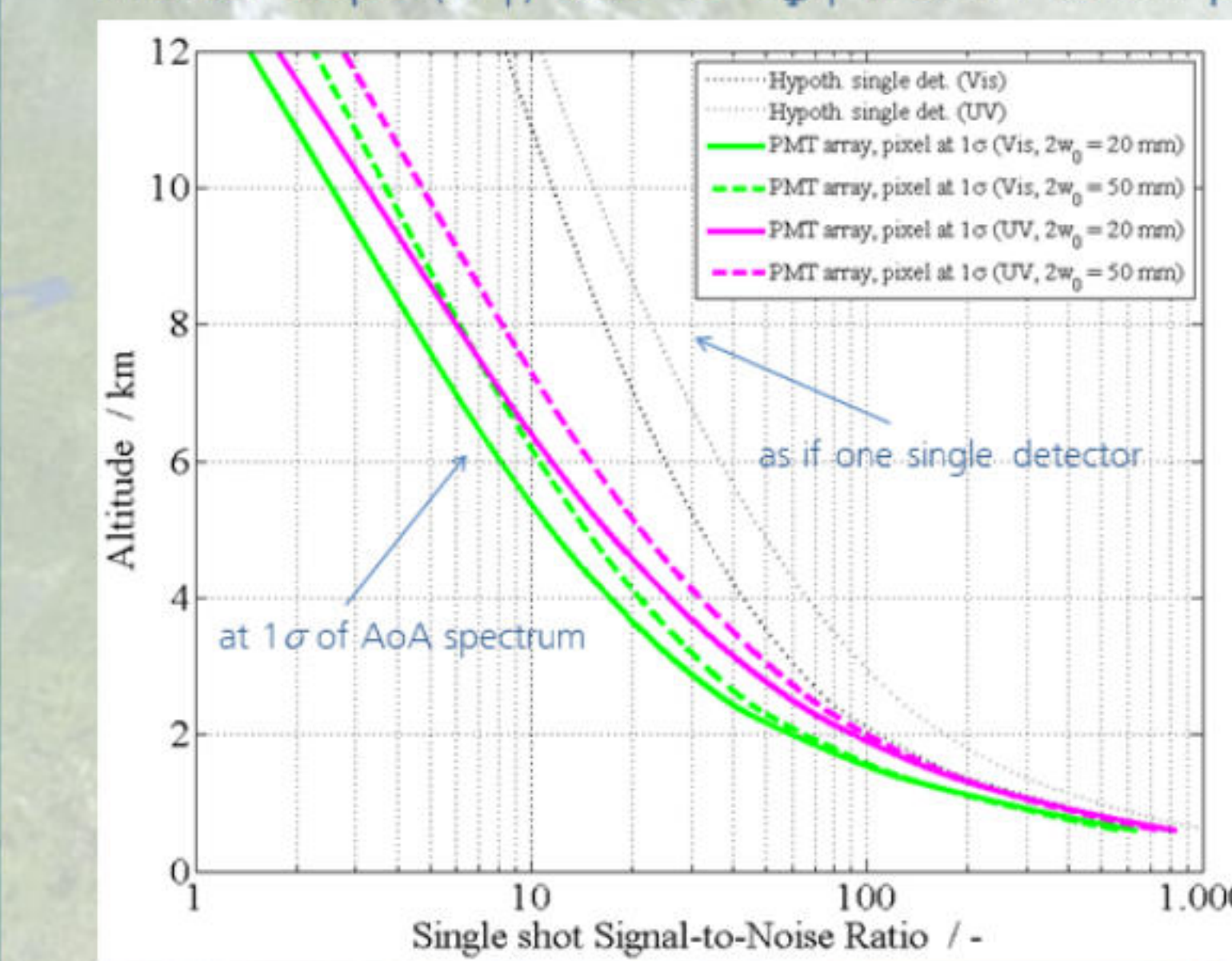
Measurement and retrieval

- Measurement is altitude-integrated AoA fluctuation spectrum width
- Recover C_n^2 features with inversion
- Resolve gradients, e.g.: 2%/100m → necessary SNR = 500 → averaging times



SNR – per pulse

- Determine single-shot SNR with lidar equation
- Flatter slope ($h \uparrow$) due to $\sigma_{\varphi} \uparrow$ from 1 to $>7 \mu rad$



SNR – detector and laser considerations

- AoA-fluctuation 2D „spectrum“ → compress to 1D
- e.g. PMT line detector H7260
- demonstrated sub-pixel resolution 2.5 mPix
- size AoA spectrum on detector: $[3\sigma_{AoA} + 3\sigma_{\varphi}] \times 2$
- COTS Nd:YAG $P_{Vis} = 110mJ$, $P_{UV} = 60mJ$
- Beam width $2w_0 = 20 + 50mm$, Tel- $\emptyset = 50cm$, O.R.

