

On the Relevance of Point Defects for the Selection of Contacting Electrodes: Ag as an Example for Mg₂(Si,Sn)-based Thermoelectric Generators

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Abstract:

In developing thermoelectric generators, optimizing interfaces between thermoelectric materials and contacting electrodes is a crucial step. Among the tested electrodes for Mg₂(Si,Sn)-based generators, Ag shows good adhesion, controllable interfaces and low electrical contact resistances. However, it induces unexpected changes in the Seebeck coefficient of n-type samples, while no change is observed in p-type.

In order to understand said behavior, contacting results for Bi-doped Mg₂Si, Mg₂Sn and Mg₂Si_{1-x}Sn_x with Ag are compared with predictions based on defect formation energies obtained within hybrid-density functional theory (DFT). A qualitative description of the Ag diffusion mechanism in Mg₂X is also introduced.

Calculation results show that Ag-induced defects have sufficiently low formation energies to influence charge carrier concentrations, particularly Ag substitution on the Mg site (Ag_{Mg}). Ag_{Mg} acts as an acceptor and causes a counter-doping effect by compensating the electrons provided by Bi. However, in Li-doped p-type, as Li-defects have the lowest formation energies, a negligible charge carrier concentration change is predicted, which fits with experimental observations. Concerning solid solutions, interpolation from the binaries predicts a similar behavior, which also meets experimental findings. Therefore, this work not only establishes the calculation method and explains the observed effect, but also proves the importance of defects in selecting contacting electrodes.

1. Introduction

Thermoelectric (TE) materials are used in several industrial fields such as aerospace, automotive, and industry; and research to develop more environmental-friendly TE generators is continuously expanding [1-4]. In order to have a highly efficient TE device, contacting the TE legs is as important as optimizing the TE material [5, 6]. In fact, this step adds contact resistances and potential chemical interactions between the contact materials and the TE material, and both can be detrimental to the TE device if not controlled. The electrical contact resistances R_c , as well as the thermal contact resistances, have to be kept as low as possible, and the electrodes should be chemically and physically stable metals or conductive intermetallics that (mechanically) adhere well to the TE material [7, 8]. There should also preferably be very limited diffusion between the metal and the semiconductor that would result in reactions forming new phases. All the mentioned conditions should remain stable in the long term under working temperature and thermal stress [9]. That is also why the electrode and the TE material should have similar coefficients of thermal

expansion (CTE), which would guarantee a stable behavior free of failure under temperature cycling.

Several studies on developing contacting solutions were conducted, studying different material systems for thermoelectric applications. In fact, finding suitable contacts is a material specific problem, as the outcome will depend on the TE material, the metallic electrode and the potential interactions between them (CTE, adhesion, diffusion, reaction ...). Among others, Ni [10, 11] and Fe [12] were studied with PbTe showing good bonding results thin interface layers and low electrical contact resistances, Ti [13] and Fe-Ni [14] were successfully tested for skutterudites materials, and Mo [15] and Ag [16] were used with half-heusler systems.

One of the also frequently studied TE materials are $Mg_2Si_{1-x}Sn_x$ solid solutions as they consist of abundant elements, are environmentally friendly, and have improved thermoelectric properties compared to their binaries [17-21]. Contacting of $Mg_2Si_{1-x}Sn_x$ materials was tested using Ag [22] Ni [22-24] and Cu [7, 25, 26] electrodes, and electrical contact resistances and microstructure of the reaction layers were reported.

In this work and for the first time, contacting $Mg_2Si_{1-x}Sn_x$ based-TEGs is studied from a point defect perspective. We discuss here experimental results of contacting for the binaries Mg_2Si and Mg_2Sn as well as the $Mg_2Si_{1-x}Sn_x$ solid solutions with Ag as a suitable example for the importance of point defects in the thermoelectric material in the selection of joining electrodes.

The issue was first observed while contacting n- and p- type $Mg_2Si_{1-x}Sn_x$ (with $x = 0.4$ and $x = 0.3$, respectively) with Ag, where the results showed different behaviors of the TE materials after joining [22]. In fact, not only the electrical contact resistances were very different ($r_c \sim 400 \pm 38 \mu\Omega \text{ cm}^2$ for n-type vs. $\sim 9 \pm 1 \mu\Omega \text{ cm}^2$ for p-type, both joined at $450 \text{ }^\circ\text{C}$), but also a change in the Seebeck values of the n-type samples was measured after joining (from $\sim -110 \mu\text{V K}^{-1}$ to $\sim -200 \mu\text{V K}^{-1}$ at room temperature), while they remained unchanged for p-type samples ($\sim 100 \mu\text{V K}^{-1}$).

A similar behavior was also observed after contacting n- and p-type $\text{Mg}_2\text{Si}_{0.3}\text{Sn}_{0.7}$ with Cu [25]. Seebeck values of n-type samples also changed during contacting (from $\sim -110 \mu\text{V K}^{-1}$ to $\sim -160 \mu\text{V K}^{-1}$) and annealing (to $\sim -230 \mu\text{V K}^{-1}$), while no change was observed for p-type samples. In this study, only Ag will be considered because it showed a less complex reaction layer and much less diffusion than what was observed with Cu as reported in [22] and in [25].

However, $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ solid solutions are known to suffer from demixing under certain conditions [27-29] and indeed demixing into Si-rich and Sn-rich phases was observed for both Cu and Ag contacted samples, potentially also influencing the Seebeck coefficient. In order to reduce the chemical complexity and identify the origin of the observed alteration of the Seebeck coefficient, we contacted n-type Mg_2Si and Mg_2Sn with Ag at different temperatures. To further understand the observed Seebeck behavior, an investigation of the intrinsic and extrinsic point defects of the studied binaries is required. This does not come as a surprise, as point defects are known to play a crucial role in determining semiconductors' conduction types [30-33]. In fact, for materials like Bi_2Te_3 , references [34, 35] reported that, under anion-rich conditions, the antisite defect Te on Bi (Te_{Bi}) account for the n-type conduction, while, under cation-rich conditions, the negatively charged antisite defects such as Bi on Te sites (Bi_{Te}) account for the p-type conduction. As for the case of Bi_2Se_3 , the n-type conduction was related to the Se on Bi antisite defect (Se_{Bi}) under anion-rich conditions, while it was related to the Se vacancies (V_{Se}) under cation-rich growth conditions. Defect studies and computation of their formation energies can be easier done for binaries than for solid solutions, and an interpolation to the intermediate ternary compositions can be achieved from the results of the binaries. This explains why almost all respective research focuses on the binary Mg_2X ($\text{X} = \text{Si}, \text{Sn}, \text{Ge}$) rather than to their solid solutions.

In the case of Mg_2X materials, Kato *et al.* [36] used density-functional theory (DFT) calculations to evaluate point defect formation energies in Mg_2Si and to understand the origin of the previously reported intrinsic n-type conduction of this material [37, 38] Their results showed that the n-type conduction comes from the positively charged ($q = 2+$) Mg ions at interstitial sites (I_{Mg}), which are the most energetically stable point defects under both Mg-rich and Mg-poor (Si-rich) conditions. Jund *et al.* [39] studied the relative stabilities of Mg_2Si and Mg_2Ge using first principles calculations with different functionals. They showed that the stability of the point defects strongly depends on the growth conditions. In case of Mg_2Si , under stoichiometric and Mg rich conditions, Mg interstitials (I_{Mg}) is the most stable defect, while under Mg poor conditions, Si_{Mg} is more stable. This contradicts what was reported by Kato [36], but Kato *et al.* considered charged defects and dependence of the formation energies on chemical potentials, while Jund *et al.* considered neutral defects.

Another work by Liu *et al.* [40] stated that Mg vacancies V_{Mg} and Mg interstitials I_{Mg} are the dominant defects in Mg_2Si and Mg_2Sn , independently of the chemical environment (Mg-rich or Si/Sn-rich). The concentration of these defects is what determines the conduction type in each material. V_{Mg} is an acceptor ($q = 2-$) more favorable under Mg-depleted conditions, and I_{Mg} is a donor more favorable under Mg-rich conditions. Si/Sn related defects are less likely to occur in the binaries, partly because their ionic radii (2.72 Å / 2.94 Å) are larger than that of Mg (0.66 Å), so the local disorder and strain due to these defects are much larger than the strain caused by Mg related defects.

Meanwhile, there have been few studies on intrinsic defects in Mg_2Sn mitigated by the band gap underestimation in conventional DFT calculations, i.e. using the local density approximation or generalized gradient approximation. While Liu *et al.* [40] reported a quantitative analysis of the possible intrinsic defects in Mg_2Si , Mg_2Ge , and Mg_2Sn , their quantitative analysis of the defect

densities suffers from a severe band gap underestimation: most of the major carriers are compensated by the minority carriers due to the small band gap calculated by DFT. This underestimation of the band gap persists with other works using conventional DFT, including the works of Kato *et al.* [36] and Jund *et al.* [39] mentioned above. In agreement with this, our conventional DFT calculations also showed that the band gap is obtained negative for Mg₂Sn. Such band gap underestimations affect the electronic chemical potential, which in turn affects defect stabilities. To overcome this issue, advanced computational methods such as hybrid-DFT [41] and quasi-particle calculations [42] were found to be important. Our recent hybrid functional study on intrinsic defects in Mg₂Si and Mg₂Sn finally quantitatively describes the intrinsic defect properties of these material systems [43].

Besides intrinsic defects, extrinsic defects (e.g. due to doping) are used to tune the carrier concentration of TE materials as the most common way to improve zT [44-47]. As these “added” defects can be more stable than the intrinsic defects of the material and influence the charge carrier concentrations in the chemical potential region of interest, both defect types need to be taken into consideration in order to have a full picture and predict the materials’ behavior [48].

The aim of this paper is to understand the unexpected behavior of Ag contacted n-type Mg₂Si_{1-x}Sn_x using first principle calculations of point defect formation energies. In order to model the experimental situation (doped Mg₂X in contact with Ag), we investigate the simultaneous presence of intrinsic and extrinsic defects in n- and p-type Mg₂Si and Mg₂Sn employing hybrid DFT calculations [41].

An understanding for the solid solutions can then be extrapolated. The considered dopants for n- and p- type conduction are respectively Bi and Li, and both Mg-rich (for n-type) and Mg-poor (for p-type) conditions are discussed.

Our findings show that the extrinsic defects generated after joining Ag with $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$, namely Ag_{Mg} , are behind the experimentally observed Seebeck changes in n-type materials. Ag_{Mg} acts as an electron trap for the conduction electrons provided by Bi (Bi_{Si} for Mg_2Si and Bi_{Sn} for Mg_2Sn), leading to a decrease in the majority charge carrier density. In case of p-type materials, Ag related defects have higher formation energies than Li defects, which makes the influence of Ag_{Mg} or I_{Ag} not as visible as in n-type materials.

This example highlights that, in thermoelectricity, defect calculations are not just important for TE material development and dopant selection, but they also need to be taken into consideration when selecting contacting electrodes.

2. Material and methods

2.1. Sample Preparation and Characterization

Mg_2Si and Mg_2Sn were prepared from ball milled powder as reported in [18] with the respective nominal stoichiometries $\text{Mg}_{2.06}\text{Si}_{0.97}\text{Bi}_{0.03}$ and $\text{Mg}_{2.15}\text{Sn}_{0.97}\text{Bi}_{0.03}$. The powders from each material were pressed into three 15 mm diameter pellets for 10 min, at 800 °C for Mg_2Si and at 600 °C for Mg_2Sn [49] in a direct sinter press and then joined with Ag foil. [The contacting experiments were also done through current assisted joining in the same direct sinter press.](#) Each pellet was joined at a different temperature: 450, 500 and 550 °C for Mg_2Si , and 400, 450 and 500 °C for Mg_2Sn . The heating rate was 1 K s⁻¹ and the holding time was 10 min for each sample. These temperatures were selected because 450 °C showed to be a good joining temperature for $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ [22].

The solid solution $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ samples were prepared with the following stoichiometry: $\text{Mg}_{2.06}\text{Si}_{0.3}\text{Sn}_{0.665}\text{Bi}_{0.035}$ for n-type and $\text{Mg}_{1.98}\text{Li}_{0.02}\text{Si}_{0.4}\text{Sn}_{0.6}$ for p-type according to the procedures reported in [22], [25] and [50]. Three extra samples were prepared for this particular study following the procedure described in [22] to further investigate the observed trends: the first of

these samples was prepared using 5 g of n-type $\text{Mg}_2\text{Si}_{0.3}\text{Sn}_{0.7}$ powder instead of the usual 1.2 g, which was then pressed in a 15 mm diameter pellet (700 °C, 20 min) and contacted with Ag foil at 450 °C for 10 min. The second and the third samples were made out of pre-pressed n- and p-type pellets that were joined together with Ag foils in between, also at 450 °C for 10 min. These samples were joined in two different experiments, one where the n-type pellet was at the bottom and the p-type pellet was on top of the Ag foil (referred to as $n//\text{Ag}/p$) and one where the stacking order was reversed ($p//\text{Ag}/n$).

Property characterization of the samples was done with SEM/EDX for microstructure investigations along the cross sections, and with an in-house built Potential & Seebeck Scanning Microprobe (PSM) [23, 51] for Seebeck measurements. Estimations of carrier concentration n and reduced chemical potential η were obtained from experimental results of the Seebeck coefficient combined with the effective mass (m_D^*) values from a single parabolic band (SPB) model based on the following equations [19, 52-54]

$$S = \frac{k_B}{e} \left(\frac{2F_1(\eta)}{F_0(\eta)} - \eta \right) \quad (1)$$

$$n = 4\pi \left(\frac{2m_D^* k_B T}{h^2} \right)^{1.5} F_{\frac{1}{2}}(\eta) \quad (2)$$

where k_B is Boltzmann's constant and $F_i(\eta)$ is the Fermi integral of order i .

2.2. Hybrid-DFT Calculations for Defect Formation Energies

First-principles calculations were performed to investigate the electrical properties of intrinsic and extrinsic defects in Mg_2Si and Mg_2Sn within the hybrid-DFT calculations [55] using the Vienna Ab Initio Simulation Package [56, 57]. The hybrid exchange-correlation energy function of HSE06 was employed with the exact-exchange mixing parameter of 25% and the screening parameter of

0.208 Å⁻¹. The planewave energy basis set was used with the energy cutoff of 296 eV. The projector-augmented wave pseudopotentials were used for atomic potentials.

To model the defective system, a (2×2×2) cubic supercell was used with the lattice parameters of 6.35 Å and 6.75 Å for Mg₂Si and Mg₂Sn, respectively. In the supercell, there are 64 Mg and 32 Si/Sn atoms, and the dopant atom is added, removed, or replaced in the host supercell to generate defective supercells for vacancy, substitutional, and interstitial defects. The Γ -centered (2×2×2) k -point mesh was sampled for charge density integration over the Brillouin zone. The atomic positions were fully relaxed until the magnitude of the remaining forces was smaller than 0.005 eV Å⁻¹.

The charged defect formation energy of a defect D in the charge state q (D^q) in the Mg₂X was obtained using the following equation

$$E_{\text{form}}(D^q, \text{Mg}_2X) = E_{\text{tot}}[D^q] - E_0 - \sum_j (\mu_j \Delta n_j) + q(E_F + E_{\text{CBM}})$$

where $E_{\text{tot}}[D^q]$ and E_0 are the total energies with and without defect in the supercell, j is the atomic species in the supercell, Δn_j is the number change of atomic species j in the defective supercell with respect to the pristine supercell without defects, E_F is the electron Fermi level, and E_{CBM} is the energy of the conduction band minimum (CBM) [43, 58, 59]. Note that for the defects, the total energies were calculated using HSE06. However due to the huge computational cost, the spin-orbit interaction is not included.

3. Results

3.1. Mg₂Si/Sn with Ag

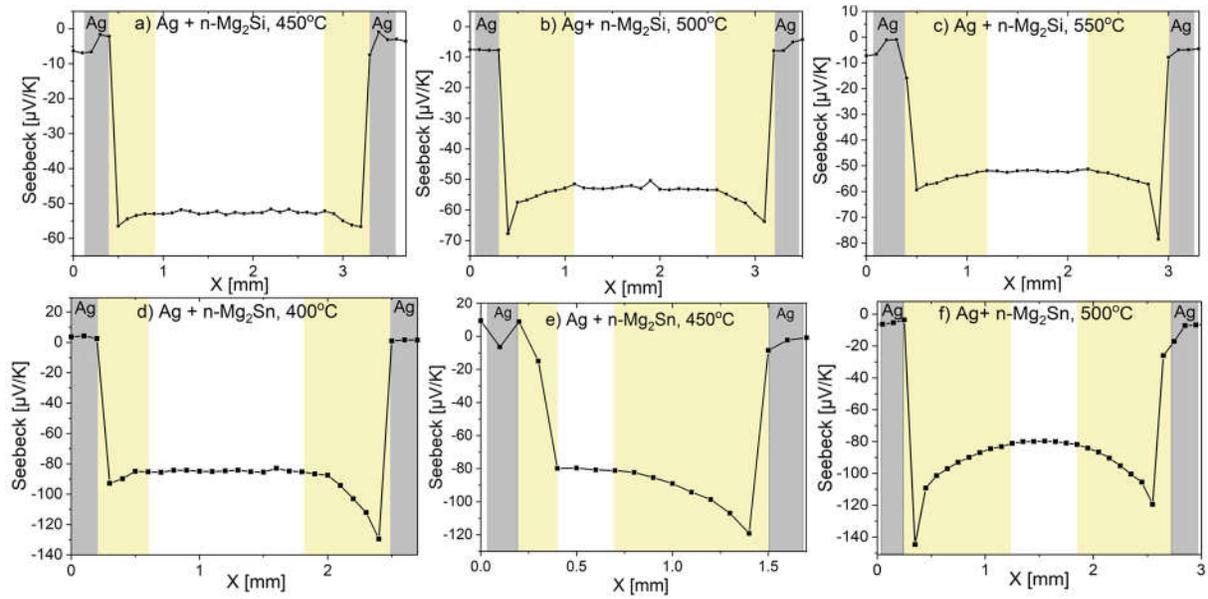


Figure 1: Representative Seebeck profiles for Mg_2Si and Mg_2Sn contacted with Ag at different temperatures. The grey rectangles indicate the Ag foil and the yellow rectangles delimit the length where the Seebeck coefficient is altered. (Color should be used in print).

Seebeck scan lines by the PSM at room temperature of n- Mg_2Si and n- Mg_2Sn joined with Ag at 3 different temperatures, (450 °C, 500 °C, 550 °C) and (400 °C, 450 °C, 500 °C) respectively, are presented in **Figure 1**. All the samples displayed an interesting Seebeck profile where the S values peak near the interfaces and then return back to the bulk value beyond a certain depth. The portions of the samples where S changed are marked with yellow rectangles on **Figure 1**. As no significant local variation was observed in the samples before the joining step, it must be linked to the interaction with the electrode. The observed changes in the Seebeck coefficient are believed to be caused by the diffusion of Ag into the TE material. For each binary, the diffusion of Ag, observed by the zone width of the altered Seebeck coefficient, differs with temperatures as can be seen in **Figure 1**. The presented line scans of the Seebeck coefficient are representative of the general behavior for each sample.

The average change in Seebeck coefficient in the Mg₂Si samples is comparable for all joining temperatures. The Seebeck value of the bulk of the TE material is maintained around -55 $\mu\text{V K}^{-1}$ for all samples, and the average values close to the interface are $-57 \pm 1 \mu\text{V K}^{-1}$, $-63 \pm 10 \mu\text{V K}^{-1}$ and $-58 \pm 2 \mu\text{V K}^{-1}$ respectively for 450 °C, 500 °C and 550 °C. The high standard deviation observed for the sample joined at 500 °C comes from the line to line scatter, potentially due to local inhomogeneities in the sample. Moreover, while the maximum drop of the Seebeck coefficient recorded for 450 and 550 °C were respectively -65 $\mu\text{V K}^{-1}$ and -81 $\mu\text{V K}^{-1}$, it locally reached -115 $\mu\text{V K}^{-1}$ for 500 °C.

The Mg₂Sn samples showed a similar Seebeck gradient behavior, but unlike for the Mg₂Si samples, we consistently observed differences between the two contacting interfaces. As can be seen from **Figure 1**, Mg₂Sn joined at 400 and 450 °C exhibit steep drops on the one side, but almost no drop on the other. Whether this is due to the electromigration of Ag during the current-assisted joining or due to different reaction layers on both sides cannot be clearly stated. Interestingly, in the case of the sample joined at 500 °C, both sides have similar average Seebeck behavior. Even though the graph shown in **Figure 1 f**) displays an uneven (local) situation, line to line variation averages both sides to similar values. Averages of the Seebeck values near the interfaces and their corresponding estimated carrier concentrations for both Mg₂Si and Mg₂Sn are provided in **Table S 1** in the Supplementary Material.

Another difference which can be observed in the samples depending on the joining temperature is the increase of the width of the layer where S is different from bulk values (interior of the TE material). In the case of Mg₂Si samples, while this layer has a length of only 0.3 mm for $T_{\text{join}} = 450 \text{ °C}$, it increases to 0.6 mm for $T_{\text{join}} = 500 \text{ °C}$ and 0.8 mm for $T_{\text{join}} = 550 \text{ °C}$.

To have a better description of Ag diffusion inside Mg₂X systems as well as gain an understanding of the dependence of this diffusion on temperature, a simple exponential decay function (Equation 1) was used to fit the experimental results and quantify the observed changes:

$$S(x) = S_{bulk} + A \exp\left(\frac{-x}{\tau}\right) \quad (3)$$

where S_{bulk} is the Seebeck of the TE material, A is the amplitude and τ the effective diffusion length. As each Seebeck line scan contains two graded sections opposite in decay direction, each line scan was divided into two fits: the first fit was the right-hand side gradient to which Equation 1 was applied as is, while the second fit was the left-hand side gradient which was first mirrored then fitted to the same equation. The fitting results are presented in **Table 1** and divided as described into left and right sides. [A verification of this model based on the fitting with Equation 3 is provided in section I of the Supplementary Material. A good agreement between the modelling and the experimental data can be deduced from Figure S1 of the Supplementary Material.](#)

Table 1: Fitting results of the diffusion length τ and the amplitude A from Seebeck line scans of Mg₂Si and Mg₂Sn.

S_{inter} is the result of Equation 3 at the interface and n_{inter} the corresponding carrier concentration obtained using Equations 1 and 2 and the constants reported in [19] and [18]. Bulk values before contacting are $S = 55 \mu V K^{-1}$, $n = 2.5 \times 10^{20} cm^{-3}$ for Mg₂Si and $S = 80 \mu V K^{-1}$, $n = 3 \times 10^{20} cm^{-3}$ for Mg₂Sn

	T_{join} – side	τ [mm]	A [$\mu V K^{-1}$]	S_{inter} [$\mu V K^{-1}$]	n_{inter} ($10^{20} \times cm^{-3}$)
Mg ₂ Si	450 – Left side	0.13	3.4	58	2.4
	450 – Right side	0.09	6.2	61	2.2
	500 – Left side	0.19	10	65	2.0
	500 – Right side	0.15	22.5	78	1.5
	550 – Left side	0.28	8.1	63	2.1
	550 – Right side	0.38	9.9	65	2
Mg ₂ Sn	400 – Left side	0.11	12	92	2.8
	400 – Right side	0.15	32	112	2.1
	450 – Left side	–	–	–	–
	450 – Right side	0.24	45.5	125	1.6
	500 – Left side	0.22	42.2	122	1.7
	500 – Right side	0.17	46.4	127	1.5

Table 1 shows that the diffusion of Ag in Mg₂Si at each temperature has comparable diffusion lengths τ and amplitudes A on both contacted sides. The table also shows an overall increase of τ and A with temperature.

As for Mg₂Sn samples, the difference in amplitude originates from the difference in interface Seebeck coefficient values between both sides of each sample, particularly those joined at 400 and 450 °C. The left side of the 450 °C sample was omitted because there was no S gradient. τ values do not show a clear temperature dependence like in Mg₂Si, as a deeper diffusion is seen at 450 °C, though just on one side.

The obtained values of τ and A were implemented in Equation 1, and values of $S(x)$ and corresponding carrier concentrations n at the interface were also reported in **Table 1**. The latter were estimated using Equations 1 and 2, assuming $m_D^* = 1.1 m_0$ [60] and $m_D^* = 2 m_0$ [61].

Using the obtained values of τ , diffusion coefficients and activation energies were calculated.

Using $\tau = \sqrt{Dt}$ where τ is the diffusion length (mm), D is the diffusion coefficient (m² s⁻¹) and t is the diffusion time (s), we can estimate the diffusion coefficient $D(T)$ for each joining temperature using averaged values of τ from both sides as given in **Table 1** and $t = 600$ s as the holding contacting time. The temperature-independent proportionality constant D_0 (m² s⁻¹) and the activation energy E_A (J mol⁻¹) are obtained from fitting the Arrhenius equation $D(T) = D_0 \exp(-\frac{E_A}{RT_{join}})$ [62]. In this equation, the molar gas constant R is fixed at 8.314 J mol⁻¹ K⁻¹ and T is the absolute temperature (K).

Here, we only present results for Mg₂Si, as they display a systematic behavior with temperature, unlike Mg₂Sn. The obtained values of E_A and D_0 were respectively 111 kJ mol⁻¹ = 1.15 eV and 1.8

$\times 10^{-3} \text{ m}^2 \text{ s}^{-1}$. They were both extracted from the slope and the intercept of the fitting line to the Arrhenius plot presented in **Figure 2**.

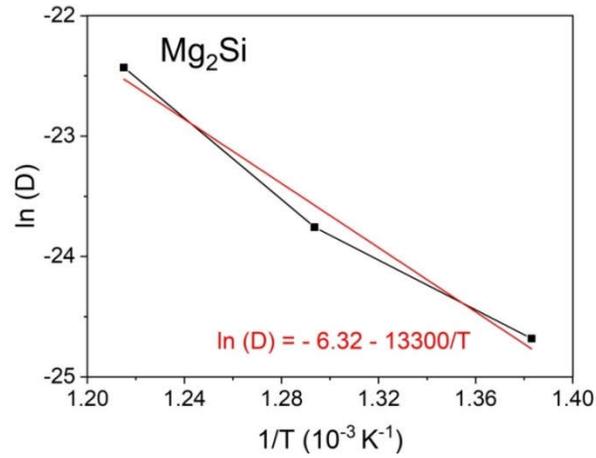


Figure 2: Arrhenius plot of the diffusion constant of Ag in Mg_2Si

3.2. $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ with Ag

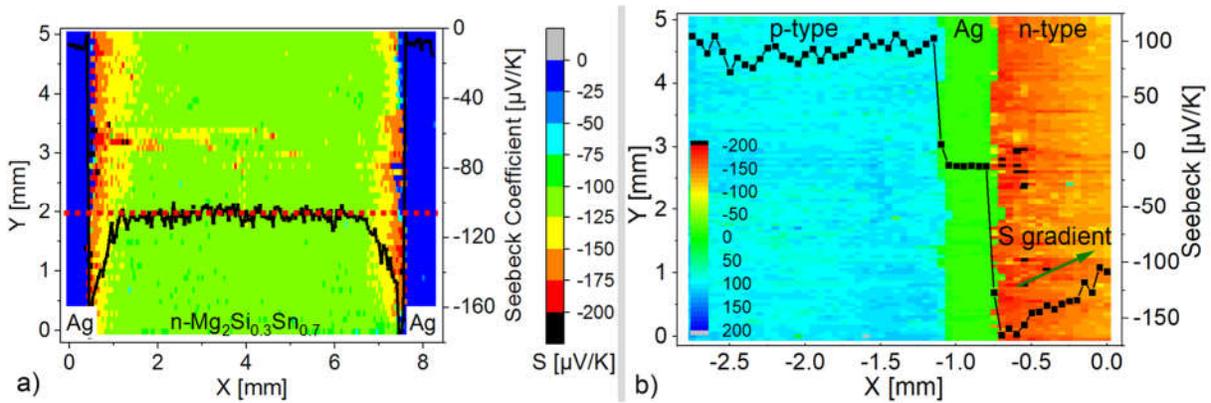


Figure 3: Exemplary Seebeck profile scans and 2D surface plots of a) thick n-type $\text{Mg}_2\text{Si}_{0.3}\text{Sn}_{0.7}$ joined with Ag at 450°C , and b) simultaneously joined p-type (bottom), Ag (middle) and n-type (top) materials displaying a Seebeck gradient only for the n-type. The selected Seebeck profile line scans correspond to the scan positions $y = 0.6 \text{ mm}$ and $y = 5 \text{ mm}$ for a) and b) respectively. (Color should be used in print).

After confirming the change of Seebeck behavior during contacting on the Mg₂Si and Mg₂Sn binaries, further experiments on the solid solution were conducted. Unlike the previously reported case with thin samples where S changed along the whole sample thickness [22], the thick n-type Mg₂Si_{0.3}Sn_{0.7} sample presented in this work showed a seemingly different behavior after joining. In fact, as shown in **Figure 3** (a), S value changes occurred near the interfaces only, reaching $S_{max} \sim -170 \mu\text{V K}^{-1}$, which is qualitatively similar to what was observed for the binaries. This change of Seebeck corresponds to a change in carrier concentration from $n = 2.9 \times 10^{20} \text{ cm}^{-3}$ to $n = 1.18 \times 10^{20} \text{ cm}^{-3}$ assuming $m_D^* = 2.5 m_0$ [17]. It is clear through the line scan as well as the 2D plot in **Figure 3** (a) that there is a gradient of the Seebeck near the electrodes, but that S values go back to the bulk value ($\sim -110 \mu\text{V K}^{-1}$, marked with the red dashed line) after a depth of $\sim 0.75 \text{ mm}$ on each side. Taking this depth into account, the results of the thick sample are not inconsistent with those of the previously reported thin samples, because the thin samples have a thickness of $\sim 1.5 \text{ mm}$, which is completely covered by the actual depth of the gradient zones on both sides.

The same fitting procedure (Equation 1) used for the binaries was also applied here, and an average value for the diffusion length $\tau(T_{join})$ from both joining interfaces was obtained. The obtained values are $\tau(T_{join}) = 0.38 \text{ mm}$ and $D(T_{join}) = 2.4 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$. These numbers are closer to those obtained for Mg₂Sn at 450 °C / 723 K ($9.6 \times 10^{-11} \text{ m}^2 \text{ s}^{-1}$) than those for Mg₂Si ($1.9 \times 10^{-11} \text{ m}^2 \text{ s}^{-1}$), which is not surprising as the used ternary is rich in Mg₂Sn ($\sim 70\%$).

The simultaneously joined n- and p- type stacked samples were produced by joining pre-pressed n- and p- pellets with Ag foil in between. No Ag foil was added on the external sides of the pellets. The purpose of this experiment was to investigate a simultaneous diffusion/electromigration of Ag, and to rule out preparation and technical uncertainties. Seebeck scans of the $p//Ag//n$ sample were collected and are presented in **Figure 3** (b), while results for the $n//Ag//p$ sample are provided in the Supplementary Material (**Figure S 2**).

As shown in the 2D plots in **Figure 3** (b), a Seebeck gradient is only visible in the n-type side of the stacked sample, while no such gradient was observed in p-type. Similar results were observed in the second stacked sample (n//Ag//p) where, the change in S was again only recorded in the n-type pellet (stacked at the bottom of the sample arrangement). This shows that the Ag diffusion has a stronger and more visible effect in n-type, and that it is mainly not driven by current (electromigration). Instead, it is driven by temperature, and the extent of the diffusion and its effects seem to depend on the dominant carrier type.

4. Discussion

The observed behavior might in principle and qualitatively be explained by Ag-induced point defects in the thermoelectric material. The formation energy of charged defects is a function of the Fermi level and will thus differ between n and p-type counterparts of the “same” composition, potentially leading to different abundance of defects in the n and p-type materials. The lattice diffusion process is governed by the diffusion barrier of the relevant defect, which is the sum of its formation energy and its migration barrier [63], and is therefore also dependent on the Fermi level of the electrons. For example, as negatively charged defects have lower formation energies in n-type than in p-type, they will be more abundant, and more mobile in n-type than in p-type. Based on our experimental results, we thus speculate that negatively charged acceptor-like defects will be generated during contacting the TE legs, affecting the charge carrier concentration and the Seebeck coefficient. To substantiate this hypothesis, calculations of the formation energies of these defects are performed for the binaries Mg_2Si and Mg_2Sn . This also establishes a base for interpolation to interpret the result for the ternary combinations.

Figure 4 shows the calculated formation energy curves of the relevant intrinsic and extrinsic defects in n-and p-type Mg_2Si and Mg_2Sn doped with Bi and Li, respectively, and contacted with

Ag. Defects related to Bi and Li were considered as dopants for Mg₂Si and Mg₂Sn, while Ag point defects were considered to understand the possible influence of the electrode on the thermoelectric materials. In both material cases, the conduction band minimum (CBM) is fixed at $E = 0$ eV. So, using the calculated values of the band gaps from hybrid-DFT, we obtained the positions of the valence band maxima (VBM) for Mg₂Si and Mg₂Sn as 0.570 eV and 0.145 eV. These values are comparable to the experimental band gaps which are 0.77 and 0.35 eV, respectively [64]. Note that within conventional DFT calculations using local-density approximation and GGA, the band gaps are severely underestimated to be ~ 0.2 eV and ~ -0.19 eV for Mg₂Si and Mg₂Sn, respectively [41], and the defect stability could be improperly described.

As n-type samples are made with 3 at% excess Mg, we might suppose that they are under Mg-rich chemical potential conditions. However, Mg losses are expected to occur during the initial pellet pressing step and then the joining step. Even though these losses are not straightforward to quantify, we also consider Mg-poor conditions for n-type Mg₂Si and Mg₂Sn. In **Figure 4**, only the relevant defects with formation energies lower than 1 eV are presented. Full figures with complete formation energies under all conditions are provided in the Supplementary Material, with **Figure S 3** and **Figure S 4** representing all the defects in Mg₂Si and Mg₂Sn, respectively.

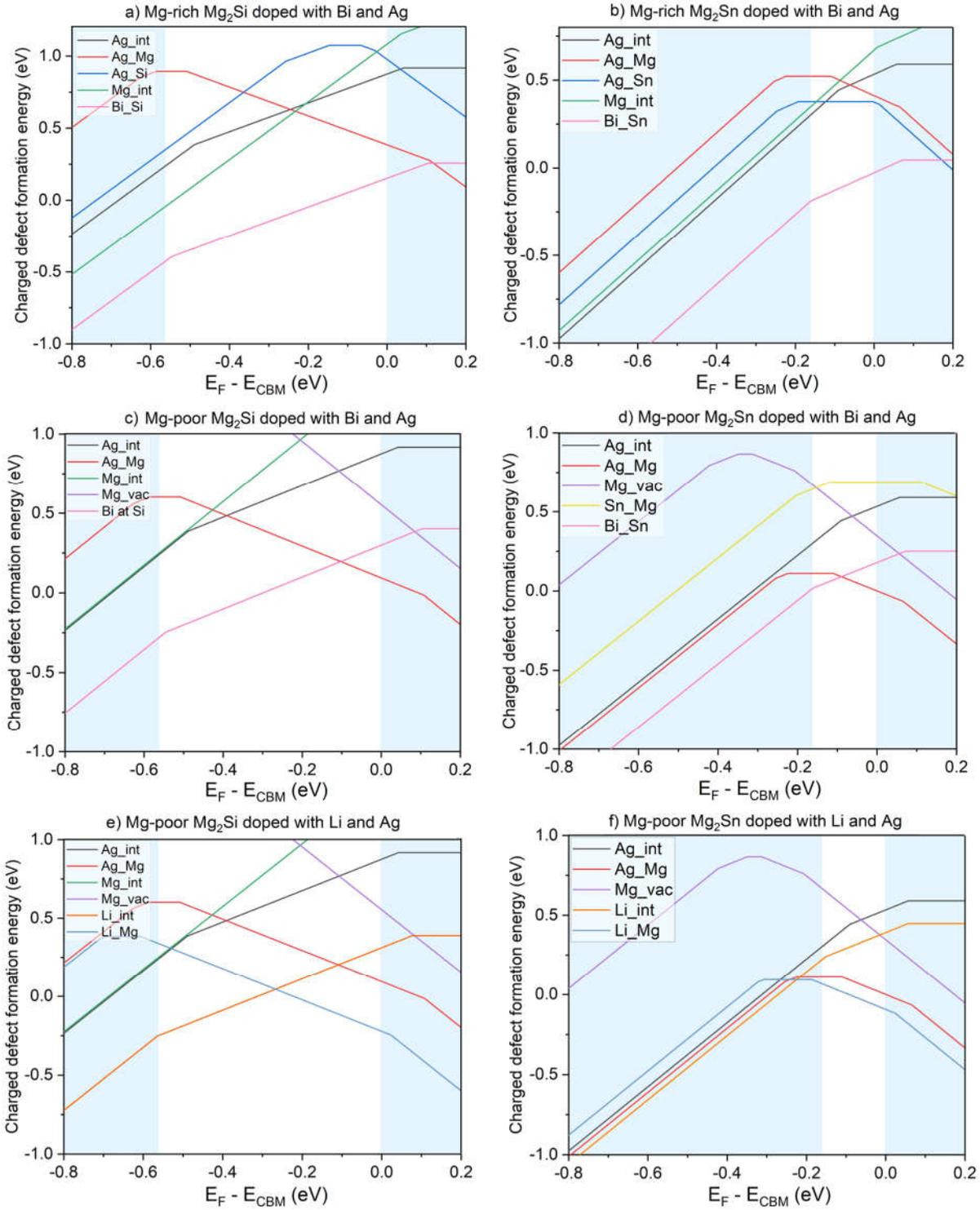


Figure 4: Formation energy curves for a) Bi- and Ag-related defects in Mg-rich Mg_2Si , b) Bi- and Ag-related defects in Mg-rich Mg_2Sn , c) Bi- and Ag-related defects in Mg-poor Mg_2Si , d) Bi- and Ag-related defects in Mg-poor Mg_2Sn , e) Li- and Ag-related defects in Mg-poor Mg_2Si and f) Li- and Ag-related defects in Mg-poor Mg_2Sn . E_F is given with respect to the conduction band maximum, and the white regions indicate the band gaps. (Color should be used in print).

In n-type Mg₂Si on **Figure 4** (a), Bi_{Si} becomes the most stable defect with the lowest formation energy. It is a shallow donor defect with the charge state of $q = 1+$ for both low and high doped Mg₂Si (up to $E_F = 0.1$ eV, which is where the Fermi level can be pinned). It is also more stable than I_{Mg} which is the main (intrinsic) defect behind the n-type conduction in non-doped Mg₂Si. Such observation can be underpinned by experimental findings showing that the tuning range of the carrier concentration with extrinsic dopants is wider than by just adjusting Mg content. Kato *et al.*[36], in fact, demonstrated that they could tune the carrier concentration by less than 1×10^{20} cm⁻³ with changing Mg content, while they could reach $1 \sim 2 \times 10^{20}$ cm⁻³ through Bi or Sb doping. Under Mg-poor conditions, as displayed on **Figure 4** (c), Bi_{Si} is also the most stable defect, however only for a smaller chemical potential range than Mg-rich conditions. In fact, the pinned Fermi level E_F is at -0.1 eV, if Ag point defects are considered. However, if we disregard the Ag defects potentially generated due to the contacting electrode, Bi_{Si} would be the most stable defect up until a chemical potential of 0.1 eV.

For the n-type samples, the chemical potential for the electrons is $E_F \sim 0$ eV. Under both (Mg) chemical potential conditions, the second defect of interest is Ag_{Mg}, a shallow acceptor defect with $q = 1-$. As shown in **Figure 4** (a) and (c), in the range of $E_F = -0.5$ to 0.1 eV, Bi_{Si} and Ag_{Mg} have opposite charges, as the former is a 1+ donor and the latter is a 1- acceptor. These two most stable defects will then compensate, which causes a decrease in the charge carrier concentration in the n-type material. With increasing E_F , the defect density of Ag_{Mg}¹⁻ increases, and at a certain energy, Ag_{Mg}¹⁻ can be the major defect. Note also that the Ag_{Mg} defect formation energy becomes lower when the Mg atomic chemical potential changes from Mg-rich to Mg-poor.

Considering the defect density equation $n(D, q) = N_0 e^{-\frac{E_{form}(D, q)}{k_B T}}$, where N_0 is the total density of possible sites that can form a defect D at charge state q [65], $n(D, q)$ of a defect decreases quickly with increasing formation energy $E_{form}(D, q)$. Therefore, the compensation effect of Bi_{Si}¹⁺

by $\text{Ag}_{\text{Mg}}^{1-}$ is more visible when the formation energies of both defects are either close or when $E_{\text{form}}(\text{Ag}_{\text{Mg}}) < E_{\text{form}}(\text{Bi}_{\text{Si}})$. Our experimental samples are heavily doped, with $E_F \sim 1 \text{ kBT} \sim 0.026 \text{ eV}$. Around this chemical potential, E_{form} of Ag_{Mg} and Bi_{Si} are comparable, so the charge compensation effect would be detectable, which matches the experimental data. For lower Fermi level samples, the difference in formation energy between the two defects increases, corresponding to a smaller expected compensation.

Using the method of climbed nudged elastic band (cNEB) calculations [59, 66, 67], we reveal that Ag defects in Mg_2Si can easily diffuse to form Ag_{Mg} defects via the interstitial diffusion of the I_{Ag} interstitial defect with a migration energy barrier of 0.652 eV. When the Fermi level is 0 (i.e. $E_F = E_{\text{CBM}}$), as the formation energies of $\text{I}_{\text{Ag}}^{1+}$ are 0.88 and 0.53 eV in Mg-rich Mg_2Si and Mg_2Sn respectively, the diffusion barrier will be in the range of 1.2 – 1.5 eV. When the diffused I_{Ag} is split into Ag_{Mg} (electron trap) and $\text{I}_{\text{Mg}}^{2+}$ (donor), and the separated $\text{I}_{\text{Mg}}^{2+}$ defect diffuses far away (e.g. to grain boundary or electrode), the remaining Ag_{Mg} defect will finally act as the electron trap and is the source of charge compensation. In the previous study, we showed that Mg diffuses easily in Mg_2Si via the interstitial position [43].

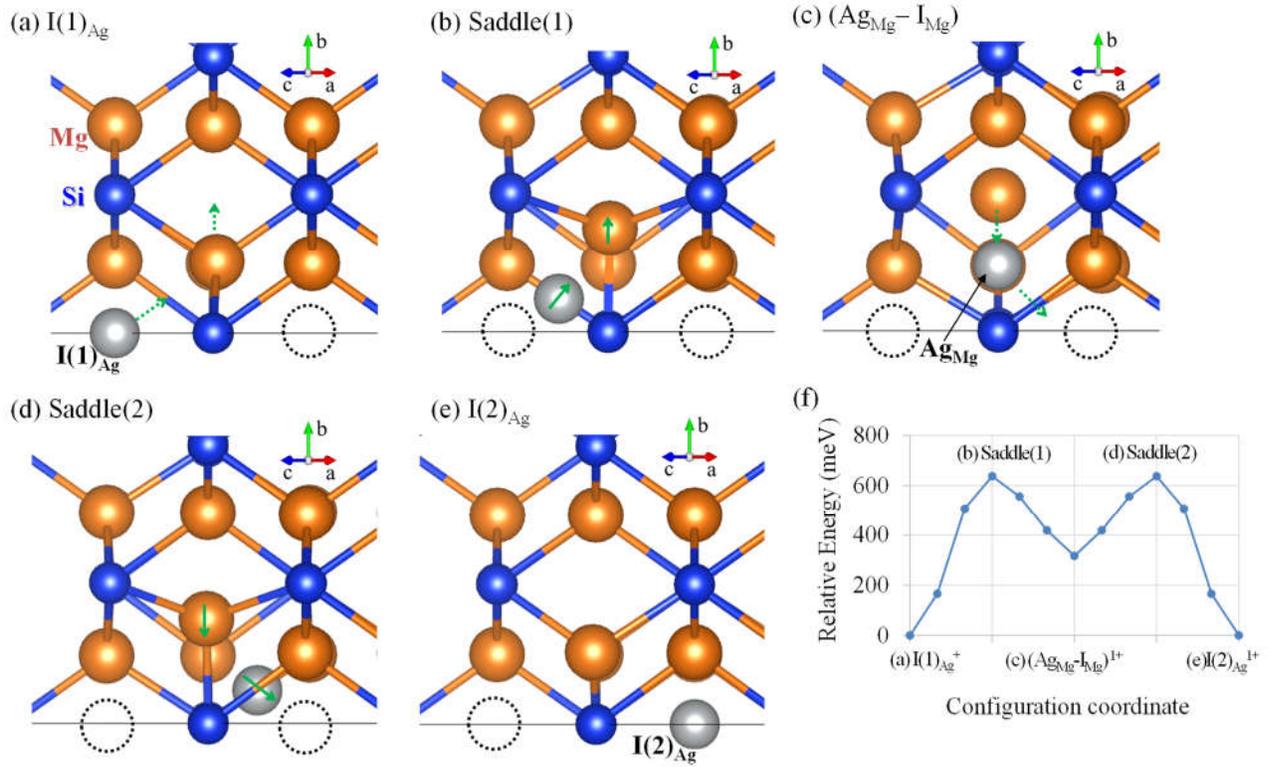


Figure 5: Suggested diffusion mechanism of Ag in Mg_2Si . The individual steps are presented in (a)-(e). The calculated relative energies of configuration coordinates during Ag diffusion are given in (f). (Color should be used in print).

Figure 5 (a), (b), (c), (d) and (e) shows the atomic configurations during the Ag diffusion. For the interstitial diffusion of I_{Mg} , we consider the initial configuration of the I_{Ag}^{1+} defect in Mg_2Si (**Figure 5** (a)) and the intermediate configuration of the defect complex of $(Ag_{Mg}-I_{Mg})^{1+}$ (**Figure 5** (c)). The defect I_{Ag} can be transformed into an Ag_{Mg} and an I_{Mg} defect. In this step-1, the I_{Ag} defect moves toward an Mg site to form Ag_{Mg} . At the same time, the pushed Mg atom moves to one of the adjacent interstitial sites to form I_{Mg} . These diffusion steps are described by the saddle 1 presented in **Figure 5** (b). **Figure 5** (f) shows the relative energy between the configurations during the diffusion path. Note that the energy for the intermediate state of $(Ag_{Mg}-I_{Mg})^{1+}$ is higher by 0.359 eV than that for the initial configuration state of I_{Ag}^{1+} , and the migration energy barrier of the “saddle 1” step is found to be 0.652 eV. After this step-1 ((**Figure 5** (a), (b) and (c)), the $(Ag_{Mg}-$

I_{Mg}^{1-} defect cluster can be transformed again into a single I_{Ag}^{1+} defect at an adjacent interstitial position. The Mg at the interstitial site can push the Ag atom at the Mg site (“*saddle 2*”, (**Figure 5 (d)**), and then the pushed Ag_{Mg} moves to one of the adjacent interstitial sites (**Figure 5(e)**). Thus, Ag_{Mg} and I_{Mg} can be combined into a single I_{Ag} interstitial defect: we call this step-2. This step is the exothermic reaction with the energy difference of 359 meV with a migration energy barrier of 293 meV. Note that the exothermic reaction step-2 is the reverse process of step-1. Depending on the diffusion path, the I_{Ag} can be located at the original interstitial site or at a next lattice interstitial site via combination of step-1 and step 2. Thus, with multiple repetitions of step-1 and step-2, the Ag defect can easily diffuse throughout the Mg_2Si in the form of I_{Ag}^{1+} . During the diffusion of I_{Ag}^{1+} , the decomposed defect of I_{Mg}^{2+} can separately diffuse back into the electrode region. Then the remaining Ag_{Mg}^{1-} defects can cause the charge compensation of electron carriers which were donated by Bi donors.

From the charged defect formation energies, we found that when E_F is at the CBM, the defect formation energy of I_{Ag} is ranging between 0.88 and 0.53 eV in Mg_2Si and Mg_2Sn . Therefore, the diffusion barrier, the sum of the defect formation energy and the migration energy barrier, is calculated to be 1.2-1.5 eV, which is comparable to the activation energy of 1.15 eV reported in section 2.1.

From the defect density equation given above, an increase in T leads to an increase of defect density. Consequently, Ag related defects are expected to be higher in number as T increases, and so is the compensation effect. The number of Bi-related defects on the other hand, most likely doesn't increase with temperature, as there is no source for new Bi incorporation and the defect configuration is frozen after material synthesis. However, a quantitative comparison between the experimental results and the predictions by DFT are difficult as, first, the carrier concentrations are

also affected by the (unknown) Mg content/Mg chemical potential in the samples and second, we are clearly not in an equilibrium situation.

In n-type Mg_2Sn , as presented in **Figure 4** (b), Bi_{Sn} is the most energetically stable defect. Similar to Bi_{Si} , it is a single shallow donor. The defects with the next lowest formation energies are Ag_{Sn} and Ag_{Mg} . However, in the chemical potential range of $E_F = -0.2 \sim 0$ eV (E_{CBM}), Ag_{Sn} is a neutral defect ($q = 0$) and therefore doesn't affect charge carrier concentration. Ag_{Mg} is a single acceptor, which basically compensates the carriers provided by Bi_{Sn} , just like it did for Mg_2Si .

These observations complete the experimental results discussed in the previous section, where a change in the Seebeck values of both binaries was observed near the contacting interfaces. We also conclude that a similar behavior can be expected for Mg_2Si and Mg_2Sn n-type solid solutions. In all cases, Ag_{Mg} defects are expected to trap conduction electrons provided by $\text{Bi}_{\text{Si/Sn}}$, leading to a depletion of carrier concentration. Such results are detected experimentally as an increase of the Seebeck values (in absolute value), which fits with the experimental results of **Figure 3** and explains the findings of previous reports [22] and [25].

Figure 4 (e) and (f) show the defect formation energies for Mg_2Si and Mg_2Sn doped with Li and Ag under Mg-poor conditions, as p-type samples are synthesized with Li substituting Mg. It is worth noticing on **Figure 4** (e) that the Fermi level in Mg_2Si is pinned deep inside the band gap, which explains the experimental challenges in making good p-type Mg_2Si [19, 65]. For Mg_2Sn , Li doping can induce p-type conduction under Mg-poor conditions due to the narrow band gap, while Li hardly gives p-type characteristics under Mg-rich conditions (see Supplementary Material).

In contrast to Ag defects in n-type $\text{Mg}_2\text{Si/Sn}$, the Ag related defects in p-type $\text{Mg}_2\text{Si/Sn}$ doped with Li have much higher formation energies than major Li defects. This means that the addition of Ag doesn't influence the p-type conduction determined by Li defects.

As for p-type $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ studied here and in [22], a behavior similar to Mg_2Sn is expected, as the samples are Mg_2Sn rich (70 and 60%). Li-related defects are expected to be the most stable, and Ag-related defects to have high enough formation energies so that no doping effect would be experimentally detectable in a Seebeck mapping, as is experimentally observed. Similarly, the hybrid-DFT calculation results confirm that, for $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$, Li is a better p-type dopant than Ag. In such analysis, it is important to keep in mind potential interactions between the electrode and the TE material, as well as the resulting interfaces between them. In our case, the actual diffusion process of Ag is presumably more complex than considered here. As shown in [22], Ag and $\text{Mg}_2(\text{Si},\text{Sn})$ are practically not in direct contact but are separated by an Ag containing intermetallic layer. This, as well as potential other diffusion paths inside the thermoelectric material, will influence the diffusion of Ag, and a microscopic model is required to analyze this in depth. Nevertheless, the Seebeck coefficient profile predicted based on our simple diffusion model shows good agreement with the actual experimental $S(x)$, as shown in **Figure S 1** of the Supplementary Material. Thus, due to the good qualitative and quantitative agreement between experiment and calculation in our work, we believe our effective model provides valuable insight.

Technologically, it is also important to keep in mind that Ag diffusing into the n-type $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ causes a loss of major charge carriers; hence the functional material does not possess its optimum thermoelectric properties anymore, which leads to the degradation of the TE device. To illustrate this, a comparison between the properties of $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ before and after joining is presented.

To calculate zT and the efficiency of the pristine sample (before contacting), electrical resistivity and thermal conductivity, ρ and κ , data was taken from previous measurements [18]. For contacted samples, properties as observed at the interface were assumed for the whole sample, taking the interface properties as hypothetical equilibrium state after Ag saturation. As local experimental measurements of the conductivities were unfeasible and using a simple SPB model to approximate

carrier concentration from S then approximating ρ and κ does not hold at high temperatures (contribution of minority charge carriers becomes substantial), the needed thermoelectric properties were taken from literature which provides a full TE study of a sample with similar S as observed at the interface of **Figure 3** [68]. Therefore, the following calculations are rough estimations due to certain differences between the literature and our current work (synthesis method, dopant...). However, these effects are expected to be minor and the general trend in zT and efficiency is believed to be similar. More details about the calculation and approximation procedures are provided in section III in the Supplementary Material.

The initial TE material is synthesized and doped to have optimum carrier concentration which guarantees maximum zT . Any loss of majority charge carriers caused by Ag diffusion, for example, results in a decrease in zT as schematically shown in **Figure 6**.

Simulation results also show that, for an $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$ leg of 5 mm length with a hot side temperature of 700 K and a cold side temperature of 300 K, the loss of carriers corresponds to a decrease of maximum efficiency from 10.5% to 7.2% and of maximum power output from 0.028 to $0.013 \times 10^6 \text{ W m}^{-2}$. Further decrease in these values is expected to occur as Ag continues diffusing inside the TE material and might alter its TE properties further beyond what we assumed to be the equilibrium state. This also establishes the importance of defect consideration in contacting electrode selection and module building.

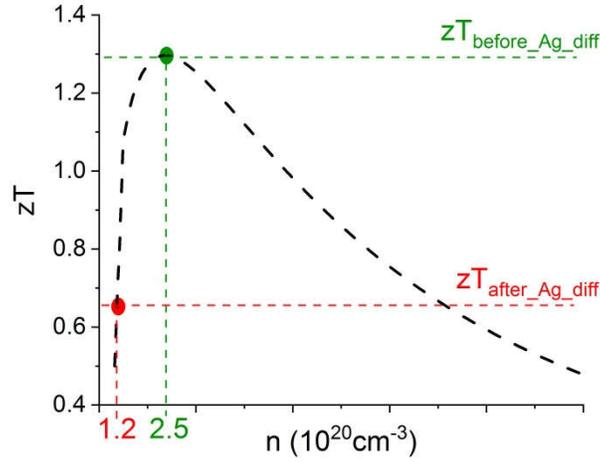


Figure 6: Schematic dependence of zT on carrier concentration for n -type $Mg_2Si_{1-x}Sn_x$ before and after Ag diffusion at $T = 700K$.

5. Conclusion

In this work, we re-assess the selection of Ag as a contacting solution for $Mg_2Si_{1-x}Sn_x$ -based thermoelectric generators by describing the Ag diffusion mechanism and correlating unexpected experimental results with hybrid-DFT defect calculations. The observed change in Seebeck values of n -type binaries Mg_2Si , Mg_2Sn and their solid solutions is explained by Ag_{Mg} defects which have low enough formation energy to counteract Bi-related defects and cause a diminution in charge carrier concentration. This qualitative agreement between experiments and calculations establishes the credibility of both methods, as well as the importance of a potential doping effect of the contacting electrode. Thus, we clearly show that, Ag is not a suitable electrode for n -type Mg_2X without further technological steps (e.g. diffusion barriers).

Furthermore, we show that the intrinsic and extrinsic defects of the considered TE material and the joining material are important criteria to consider while screening for contacting electrodes.

CRedit authorship contribution statement

Sahar Ayachi: Methodology, Validation, Formal analysis, Investigation, Writing - original draft, Visualization.

Radhika Deshpande: Validation, Investigation.

Prasanna Ponnusamy: Software, Validation.

Sungjin Park: Software, Validation, Formal analysis, Investigation (theoretical).

Jaywan Chung: Software.

Sudong Park: Software, Validation, Writing - review & editing, Supervision, Funding acquisition.

Byungki Ryu: Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation (theoretical), Writing – original draft, Project administration, Funding acquisition.

Eckhard Müller: Writing - review & editing, Supervision.

Johannes de Boor: Conceptualization, Methodology, Writing - review & editing, Supervision, Project administration.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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The raw/processed data required to reproduce these findings cannot be shared at this time due to legal or ethical reasons.

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