Numerical Investigation of Combustion Instabilities in a Rocket Combustion Chamber with Supercritical Injection Using a Hybrid RANS/LES Method

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An experimentally measured model rocket combustion chamber is investigated numerically using a time resolving high order hybrid RANS/LES method. The selected operation point is characterized by weak combustion instabilities which are challenging to predict. The aim of this work is to enhance the prediction capabilities of combustion chamber instabilities by numerical methods. This aims on a better understanding of the reasons for combustion instabilities as well as on techniques to avoid them. The weak oscillating combustion instabilities found in experiment and simulation are analyzed in detail.

I. Introduction

Since the beginning of rocket development, combustion instabilities are an important subject of investigations. First discovered in the late 1930s, unstable oscillations were found in many, if not all rocket combustion chambers. They involve extreme loads in both low and high frequencies. The loads can be so severe that they cause a complete failure of the combustion chamber. This is especially critical for manned missions. To avoid this, the F-1 engine of the Saturn V rocket for example was tested over 2000 times in full-scale to solve problems with combustion instabilities. This causes enormous costs in the process of design.

Experimental investigations of rocket combustion chambers are often challenging due to extreme flow conditions. The propellants are injected cryogenically and/or at very high pressure. Additionally, the combustion products can reach temperatures up to roughly 4000 K. Diagnostic possibilities in rocket combustion chambers are still limited due to these extreme conditions. Even in simplified model combustors, dynamic and static combustion chamber pressures, static wall temperatures and heat flues are often the only values measured quantitatively. Dynamic temperature measurements are often inaccurate due to the high response time of the sensors. In some cases it is also possible to install quartz windows in model rocket combustors to allow optical access. This makes capturing of shadowgraphs and OH*-chemiluminescence pictures possible. Quantitative optical diagnostics like laser-based flow field measurements are still impossible in most rocket combustion chamber flows.

Numerical simulations can support the design process of combustion chambers in combination with experiments. Good validated Computational Fluid Dynamics (CFD) codes can improve the understanding of the flow field behaviour in connection with experimental data. The full knowledge of the flow field enables analyses of the causes of combustion chamber instabilities, which can be verified in specially designed experiments. Up to now it is impossible to perform Direct Numerical Simulations (DNS) for rocket combustion chambers even for simple geometries as the one presented in this paper. The fine grids needed for DNS to resolve the fine turbulent scales in combination with the small timescales of combustion would require too much computing resources. To minimize the computational effort, the small scale turbulence can be modeled, while only the large scales are resolved. This is the concept of the Large-Eddy Simulation (LES).

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However, especially close to solid walls a good resolved LES requires still extremely fine grids in each coordinate direction to resolve the turbulence in the boundary layer accurately. On the other hand, impact of the near wall region on the main flow can be predicted properly by modern Reynolds-Averaged Navier-Stokes (RANS) turbulence models at relatively low costs. Therefore, to further reduce the computational effort, hybrid RANS/LES methods were proposed, where the near wall region is simulated by RANS and the main flow by LES. This principle is used in the in-house code Turbulent All Speed Combustion Multigrid Solver 3D\textsuperscript{2} (TASCOM3D) to simulate combustion instabilities in rocket combustion chambers.

In the present paper, the experimentally investigated single injector rocket combustion chamber BKC\textsuperscript{3,4} is studied numerically. The chosen operation point (OP) is characterised by weak oscillations and is described in detail in Sec. II. In former investigations, the occurring instabilities could not be reproduced by inexpensive 2D-Unsteady Reynolds-Averaged Navier-Stokes (URANS) simulations.\textsuperscript{5} Hence, the same operation point is simulated again using a hybrid RANS/LES method called improved Delayed Detached Eddy Simulation (iDDES) which is described in detail in Sec. III. The results are presented and discussed in Sec. IV.

II. Test case description

The investigated single injector combustion chamber BKC has been built and experimentally investigated at DLR Lampoldshausen.\textsuperscript{3,4} It has been designed to map the operating point of real upper stage engines. The combustion chamber is of cylindric shape and is completed by a convergent-divergent nozzle. Fig. 1 shows the axisymmetric BKC in a two dimensional plane. Furthermore geometric details are given in Table 1.

The combustion chamber can be operated with different fuel-oxidizer mixtures like hydrogen with oxygen or methane with oxygen. The mean combustion chamber pressure can be varied over a wide range from sub- to supercritical with respect to the critical pressure of oxygen. The injection temperature can be chosen from cryogenic to ambient. The test case discussed in this paper is a combustion of H\textsubscript{2} and O\textsubscript{2} at supercritical pressure (60 bar) with cryogenic injection (injection temperature is \(\sim\)120 K). Thus, the conditions are similar to the operation point of the Vinci upper stage engine of the Ariane 6 rocket.\textsuperscript{6} A detailed description of the operation point is also given in Table 1.

Through the coaxial injector, O\textsubscript{2} and H\textsubscript{2} are injected separately. Mixing takes places directly downstream of the face plate where the diffusion flame is anchored. Shadow images have been captured through an optical access at the injector region. The dimension of the window is 100 mm \(\times\) 25 mm (location: see Fig. 1). To minimize the thermal loads on the window, a H\textsubscript{2} cooling film is injected directly at the combustion chamber wall. Pressure sensors map the combustion chamber pressure during the firing test. Two monitor points (MP1 and MP2) at which the time signal of the pressure is analyzed in the simulation are also shown in Fig. 1.

As already mentioned, the chosen operation point exhibits weak oscillations only. The amplitude of the pressure oscillation is clearly below 1\%. This makes an accurate prediction of the combustion instabilities challenging as these oscillations may be damped by numerical dissipation.

![Figure 1. Geometry of the axisymmetric combustion chamber scaled in \(x\)-direction by a factor of two. MP1 and MP2 indicate the locations of monitor points.](image-url)
Table 1. Geometrical and operative details.

<table>
<thead>
<tr>
<th>Geometrical details (specified in mm)</th>
<th>Operative details</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of injectors</td>
<td>1</td>
</tr>
<tr>
<td>Length of the combustion chamber</td>
<td>430</td>
</tr>
<tr>
<td>Diameter of the combustion chamber</td>
<td>50</td>
</tr>
<tr>
<td>Diameter of the nozzle throat</td>
<td>16.8</td>
</tr>
<tr>
<td>Diameter of the O&lt;sub&gt;2&lt;/sub&gt;-injector</td>
<td>4.0</td>
</tr>
<tr>
<td>Inner diameter of the H&lt;sub&gt;2&lt;/sub&gt;-injector</td>
<td>4.4</td>
</tr>
<tr>
<td>Outer diameter of the H&lt;sub&gt;2&lt;/sub&gt;-injector</td>
<td>6.5</td>
</tr>
<tr>
<td>Height of the cooling film</td>
<td>1.0</td>
</tr>
<tr>
<td>Combustion chamber pressure (bar)</td>
<td>59.4</td>
</tr>
<tr>
<td>Oxidizer to fuel ratio (injector)</td>
<td>4.83</td>
</tr>
<tr>
<td>Global oxidizer to fuel ratio</td>
<td>1.00</td>
</tr>
<tr>
<td>Injection temperature O&lt;sub&gt;2&lt;/sub&gt; (K)</td>
<td>115.5</td>
</tr>
<tr>
<td>Injection temperature H&lt;sub&gt;2&lt;/sub&gt;, injector (K)</td>
<td>117.0</td>
</tr>
<tr>
<td>Injection temperature H&lt;sub&gt;2&lt;/sub&gt;, cooling film (K)</td>
<td>320.5</td>
</tr>
<tr>
<td>Mass flow rate O&lt;sub&gt;2&lt;/sub&gt; (kg/s)</td>
<td>0.29</td>
</tr>
<tr>
<td>Mass flow rate H&lt;sub&gt;2&lt;/sub&gt;, injector (kg/s)</td>
<td>0.06</td>
</tr>
<tr>
<td>Mass flow rate H&lt;sub&gt;2&lt;/sub&gt;, cooling film (kg/s)</td>
<td>0.23</td>
</tr>
</tbody>
</table>

III. Numerical method

All simulation are performed with the in-house code TASCOM3D. TASCOM3D solves the full set of the three-dimensional compressible Navier Stokes equations containing conservation equation of mass, momentum and energy. Additionally for combustion, the conservation equations of a number of species are solved.

For the described test case, former investigations have shown, that numerical methods with low computational effort like 2D-URANS simulations did not resolve the weak oscillations. Therefore, a high order hybrid RANS/LES method (iDDES) is used. The near wall region is simulated by URANS using the k-ω turbulence model of Wilcox while in the core flow a LES is performed. The switching between RANS and LES regime is performed automatically by suitable transition functions.

TASCOM3D uses a central spatial discretization of 6<sup>th</sup> order with a small amount of upwind discretization of 5<sup>th</sup> order with Multi-Dimensional Limiting Process - Low Dissipation (MLP<sup>ld</sup>). In contrast to conventional Total Variation Diminishing (TVD) limiters, the MLP<sup>ld</sup> scheme uses additional informations from diagonal volumes to improve shock resolution and convergence. The calculation of the inviscid fluxes is based on the Advection Upstream Splitting Method<sup>+</sup>-up (AUSM<sup>+</sup>-up). The temporal discretization is done fully implicit by a Backward Differentiation Formulas (BDF) method of up to 3<sup>rd</sup> order. All entries of the required Jacobian matrix are set up analytically. The time integration is realized by a dual time stepping method. The inner iteration is assumed to be converged when the global residuum has decreased by at least three orders of magnitude. To enhance convergence, an all-Mach number preconditioning is implemented.

Finally the nonlinear system of equation is solved using a Lower-Upper Symmetric Gauß-Seidel (LU-SGS) method. The high pressures and cryogenic temperatures occurring in the BKC do not allow the use of the Ideal Gas Equation of State (IG-EOS) to complete the equation system. Instead, the real gas behavior is described by the Soave-Redlich-Kwong Equation of State (SRK-EOS). The thermodynamic properties of the gas mixture is described by the model of Huber and Hanley. Combustion is modeled with detailed Finite-Rate Chemistry (FRC) using the reaction mechanism of Ó Conaire. This mechanism includes 8 species and 20 reactions. The Turbulence/Chemistry Interaction (TCI) is modeled by a multivariate assumed Probability
IV. Results and discussion

A. Analysis of grid resolution

To check the quality of a LES grid, many different criteria are commonly used. Here, the amount of resolved turbulent kinetic energy and two-point correlations are applied. According to Pope \cite{Pope1992} a good LES resolution is achieved if more then 80% of the total turbulent kinetic energy is resolved. A corresponding parameter $\gamma$ is calculated by \cite{Davidson2000, Davidson2001}

$$\gamma = \frac{k_{res}}{k + k_{res}}, \quad k_{res} = \frac{1}{2} \langle u_i' u_i' \rangle,$$

where the modeled turbulent kinetic energy $k$ is taken directly from the subgrid turbulence model.

In contrast, Davidson \cite{Davidson2000, Davidson2001} favours two-point correlations to determine the LES quality of the grid. The two-point correlation of the axial velocity $u$ is calculated as follows

$$B_u(\hat{x}) = \frac{\langle u'(x)u'(x-\hat{x}) \rangle}{\langle u'(x)u'(x) \rangle}.$$  

According to Davidson a good grid resolution is achieved when the decrease of $B_u(\hat{x})$ for $\hat{x} \rightarrow \infty$ expands over more then ten cells. \cite{Davidson2001}

A corresponding analysis has been performed for six points in the combustor which are given in Table 2. The points P1-P3 are located in the highly resolved region close to the injectors: In the shear layer between...
Table 2. Amount of resolved turbulent kinetic energy at six different locations.

<table>
<thead>
<tr>
<th>point</th>
<th>$x$ (m)</th>
<th>$y$ (m)</th>
<th>$z$ (m)</th>
<th>$\gamma$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P1</td>
<td>0.0037</td>
<td>0.0021</td>
<td>0.0</td>
<td>11.90</td>
</tr>
<tr>
<td>P2</td>
<td>0.0080</td>
<td>0.0021</td>
<td>0.0</td>
<td>80.53</td>
</tr>
<tr>
<td>P3</td>
<td>0.0080</td>
<td>0.0232</td>
<td>0.0</td>
<td>93.43</td>
</tr>
<tr>
<td>P4</td>
<td>0.2003</td>
<td>0.0000</td>
<td>0.0</td>
<td>96.01</td>
</tr>
<tr>
<td>P5</td>
<td>0.2003</td>
<td>0.0125</td>
<td>0.0</td>
<td>96.41</td>
</tr>
<tr>
<td>P6</td>
<td>0.2003</td>
<td>0.0234</td>
<td>0.0</td>
<td>95.75</td>
</tr>
</tbody>
</table>

Oxygen and hydrogen (P1, P2) and in the shear layer of the H$_2$ cooling flow (P3, see Figs. 2 and 3). The other three points are further downstream at an identical $x$-position at the symmetry axis, at half the radius and in the transition region between LES and RANS, respectively (see Fig. 3).

The fraction $\gamma$ of resolved turbulent kinetic energy is also given in Table 2. Despite the high grid resolution at point P1 less turbulent kinetic energy is resolved than at all other points. This is due to the switching from URANS to LES. P1 is located in the shear layer directly downstream of the oxygen and hydrogen injectors. The boundary layers of both injector tubes are calculated by URANS, where the turbulent kinetic energy is completely modeled. By convective transport, $k$ passes downstream to P1. Although the point P1 is already in LES regime, the high value of $k$ from the boundary layers are not be converted into resolved fluctuations due to the short distance between the upstream URANS regime and P1. At P2, which is somewhat further downstream, fluctuations have already developed and the flow is basically in the LES regime. As a result, more than 80% of then turbulent kinetic energy is resolved in P2 and the criterion of Pope$^{19}$ is met.

Due to the results concerning the resolved turbulent energy at P1 no meaningful two-point correlation are expected at this point. For all other points from Table 2 two-point correlations are calculated for the axial velocity in $i$-coordinate direction, which basically corresponds to the x-direction. The two-point correlation of these points are shown in Fig. 4. From these figures it can be concluded that the resolution of the LES is good, since the decrease of the correlation extends over more then ten cells.$^{21}$

The strong grid refinement close to the injectors as well as the finest turbulent structures found in this regime indicates an acceptable grid resolution. Also the rear part of the combustion chamber can be assumed to be reasonable resolved although the mesh is significantly coarsened here, because there is a high amount of resolved turbulent kinetic energy and good results from the two-point correlations.

B. Comparison with experiment

As the nozzle is included in the compressible flow simulation, the combustion chamber pressure $P_{CC}$ is part of the solution and is not given as a boundary condition. Therefore, the calculated combustion chamber pressure is a first indication of the quality of the simulation. In the experiment, a mean pressure of $P_{CC} = 59.4$ bar$^{3}$ is obtained. The time averaged pressure from the iDDES is calculated to $P_{CC} = 60.9$ bar. Thus, the combustion chamber pressure is reproduced with an accuracy of $\sim 2.5\%$.

For a further quantitative comparison a Fast Fourier Transformation (FFT) analysis of the pressure signal

![Figure 3. RANS (blue) and LES (red) regime of the iDDES. P1 to P6 indicate points for which statistics are calculated.](image-url)
Figure 4. Two-point correlation for the different locations given in Table 2. Each symbol represents a grid cell.

is performed. In Fig. 5 the power spectral density (PSD) is plotted over the frequency for the experiment and the simulation. Smith et al.\textsuperscript{3} found the first longitudinal (1L) mode at \( \sim 1800 \text{ Hz} \). The simulation also resolves this resonant frequency but somewhat underestimates the amplitude. Because this is the fundamental mode of a standing longitudinal wave, the pressure bellies are located directly at the faceplate and in the nozzle throat. Thus, this pressure fluctuation can be observed at the monitor point MP1 (near the faceplate, see Fig. 1) but not at MP2, which is located in the middle of the combustion chamber. The second longitudinal (2L) mode measured and simulated has a frequency of \( \sim 4000 \text{ Hz} \). Now both MP1 and MP2 have a pressure belly and the mode is observed at both monitor points. Higher modes with significantly lower amplitudes are hardly visible in the simulation. The source of the strong experimentally observed pressure fluctuations at higher frequencies could not be clarified beyond doubt. It is possible that these are interactions with the pressure transducer\textsuperscript{3} and therefore are not seen in the simulation.

For a qualitative comparison of experiment and simulation shadowgraphs recorded in the area of optical access are available. The intensity of the experimentally recorded shadowgraphs depends on the distribution of the refractive index in the flow field.\textsuperscript{22} Since the refractive index depends on density, the intensity of the numerical shadowgraph \( I_{CFD} \) is simply calculated from the second derivative of the density\textsuperscript{23}

\[
I_{CFD} = \left| \frac{\partial^2 \rho}{\partial x^2} \right|
\]

(3)

In the experiment high density gradients cause dark regions in the shadowgraph while in the simulation high density gradients result in high values of \( I_{CFD} \). For a good comparison, the color scale of the simulated shadowgraphs is chosen to tend towards black for high \( I_{CFD} \) values, too. Fig. 6 shows an instant shadowgraph

Figure 5. Comparison of the frequency spectrum from the experiment by Smith et al.\textsuperscript{3} with the simulation.
of the experiment (top) compared to a simulated shadowgraph (bottom). A line of sight integration was performed for the simulation to make the pictures comparable. The overall agreement is good. Despite line of sight pictures are shown, small turbulent structures are visible in the experiment. This is in contrast to the line of sight CFD-result, where small structures are blurred. An explanation for this discrepancy could be that in the experiment the shadow image is not dominated exclusively by the density gradients but also by other phenomena such as the optical density of the cryogenic oxygen, which should be considered. However, in both experiment and simulation it can be clearly seen, how the H₂-jet expands in radial direction (red lines at \( x \approx 0.02 \text{ m} \)). Likewise, the length of the nearly undisturbed O₂-jet is pretty well reproduced by the simulation.

The black regions (low intensity) along the axis of the shadowgraph in the experiment are interpreted as the oxygen core. A comparison of the shadowgraph from the simulation with the corresponding calculated O₂ mass fraction distribution for the same instant of time in the \( z = 0 \) plane is given in Fig. 7. Close to the axis, Fig. 7 shows a good agreement between the shadowgraph and the O₂ mass fraction distribution. Here the shadowgraph is significantly influenced by the density gradients of the heating oxygen. On the other hand the shadowgraph exhibits much more structures in the vicinity of walls compared to the O₂-image. Here, the shadowgraph is influenced by gradients between the high temperature regions of combustion and the cooling film. Nevertheless, the oxygen core length may be well estimated from density gradients.

C. Flow field analysis and discussion

The flow field in the near injector region is dominated by a number of vortices caused by the injected fluids, see Fig. 8. These vortices are, among other things, responsible for flame stabilisation. Fig. 8b shows in detail vortex 1 in the shearlayer between fuel and oxidizer. It can be seen that only oxygen is recirculated. This recirculation is very stable and nearly time independent. The fact that only oxygen is recirculated can be explained by the extreme expansion of the oxygen which is injected cryogenically with a density of about
Recirculation zones close to the injectors: (a) first combustor part, (b) region directly downstream of the injector tubes. Contour plot shows OH mass fraction. Isoline of the stoichiometric mixture fraction $\xi_{st}$ (white line).

1050 kg/m$^3$. An increase in temperature of 100 K decreases the density by factor 7. This forces spreading in radial direction (at $x \approx 0.0035$ m) and subsequently the recirculation of the oxidizer. This strong expansions prevents hydrogen from recirculating.

Fig. 8b also shows where combustion takes place due to increased OH concentration (colors in Fig. 8). The flame stabilizes directly at the injector post, where upstream transported oxygen and the entering hydrogen come together. The white isoline in Fig. 8 indicates the stoichiometric mixture fraction. The mixture fraction of the hydrogen-oxygen combustion is determined based on\textsuperscript{24} by

$$\xi = Y_{H_2} + \frac{1}{9} Y_{H_2O},$$

where $Y$ is the mass fraction of hydrogen and water, respectively. For fast chemistry it can be assumed, that when there is stoichiometry, only products exist. This results in the stoichiometric mixture fraction $\xi_{st} = \frac{1}{9}$ for the hydrogen-oxygen combustion. The recirculation of oxygen caused by vortex 1 and additionally the strong and fast energy release by the combustion of hydrogen and oxygen at high pressures prevents the flame from lifting off.

Two further vortices, which significantly influence the flow of the combustion chamber, are shown in Fig. 8a. In contrast to vortex 1 these vortices fluctuate strongly in time and space. The counter-rotating vortices are caused by the injected hydrogen at the center and the cooling flow at the combustion chamber wall. The extent and position of the vortices depend on the hydrogen injector conditions in interaction with the expanding oxygen jet.

In the combustor a wrinkled flame front is obtained as can be seen in Fig. 9, where the temperature field is shown. It can be seen from this figure that cold oxygen pockets are formed e.g. at $x \approx 0.28$ m. These are even better recognizable in the shadowgraph (Fig. 7). Schmitt\textsuperscript{25} found that such pockets are very stable and resilient to destruction by turbulence. This results in unburned oxygen leaving the combustion chamber despite fuel rich conditions. This is also observed in the experiment.\textsuperscript{4}
Figure 9. Instantaneous temperature field of the BKC in the $z = 0$ slice

Figure 10. Flame index in the $z = 0$ slice. Negative values show non-premixed (diffusion) flames.

In order to investigate the combustion regime (premixed, non-premixed) in more detail, a flame index

$$FI = \begin{cases} \frac{\nabla Y_{H_2} \cdot \nabla Y_{O_2}}{|\nabla Y_{H_2}| |\nabla Y_{O_2}|}, & \text{if } Y_{OH} > 0.1 \% Y_{OH,\text{max}} \\ 0, & \text{otherwise} \end{cases} \quad (5)$$

is calculated based on fuel and oxidizer gradients. This parameter only takes the resolved structures into account and neglects subgrid effects. Negative flame index values indicate non-premixed (diffusion) flames while positive values indicate premixed conditions. The minimum value of OH concentration is used here as an indicator for the flame position. The instantaneous flame index $FI$ for the BKC is plotted in Fig.10 in the $z = 0$ plane. It shows that the entire combustion takes place in a diffusion flame mode. Even at the injector where is strong recirculation a diffusion flame is obtained. This is due to the high reactivity of the hydrogen-oxygen combustion at high pressure.

V. Conclusion

The in-house code TASCOM3D is used to investigate the model rocket combustion chamber BKC numerically at supercritical conditions. The performed simulation is a full three dimensional iDDES. The behavior of the real gas is modeled by the SRK-EOS while combustion is modeled with finite-rate chemistry including aPDF approach.

In the course of the analysis, a study on the grid quality has been performed. According to the calculated amount of resolved turbulent kinetic energy and analysed two-point correlations the grid resolution is found
Results show good agreement with the experiment. The mean combustion chamber pressure is predicted accurately. Moreover, combustion chamber instabilities are resolved in accordance with the experiment. The frequency of this instabilities is determined accurately, while the amplitudes are somewhat underestimated. These combustion instabilities could not be resolved in a previous 2D-URANS simulation. Furthermore, shadow images calculated from the simulation are compared with the experiment. Good agreement is found here as well. The deflection of the hydrogen jet through the expanding oxygen jet as well as the length of the undisturbed oxygen core could be reproduced by the simulation. Finally, the significant vortex structures and their influence on the combustion have been investigated.

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