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## Application and performance evaluation of a parallel solver for energy system models with high spatial and temporal resolution

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Manuel Wetzel

German Aerospace Center (DLR)  
Energy Systems Analysis

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H L R I S



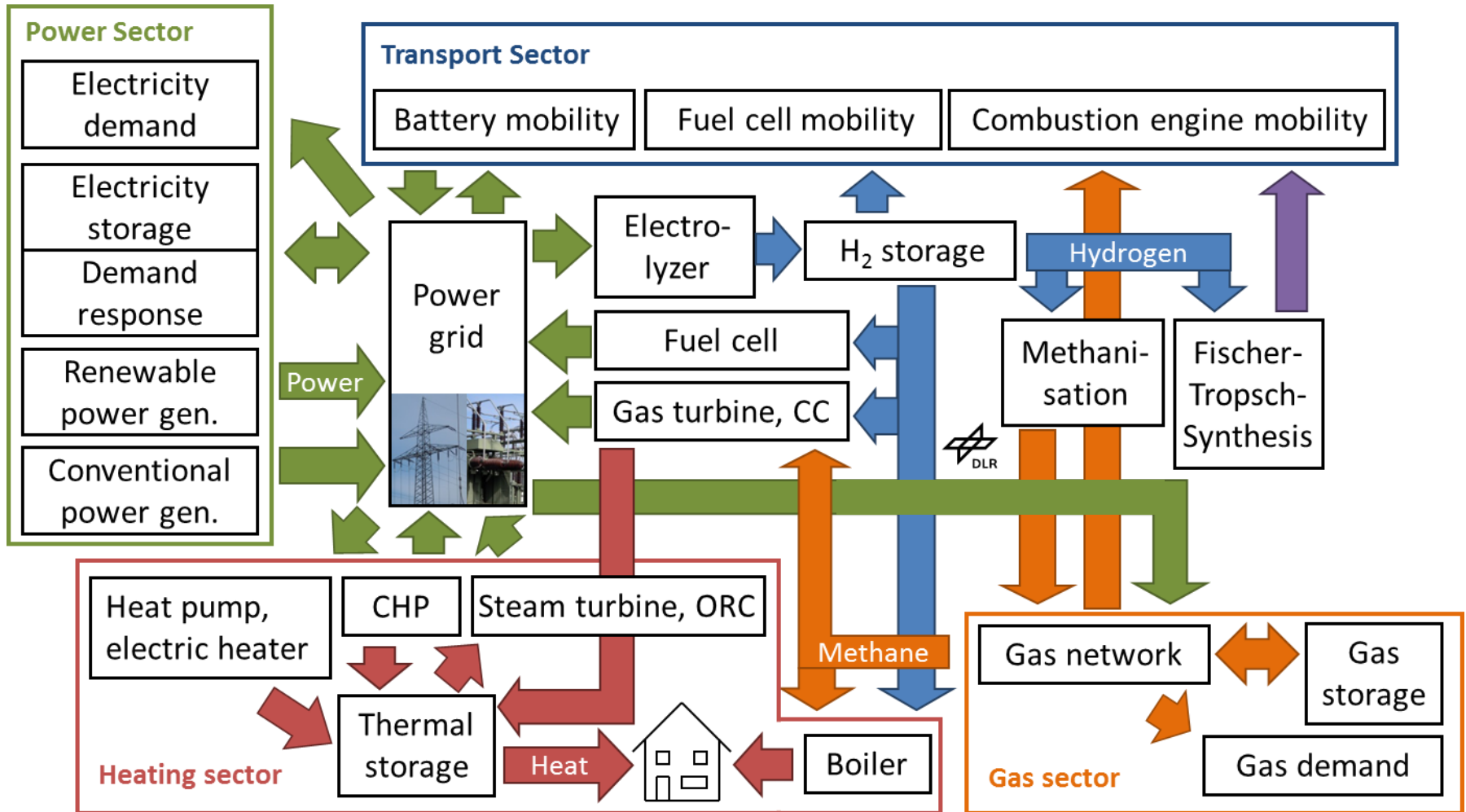
G A M S



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German Aerospace Center



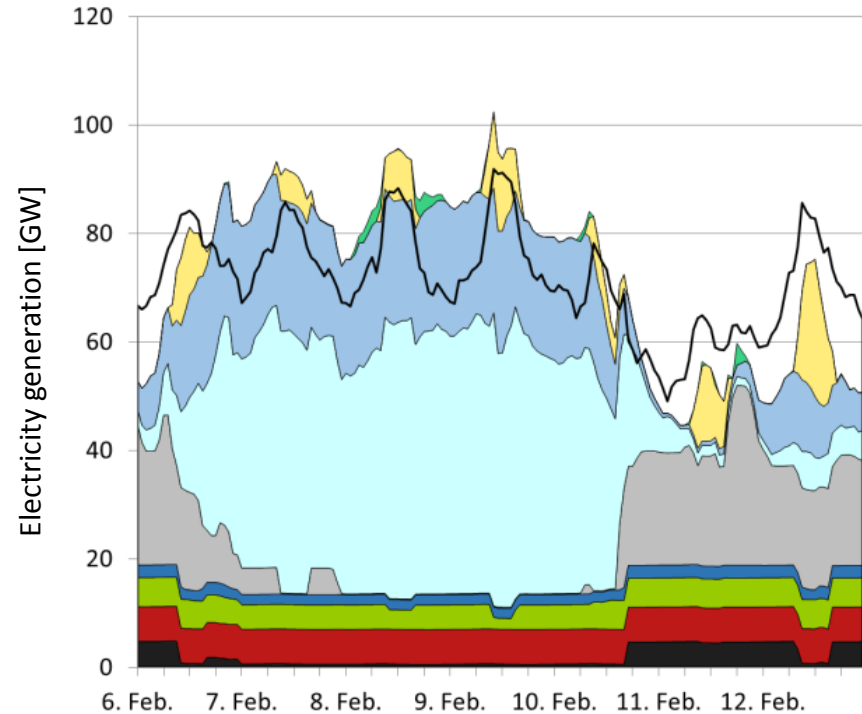
# Increasing energy system complexity



# Dimensionality of REMix problems



60 geographical regions,  
86 AC transmission lines,  
128 HVDC transmission lines

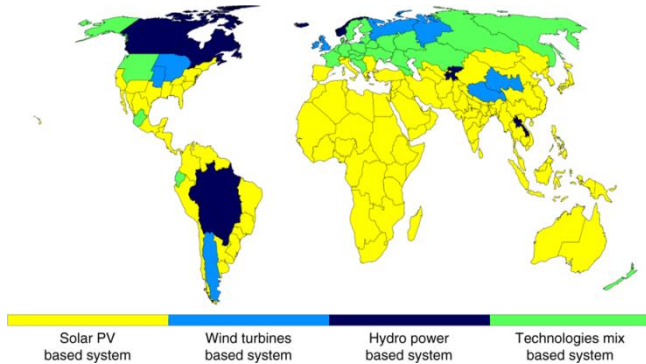


~ 30 technologies  
8760 time steps per year

System cost minimization problems with up to 120 mio. variables and constraints

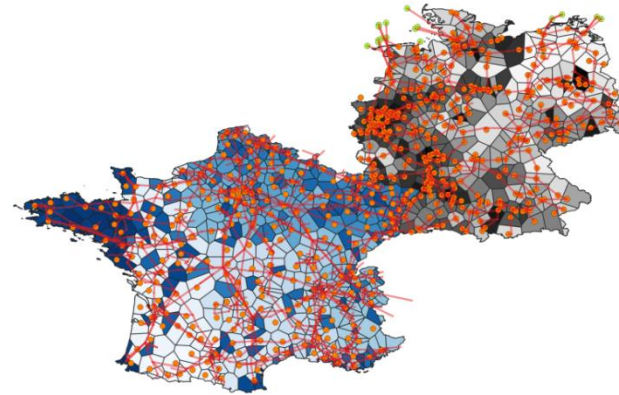
# Trends in energy system models

## Focus on global energy systems



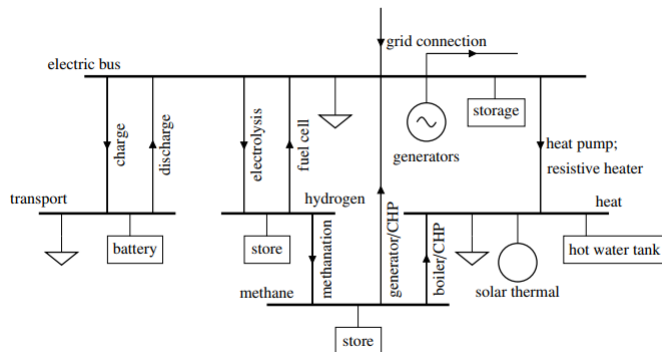
Bogdanov et al., 2019, Radical transformation pathway towards sustainable electricity via evolutionary steps

## Higher spatial resolution



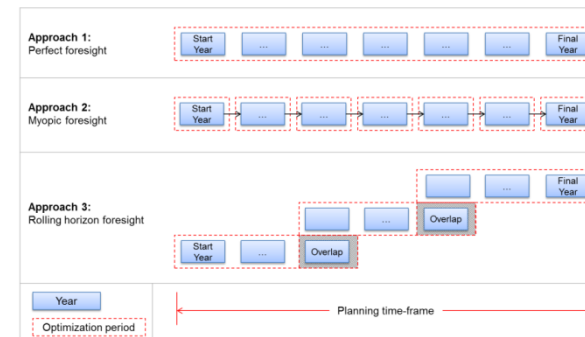
Current work-in-progress from Cao et al.

## Sector integration studies



Brown et al., 2018, Synergies of sector coupling and transmission reinforcement in a cost-optimised, highly renewable European energy system

## Transformation pathways



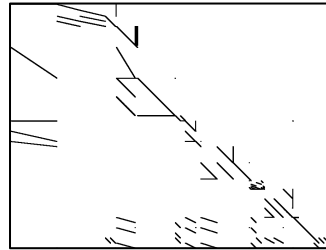
Fichter, 2018, Long-term Capacity Expansion Planning with Variable Renewable Energies

# Solving energy system models

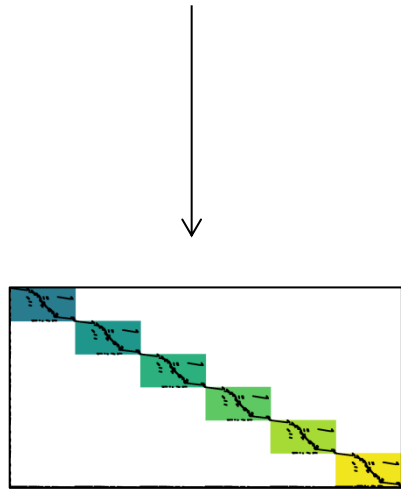
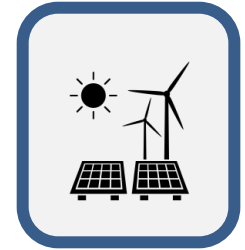
math. formulation

$$\min c \cdot x$$
$$A \cdot x \leq b$$

solver call



optimization results



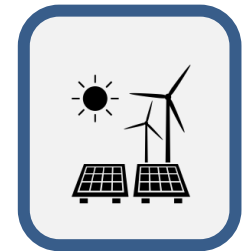
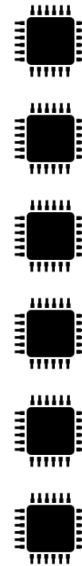
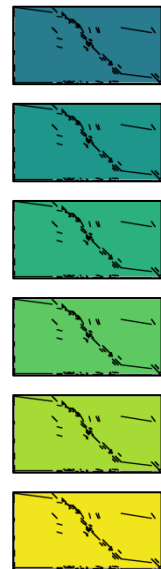
block structure

split and distribute

parallel solve

merge

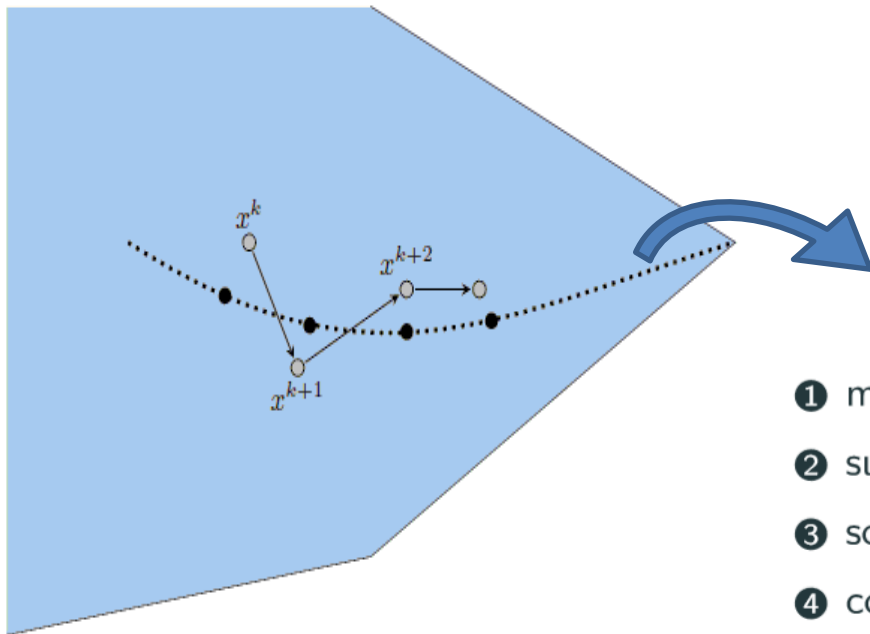
optimization results



Solution approach in a nutshell:

Each step of an interior-point algorithm requires solution of a linear system

This can be parallelized by exploiting a block diagonal structure



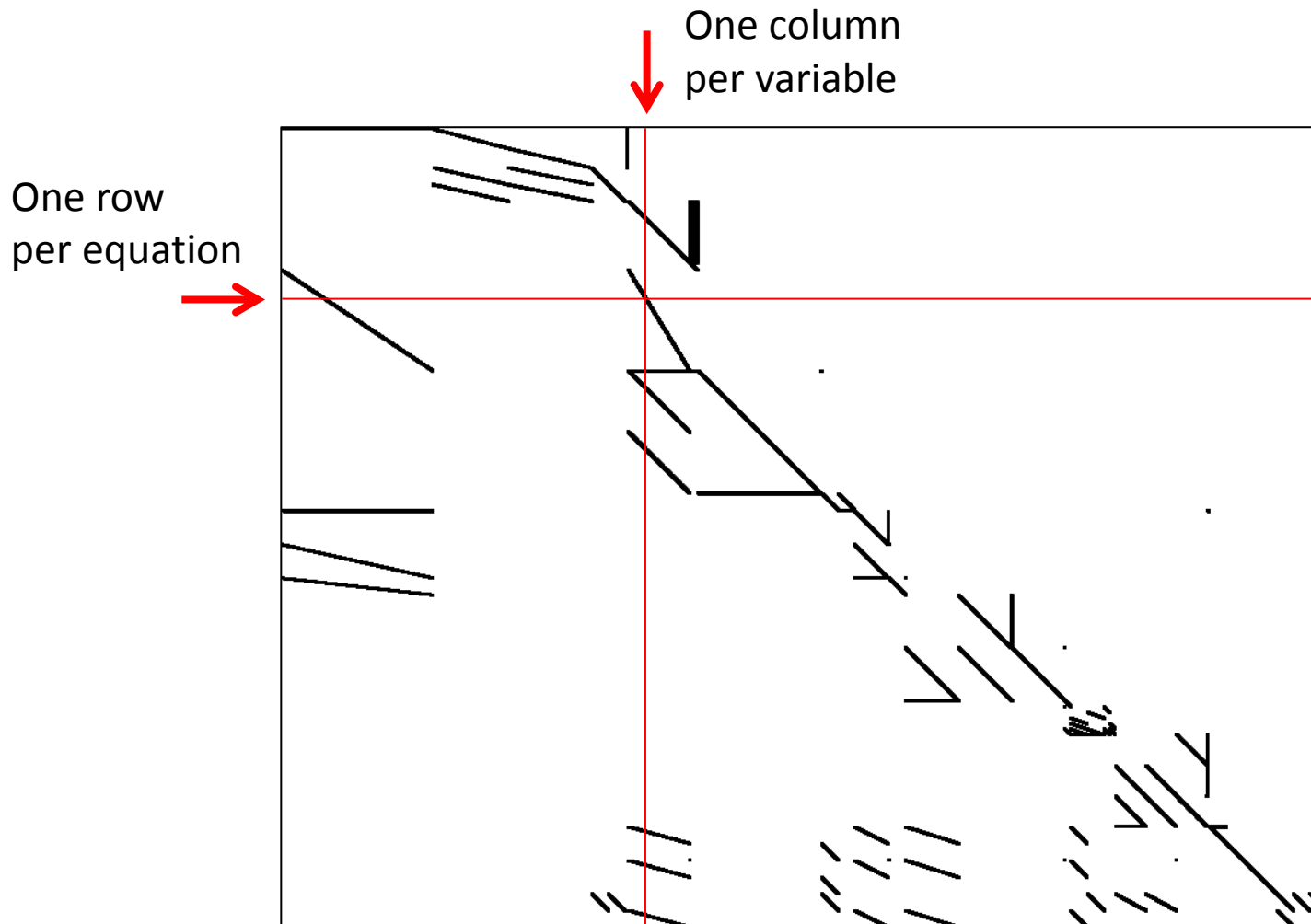
$$\begin{bmatrix} K_1 & & & B_1 \\ & \ddots & & \vdots \\ & & K_N & B_N \\ B_1^T & \dots & B_N^T & K_0 \end{bmatrix} \begin{bmatrix} \Delta z_1 \\ \vdots \\ \Delta z_N \\ \Delta z_0 \end{bmatrix} = \begin{bmatrix} r_1 \\ \vdots \\ r_N \\ r_0 \end{bmatrix}$$

- ① multiply rows  $i = 1, \dots, N$  by  $-B_i^T K_i^{-1}$ .
- ② sum up all rows
- ③ solve  $(K_0 - \sum_{i=1}^N B_i^T K_i^{-1} B_i) \Delta z_0 = r_0 - \sum_{i=1}^N B_i^T K_i^{-1} r_i$ .
- ④ compute  $\Delta z_i, i = 1, \dots, N$ .

D. Rehfeldt, The newly developed PIPS solver, May 24<sup>th</sup> 2019, BEAM-ME Workshop, Aachen

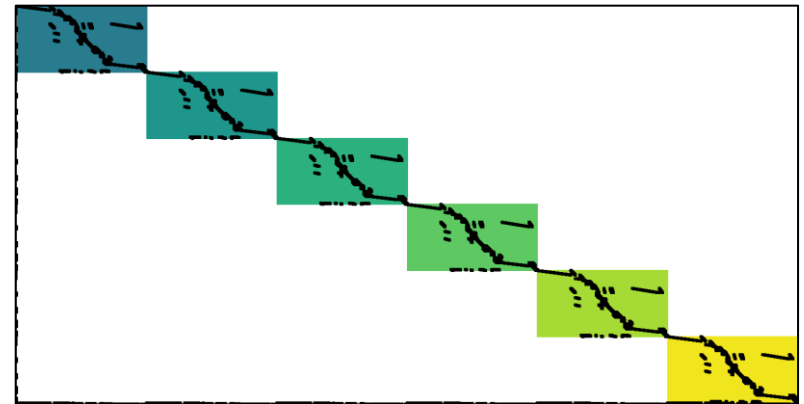
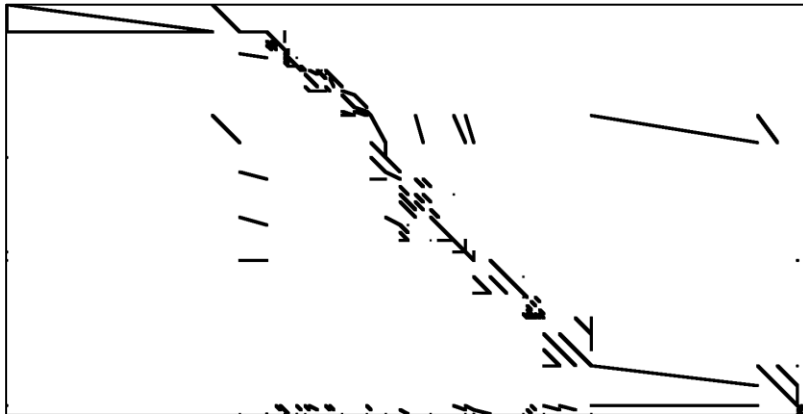
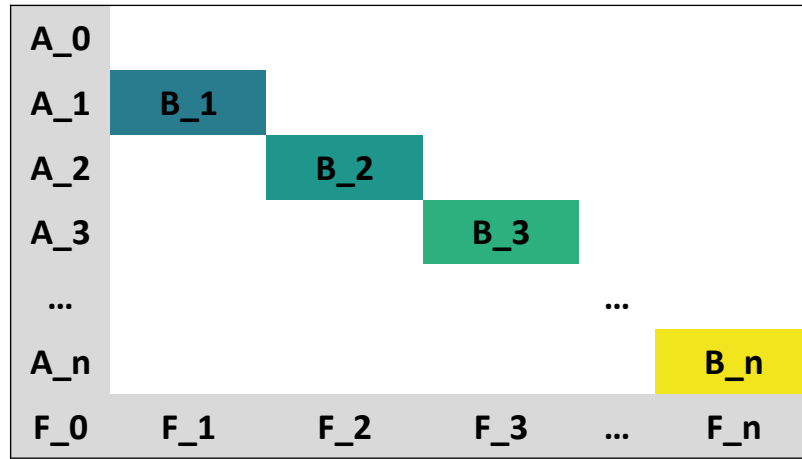
**PIPS-IPM requires a block diagonal structure to solve problems in parallel**

# The optimization matrix



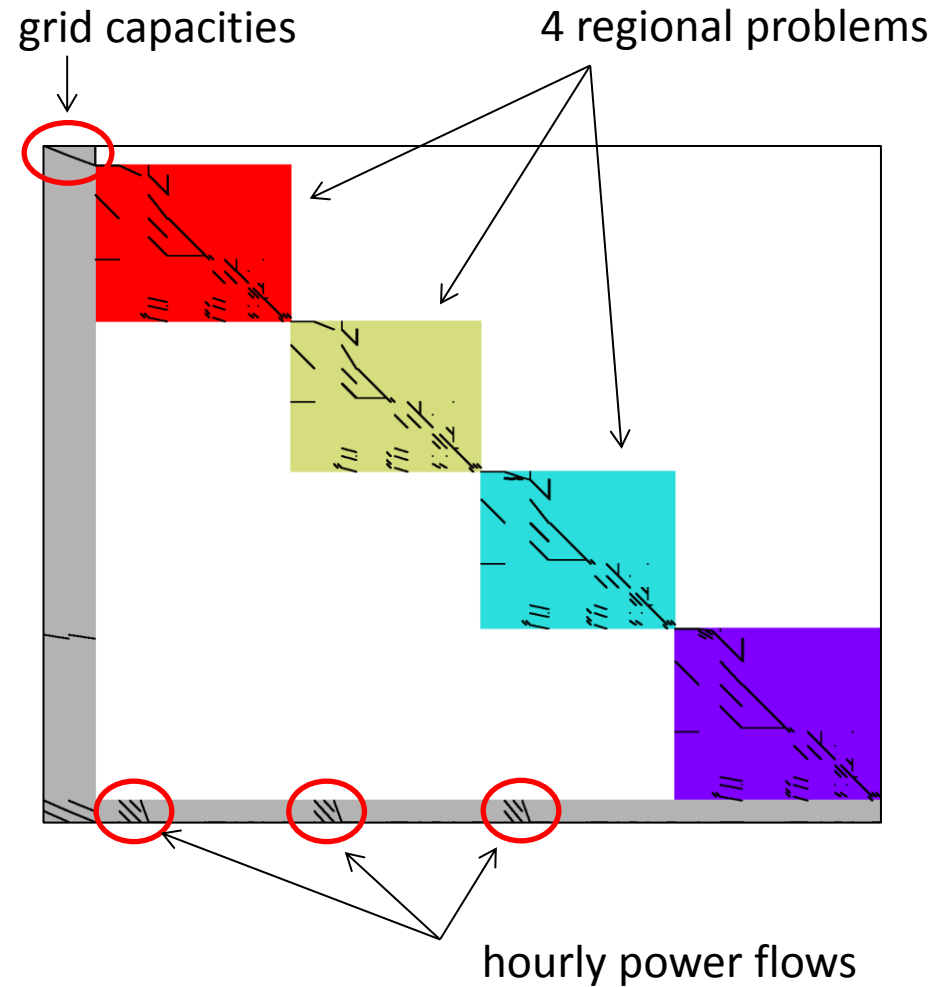
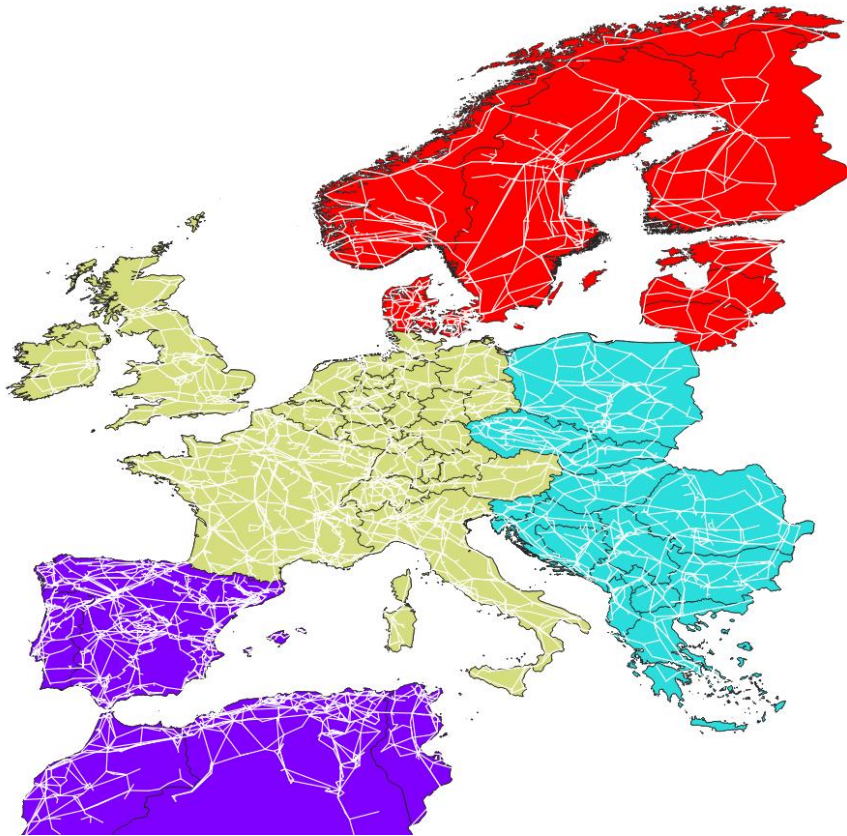
**Rows and columns can be permuted without changing the optimization problem**

# From ESM to PIPS: Annotation



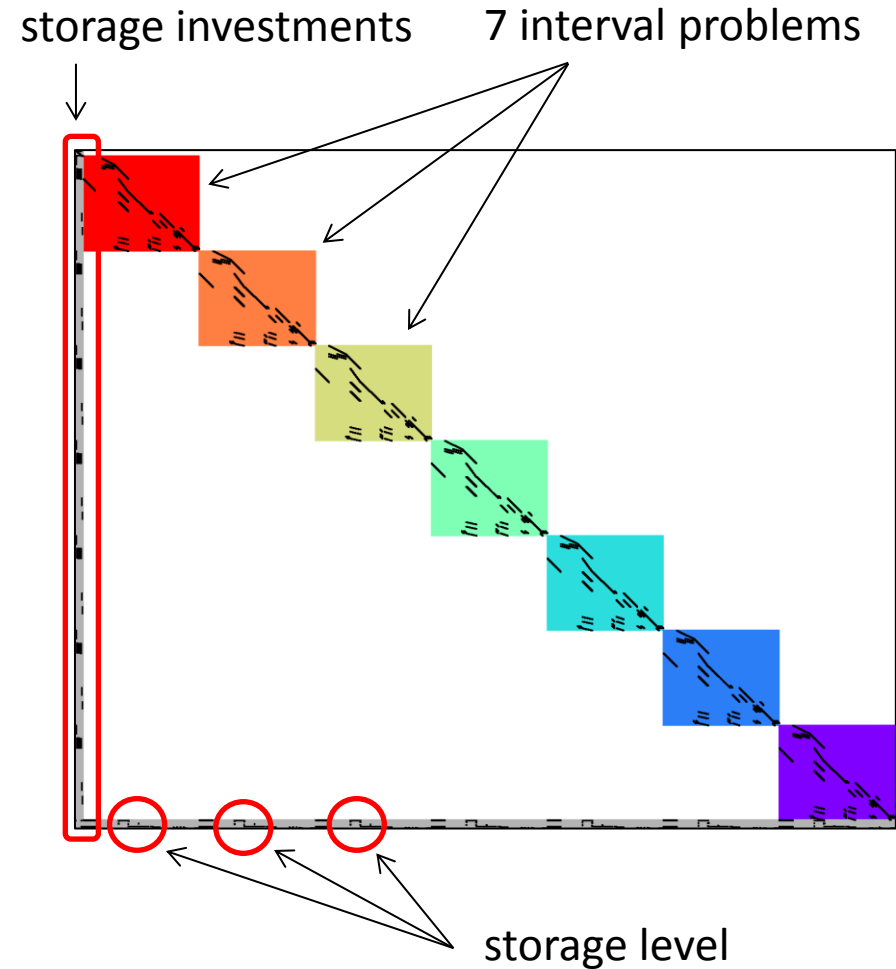
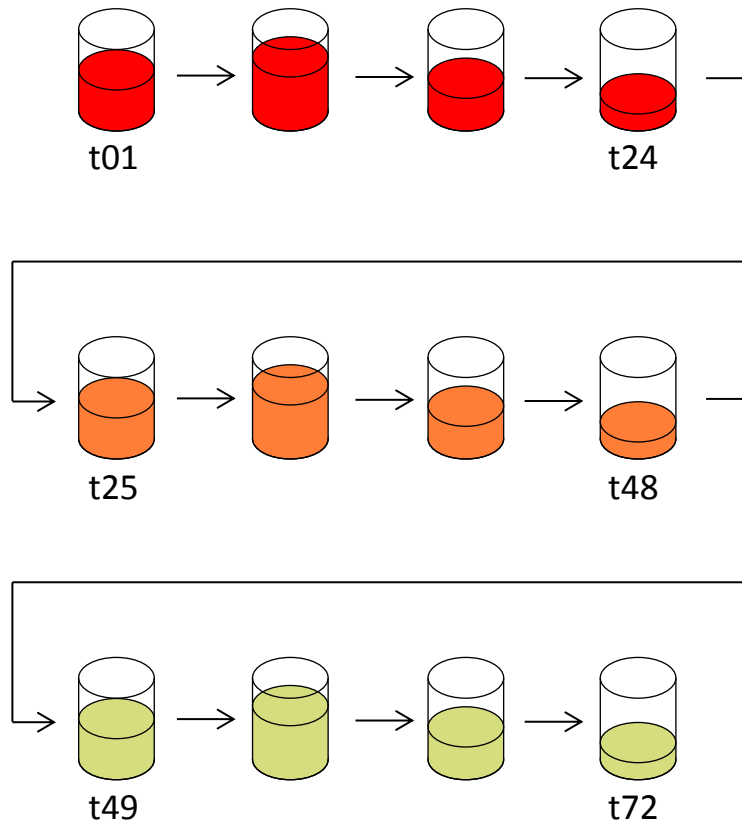
Annotation pre-structures the optimization problem for PIPS-IPM





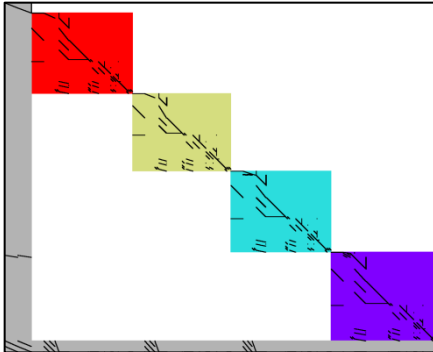
**Linking elements scale with transmission lines and time steps**

# Temporal decomposition



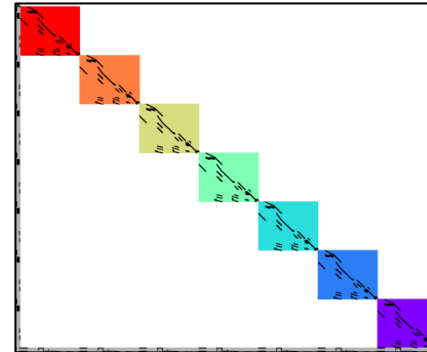
**Linking elements scale with regions and technologies**

Regional decomposition



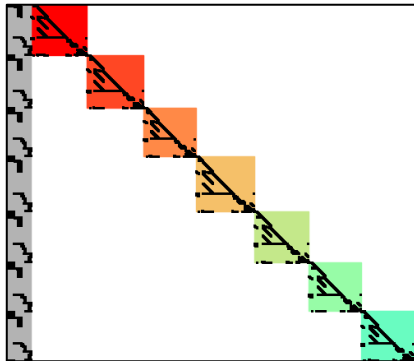
Large number of linking elements

Temporal decomposition



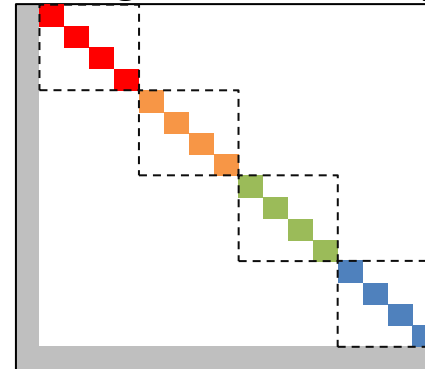
Most promising with up to 8760 blocks

Planning horizon decomposition



Limited number of blocks

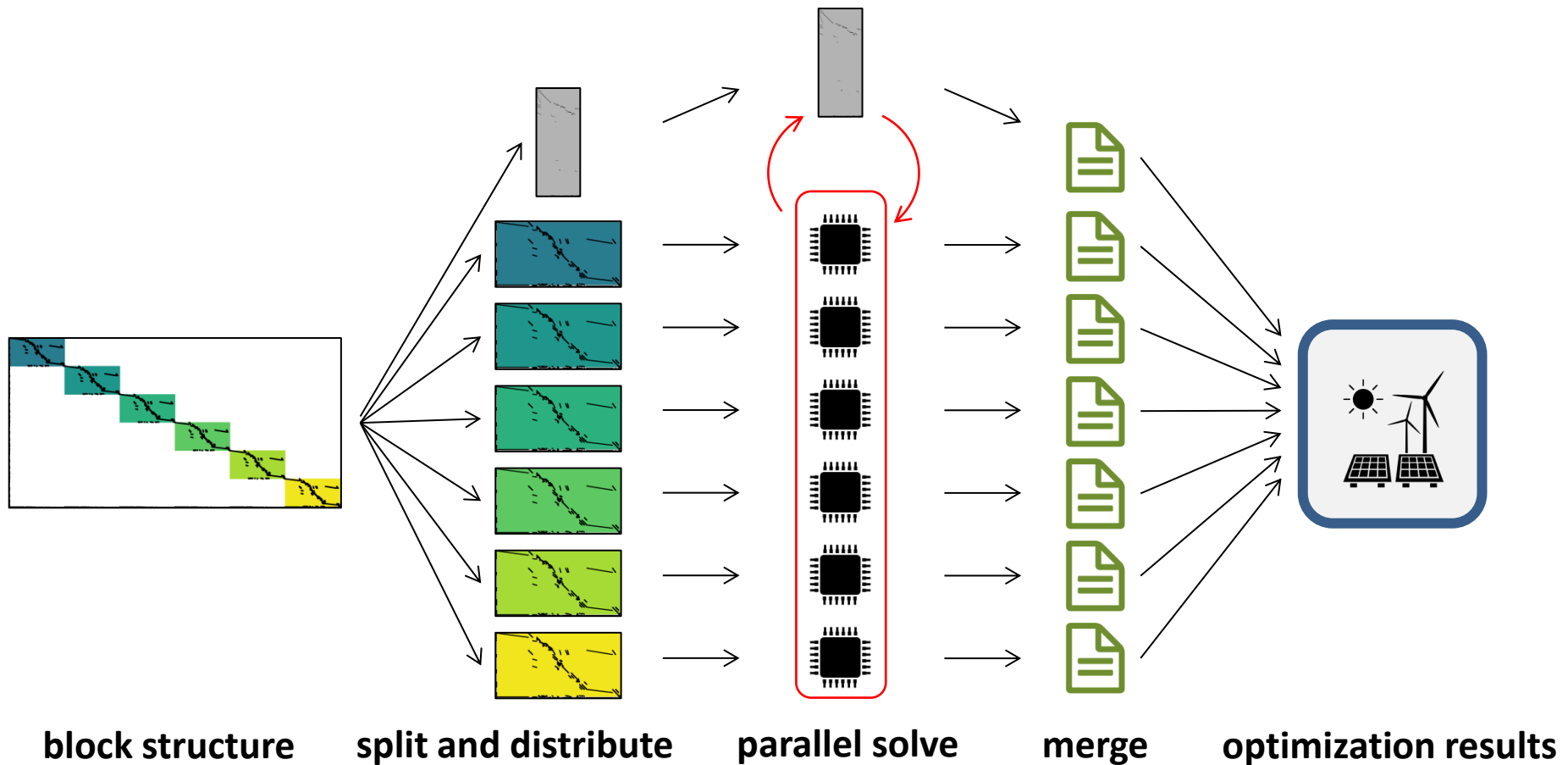
Planning horizon + temporal decomp.



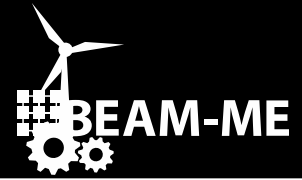
High synergies between annotation variations

**Different annotations result in different speed-ups for the same problem**

# Workflow with PIPS-IPM



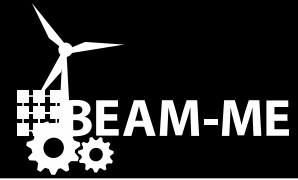
# Running REMix with PIPS-IPM I



ID	Instance	Variation	Regions	PIPS Version	MPI threads	Last iteration	Runtime (sec.)	State
1149052	YSSP	disp	30	PIPS_gps_2018b_8apr	60	55	323	SUCCESSFUL TERMINATION
1149053	YSSP	disp	30	PIPS_gps_2018b_8apr	120	53	251.02	SUCCESSFUL TERMINATION
1149054	YSSP	disp	30	PIPS_gps_2018b_8apr	292	8	92.88	SEGMENTATION FAULT
1149056	YSSP	exp	30	PIPS_gps_2018b_8apr	60	130	1236.58	SUCCESSFUL TERMINATION
1149057	YSSP	exp	30	PIPS_gps_2018b_8apr	120	133	963.19	SUCCESSFUL TERMINATION
1149058	YSSP	exp	30	PIPS_gps_2018b_8apr	292	12	226.18	SEGMENTATION FAULT
1149060	YSSP	disp	120	PIPS_gps_2018b_8apr	60	68	1153.34	SUCCESSFUL TERMINATION
1149061	YSSP	disp	120	PIPS_gps_2018b_8apr	120	67	825.51	SUCCESSFUL TERMINATION
1149062	YSSP	disp	120	PIPS_gps_2018b_8apr	292	71	861.66	SEGMENTATION FAULT
1149064	YSSP	exp	120	PIPS_gps_2018b_8apr	60	19	1131.85	SEGMENTATION FAULT
1149065	YSSP	exp	120	PIPS_gps_2018b_8apr	120	10	28812.43	CANCELLED DUE TO TIME LIMIT
1149066	YSSP	exp	120	PIPS_gps_2018b_8apr	292	-	14.4	MPI ERROR
1149068	YSSP	disp	488	PIPS_gps_2018b_8apr	60	26	1930.75	SEGMENTATION FAULT
1149069	YSSP	disp	488	PIPS_gps_2018b_8apr	120	14	21578.14	CANCELLED DUE TO TIME LIMIT
1149070	YSSP	disp	488	PIPS_gps_2018b_8apr	292	-	45.81	-
1149072	YSSP	exp	488	PIPS_gps_2018b_8apr	60	-	-	-
1149073	YSSP	exp	488	PIPS_gps_2018b_8apr	120	-	559.61	-
1149074	YSSP	exp	488	PIPS_gps_2018b_8apr	292	-	37.44	-

**PIPS-IPM does not run 'out-of-the-box' and is still in development**

# Running REMix with PIPS-IPM II



ID	Instance	Variation	Regions	PIPS Version	MPI threads	Last iteration	Runtime (sec.)	State
1267	YSSP	disp	30	linking-zib-pardiso	16	54	868.27	SUCCESSFUL TERMINATION
1268	YSSP	disp	30	linking-zib-pardiso	24	53	718.54	SUCCESSFUL TERMINATION
1269	YSSP	disp	30	linking-zib-pardiso	32	54	701.98	SUCCESSFUL TERMINATION
1270	YSSP	disp	30	linking-zib-pardiso	48	54	677.32	SUCCESSFUL TERMINATION
1271	YSSP	disp	30	linking-zib-pardiso	64	54	675.63	SUCCESSFUL TERMINATION

## Commercial solver @ DLR ENT-U

512 GB RAM

16 cores

Barrier tolerance  $1e-5$

Runtime: **392 sec.**

## PIPS-IPM @ DLR ENT-U

8 x 128 GB RAM

8 x 24 cores

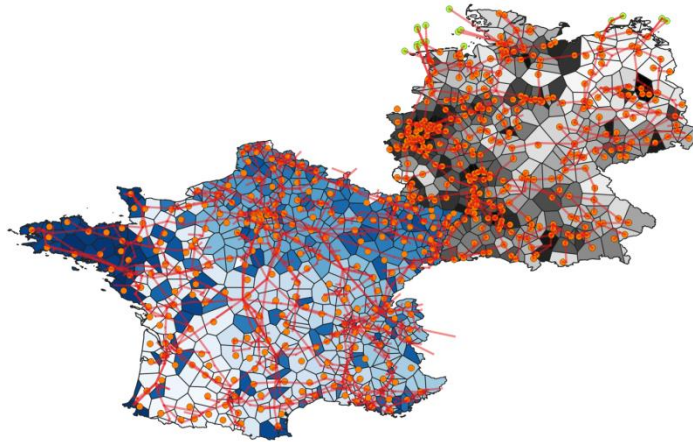
(64 MPI threads on 8 nodes)

Barrier tolerance  $1e-5$

Runtime: **675 sec.**

**No performance gain for small instances despite more hardware utilization**

# Running REMix with PIPS-IPM III



## problem size

488 regions

87.2 mio. variables

73.4 mio. equations

264.9 mio non-zeros

+ optimization of grid and storage capacities

## Commercial solver @ ENT-U

512 GB RAM

16 cores

Barrier tolerance  $1e-5$

Runtime: **155 472 sec.**

## PIPS-IPM @ JSC JUWELS

10 x 96 GB RAM

10 x 48 cores

(120 MPI threads on 10 nodes)

Barrier tolerance  $1e-5$

Runtime: **5 838 sec.**

**PIPS-IPM can outperform commercial solvers in real-world REMix instances**

**PIPS-IPM is a significant first step towards general ESM on HPC**

**Good annotation requires detailed domain knowledge**

**Number of blocks corresponds to the parallelism which can be achieved**

**PIPS-IPM can outperform commercial solvers in large scale REMix instances**



# Project BEAM-ME

## Contact:

[Manuel.Wetzel@dlr.de](mailto:Manuel.Wetzel@dlr.de)

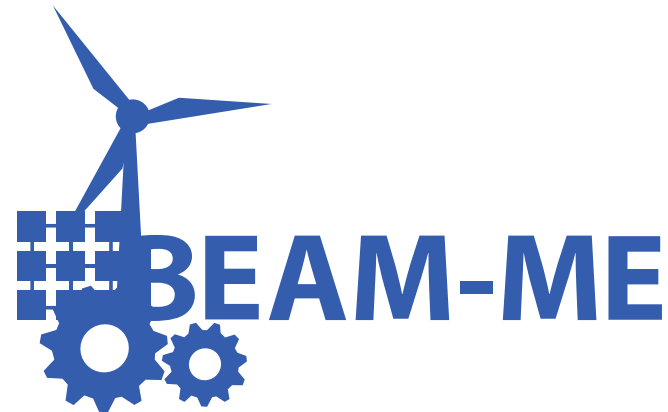
DLR – German Aerospace Center  
Institute of Engineering Thermodynamics  
Energy Systems Analysis  
Pfaffenwaldring 38-40  
70569 Stuttgart  
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