

IN-FLIGHT REMOTE SENSING AND IDENTIFICATION OF GUSTS, TURBULENCE, AND WAKE VORTICES USING A DOPPLER LIDAR

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Abstract

In this paper, in-flight remote sensing technologies are considered for two applications: active load alleviation of gust and turbulence and wake impact alleviation. The paper outlines the strong commonalities in terms of sensors and measurement post-processing algorithms and presents also the few differences and their consequences in terms of post-processing. The way the post-processing is being made is detailed before showing results for both applications based on a complete and coupled simulation (aircraft reaction due to disturbances and control inputs during the simulation is influencing the sensor measurements). The performances in terms of wind reconstruction quality for the gust/turbulence case and in terms of wake impact alleviation performance for the wake vortex case are shown based on simulations and are very promising.

Keywords: Doppler LIDAR; Gust; Turbulence; Wake Vortex; Load Alleviation

1. INTRODUCTION AND MOTIVATION

Aircraft flying into inhomogeneous wind fields experience variations of the aerodynamic forces and moments acting all over the airframe. These variations cause undesired aircraft motions as well as structural loads. In order to alleviate or prevent any threat resulting from the flight into inhomogeneous wind fields, various concrete measures are regularly be taken. For instance, aircraft structures are designed based on the maximum loads that result from standardized design cases and considering an additional safety factor. This corresponds to a robustification of the aircraft design itself. Other measures tackle these issues by modifying the procedures, i.e. where, when, and how the aircraft is used. One example of risk alleviation through the enforcement of procedure is to define a "safe air speed" that shall not be exceeded in the presence of turbulence. Another example is the enforcement of separation minima to alleviate the risk that a given aircraft might enter in the wake vortex of another aircraft.

Both strategies are very effective and have been used for decades. However, these strategies are also having drawbacks, one of which being that they negatively impact the efficiency of the aircraft either by increasing its mass or by leading to longer flight durations. Consequently, quite some research work has been performed in the last decades with the aim of finding new ways to ensure at least the same safety level than with the already existing measures but less deteriorating the overall aircraft efficiency.

There are two main strategies to mitigate these drawbacks: either to have a mean to prevent the flight into these possibly dangerous areas with less conservativeness or to directly alleviate the consequences of flying through these areas. For both applications, being able to directly measure the wind field through which the aircraft will fly would be of great help. With the first mitigation strategy, a severity assessment of each location inside that area could be made, permitting to avoid the (most) dangerous locations, whereas when applying the second mitigation strategy the measurements can be used to directly counteract the effects that will result from flying into these areas. This second strategy is schematically represented in Fig.1. The present paper focuses on this second strategy and specifically on the measurement post-processing and interpretation steps. Several technologies can be considered for the in-flight remote measurement of the wind fields. The Doppler LIDAR technology seems to be the most suited for the applications considered later and the most often used. Thus, only the Doppler LIDAR technology is considered in the following.

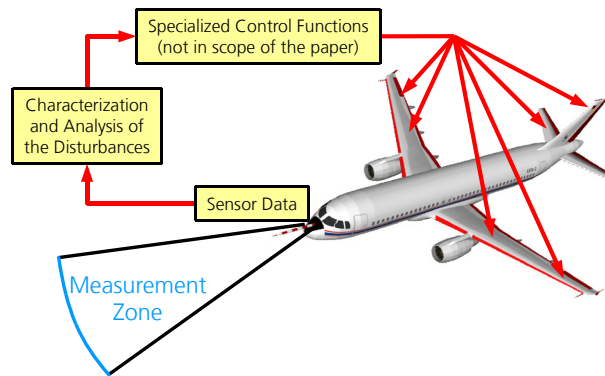


Fig.1 Schematic representation of the disturbance feedforward impact alleviation strategy

This second mitigation strategy (i.e. based on disturbance measurement and alleviation) is the base of two systems called GLAREWISE+TFAC (Gust Load Alleviation using REmote WInd Sensors and Time-Frequency Allocation Constraints) and OWIDIA (Online Wake IDentification and Impact Alleviation). The measurement and post-processing steps (focus of the present paper) are only the first two steps for both systems. Detailed information on the OWIDIA can be found in [1]. Details on the GLAREWISE+TFAC system can be found in [2] and [3]. Both systems are based on the same overall architecture, which is shown in Fig.2. In this figure, the estimation of the disturbance is represented on the upper part of the diagram. The measurements that would be made by the sensor can be simulated by combining a model of the disturbance, a set of values for the parameters of this disturbance model, and a simulation model of the sensor itself. The simulated measurements obtained can then be compared to the real measurements. The difference between simulated and real measurements can be used to estimate how well the parameterized model of the disturbances allows to “reproduce” the real measurements.

The match between simulated and real measurements usually strongly depends on the model parameter values, which leads to search for the model parameter values that provide the best possible match between simulated and real measurements. This search can be initialized based on external knowledge (e.g. traffic information on the other aircraft when dealing with wake vortices) or on the results that were previously found. Alternatively, this search process can be initialized with default (constant) values (e.g. no wind). The start of the search might well be conditioned to some kind of “activation criterion” (e.g. does it look like the measurements contain more than just information on a purely homogeneous wind field?).

Similarly, after having found a set of parameters that optimizes the match between simulated and real measurements, the plausibility of the result obtained shall be verified before using it. This result can be used for instance by a gust and turbulence load alleviation function or by a wake impact alleviation function (see lower-right part of Fig.2). If the disturbance characterization system shall be tested in simulations, the sensor system must be simulated as well. Such a simulated sensor system (see lower-left part of Fig.2) includes a high-quality sensor model and possibly also a model of the relevant parts of the data acquisition/management system (e.g. a buffer). Note that the sensor models used for validation in simulation (see lower-left part of Fig.2) and by the estimation algorithm (upper-right part of Fig.2) are usually different: the former one has much higher requirements in terms of quality than the latter one and the latter one shall be fast enough for the numerous evaluations required during the estimation process.

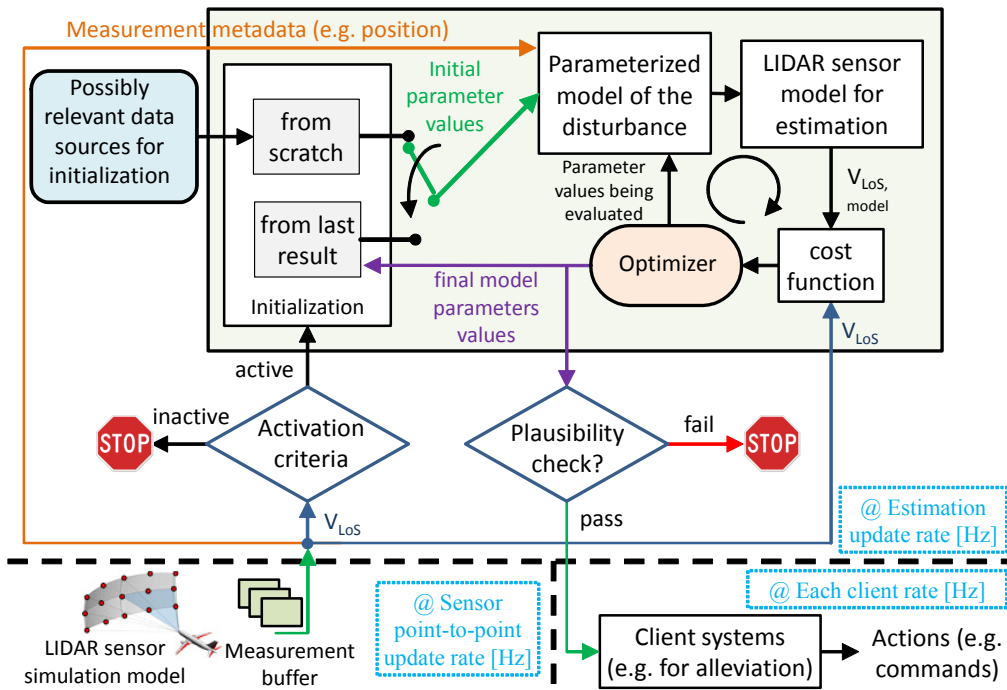


Fig.2: Overall architecture of the presented disturbance characterization systems

A general overview of the disturbance characterization methodology was shown in Fig.2 whose components will be detailed in the following sections of the paper. Section 2 presents the Doppler LIDAR sensor measurement principle and the way a simulation model for these sensors can be built and integrated into a nonlinear flight dynamics simulation program. Section 3 presents the general idea behind the sensor measurement post-processing algorithms as well as the numerical algorithms (formulation and resolution) used. Section 4 shows two examples: one for the application to gust and turbulence recognition, and the other for the characterization of wake vortices. The latter example includes the alleviation of the detected wake vortices.

2. DOPPLER LIDAR: MEASUREMENT PRINCIPLE AND SIMULATION MODELS

Doppler LIDAR sensors permit to retrieve relative velocity information based on the Doppler Effect. A laser source is used to illuminate the “objects of interest” which reflect or scatter the laser light back to a detector. The detector is able to detect the slight frequency shift that results from observing an object with nonzero relative speed with respect to the sensor. If the object relative motion is oriented toward the sensor, then the frequency of the backscattered light will be increased (so-called blue shift). On the contrary, if the object is moving away from the sensor, the backscattered light frequency will be lower than the original light frequency (red shift). Using a well-defined wavelength or frequency – as with a laser source – enables the comparison between the original and backscattered light spectrums, which, in turn, permits to determine the object/sensor relative velocity component that in the direction of the laser beam. This direction is commonly called line-of-sight direction (LoS).

There are numerous types of detector technologies, whose descriptions go well beyond the scope of the present paper. However, two main distinctions based on some technological differences between the different Doppler LIDAR sensors shall be made. The first distinction can be made on the wavelength used. Some Doppler LIDAR sensors are working in the infrared wavelength domain and are based on the light that is backscattered by small particles in the air (Mie scattering / coherent detection). Other Doppler LIDAR sensors are working in the ultraviolet wavelength domain and are based on the light that is backscattered by the molecule of the air itself (Rayleigh scattering / incoherent detection). This distinction must be made due to the fact that the performance of both technologies can significantly differ and do not depend on the same parameters [4]. The second distinction to be made is between “pulsed” and “continuous wave” LIDARs. In a pulsed LIDAR, the light is emitted during a very short time and as a pulse (duration typical in the order of a few tens of nanoseconds) and the distance at which the measurement is made is determined by the time waited between the pulse emission and the detection (forth and back travel time for the light). With a continuous wave LIDAR the distance information is lost (sometimes not necessary) unless some focusing optics is used to select the “distance of interest” [[5]-[6]]. Further information on remote wind sensing techniques can be found in the short overview proposed by ONERA in [4] as introduction for an issue containing other LIDAR articles, the very comprehensive DLR report [7] and the PhD thesis [8], which constitutes a very detailed reference regarding the LIDAR technology.

This extremely short and simplified explanation for the distinction between the various sensor types can however be ignored for the focus and the relatively generic considerations of this paper (basic properties such as spatial resolution

and level of noise are considered without considering explicitly how this performance will be achieved and the consequences for each subcomponent of the sensor system). These properties impact the quality of the measurements or the exactly measurement geometry, which must be taken into account while designing the algorithm and selecting one particular sensor but the main ideas behind the post-processing algorithms and the measurement interpretation are the same.

Sensor simulation models for use in a flight dynamics simulation program are typically based on two main elements: the simulation of the “perfect” measurement and the “error models”. “Perfect” measurement shall not be interpreted here as the measurement that the user would like to have but as the measurement that would be obtained if the sensor hardware did not deteriorate the measurement. For the case of the Doppler LIDAR sensors the perfect measurement is usually determined by the sensor geometry, i.e. where the measurements are made, and the relative wind (aircraft velocity with respect to the air particles at these locations). The location of the measurement is not a point in space but rather a three-dimensional domain. Consequently the measurement corresponds to a weighted-average of the relative wind over this three-dimensional domain, which can be generically represented by considering that the measurement can be expressed as a function of the wind field itself and of a weighting function:

$$(1) \quad \text{Measurement} = f(\text{WindField}, \text{WeightingFunc}: 3Dpos \mapsto \text{weight})$$

The weighting function results from the differences in terms of backscattering energy coming from the different locations inside this domain. Therefore this weighting function and its impact on the measured values strongly depend on the exact sensor configuration. A simplified representation that can be used when no better information is available or to perform relatively generic investigations is to consider the wind field along a segment of the laser beam direction and to take the average wind along this segment. As mentioned before the Doppler Effect applies to the rate of change (over time) of the distance between the observed object and the observer location. This means that only the velocity component in the line-of-sight direction (assuming laser source and detector are the same place) is measured. There are some unusual sensor setups that should permit to retrieve other velocity components than the LoS one, which can also be modeled and treated with the same kind of post-processing algorithms, but that will not be considered hereafter for conciseness reasons [[5]-[6]].

For any point P the line-of-sight (LoS) component of the wind vector $\vec{W}(P)$ can simply be computed as the dot product $\vec{W}(P) \cdot \vec{u}_{LoS}$ between the local wind at P and a unit vector in LoS direction. In order to simply model the fact that the measurement domain is not a point is to consider a segment S_1S_2 of the line-of-sight direction and to compute the average the LoS-wind \bar{v}_{LoS} as follows:

$$(2) \quad \bar{v}_{LoS} = \frac{\int_{S_1}^{S_2} \vec{W}(s) \cdot \vec{u}_{LoS} ds}{|S_1S_2|},$$

where \vec{u}_{LoS} in a unit vector is line-of-sight direction. This integral can be approximated by taking enough discrete points along the segment S_1S_2 .

When flying at a given airspeed, the measurement rate (i.e. the number of measurements per time interval) partly determines the average distance between the individual measurements that are performed. The other factors are the measurement geometry (spread left/right and above/below the flight path direction) and the measurement distance. These factors and the dimensions of the three-dimensional domains where each measurement is being performed together define the spatial resolution of the sensor. In the present work, a poor-spatial resolution is considered as an intrinsic property of the sensor configuration and not as an imperfection.

Imperfect measurements and errors occur for instance when the direction of the laser beam does not match the direction that was assumed or configured for this measurement. Similarly, the energy distribution over the three-dimensional domain might not be perfectly known. An uncertainty regarding some time-delays in the processing chain can also be considered as a measurement location uncertainty. To summarize, all the aforementioned sources of error can be defined as “pointing” or “geometrical” uncertainties. More classical measurement errors such as imperfect measurement or determination of the frequency shift caused by the Doppler Effect can also affect the remote wind measurements. They can result from plenty of different causes, ranging from some small misalignments in the detector optical system to basic noise on the detector photosensitive components. Doppler LIDAR sensors are complex and as for any type of modelling activity, it is crucial to select the right model complexity for the targeted application. Fortunately, it appears that for the present task pretty simple generic measurement error models can be used to test and validate the developed post-processing techniques.

3. MEASUREMENT POST-PROCESSING AND INTERPRETATION

This section focuses on the post-processing of the measurements. First the models used for the post-processing are explained in section 3.1. Then, the required equations (based on the Bayesian estimation theory and more specifically the maximum likelihood estimation method) are derived in section 3.2: further information on Bayesian estimation can be found in [[9]-[10]]. Finally additional information relevant for developing a practical application based on the same

post-processing techniques is provided in sections 3.3 and 3.4. The results obtained by utilizing this post-processing on the two considered applications (active load alleviation and wake impact alleviation) are shown later in section 4.

3.1. Model used for the post-processing

The post-processing algorithms that are considered in the presented work are all considering parameterized models where the parameters are directly connected to the physics of the phenomena that shall be detected by means of the sensor measurements (e.g. gust, wake-vortex, etc.). Other modelling strategies (e.g. black-box models, neural networks,...) could theoretically be used, but in practice the connection with the physics is very useful to be able to check the plausibility of the results obtained, to build more robust algorithm, and to be able to physically interpret the detected situation. Besides, choosing a model structure is also a way for the engineer to provide the existing domain-specific knowledge on the physical phenomenon at stakes to the post-processing algorithms.

There are two main types of physics-based parameterized model structures that are usually used. The first and most common type of physics-based parameterized model structure is encountered when sufficient knowledge on the physical phenomena has been acquired and that a certain level of abstraction or comprehension for the phenomenon has been reached. In that case, this knowledge can be used to generate simple parameterized models of these phenomena. These models usually correspond to a very good trade-off between representativity (precision) and complexity (number of parameters, complexity of the relationships). This is typically the case that is encountered when trying to detect and characterize wake vortices based on velocity measurements.

Various low-order / analytical models of wake vortex velocity distributions have been proposed, e.g. by Burnham and Hallock [11], by Lamb and Oseen [12] (derived from a well-known solution to the Navier-Stokes equations), by Proctor [13], by Winkelmanns [14] or by Fabre and Jacquin [15]. These models describe the wind vector that is induced by a vortex at a point in space by specifying that this vector is perpendicular to both the vortex core line and the shortest line joining the vortex core line to the point that is considered. The differences between these models lie in the function $V: r \mapsto V(r)$ that relates the distance r between the point considered and the vortex line to the velocity vector magnitude $V(r)$. The mathematical expressions for the tangential velocity distribution functions defined by the aforementioned models are provided in Tab.1.

These models describe the velocity distribution depending on the distance between the vortex line and the considered position. The vector direction is contained in the plane that is perpendicular to the vortex line. This vector is also perpendicular to the line joining the vortex core and the considered position. The flow field induced by a single vortex and based on the Burnham-Hallock tangential velocity distribution model is schematically represented in Fig.3. In this figure, for readability reasons only the wind vectors at some specific positions are shown. It can be seen that the magnitude of the velocity only depends on the distance to the core and that the maximum velocities are reached at/around the core radius.

Name	Function $V: r \mapsto V(r) = \dots$
Lamb-Oseen	(3) $\frac{\Gamma}{2\pi r} \left(1 - e^{-\beta \left(\frac{r}{r_c}\right)^2} \right)$
Burnham-Hallock	(4) $\frac{\Gamma}{2\pi} \frac{r}{r_c^2 + r^2}$
Proctor	For $r > r_c$, (5) $\frac{\Gamma}{2\pi r} \left(1 - e^{-10 \left(\frac{r}{b}\right)^{3/4}} \right)$ Otherwise, (6) $\frac{1.4 \Gamma}{2\pi r} \left(1 - e^{-10 \left(\frac{r}{b}\right)^{3/4}} \right) \left(1 - e^{-1.2527 \left(\frac{r}{r_c}\right)^2} \right)$
Winkelmanns	(7) $\frac{\Gamma}{2\pi r} (1 - e^A)$, (8) with $A = -\frac{\beta_i \left(\frac{r}{b}\right)^2}{\left(1 + \left(\frac{\beta_i \left(\frac{r}{b}\right)^{5/4}}{\beta_o}\right)^p\right)^{1/p}}$ (9) $\beta_o = 10, \beta_i = 500, \text{ and } p = 3$
Fabre-Jacquin	(10) $\frac{\Gamma r}{2\pi r_1^2} \left(\frac{r_1}{r_2}\right)^{1-\alpha} \frac{1}{\left(1 + \left(\frac{r}{r_1}\right)^4\right)^{\frac{1+\alpha}{4}} \left(1 + \left(\frac{r}{r_2}\right)^4\right)^{\frac{1-\alpha}{4}}}$

	Typical values: $\frac{r_1}{r_2} = 0.1$ and $0.4 < \alpha < 0.6$
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Tab.1 Common wake-vortex tangential velocity models (further explanation on these models found in references [[11]-[16]])

The wake of an airplane is composed of two such vortices: one generated at the extremity of the left wing and another one rotating in the opposite direction generated at the extremity of the right wing. The typical flow field of a vortex pair is illustrated in Fig.4.

The various models mentioned previously exhibit some differences in and around the vortex core, but a very similar overall wind field otherwise (see for instance [16]). The large-scale representativeness of these models has been shown over the last decades in many studies (see for instance [[17]-[18]]).

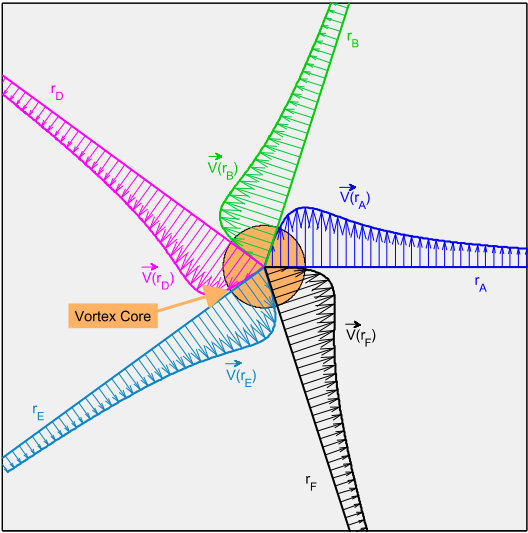


Fig.3: Schematic representation of the flow induced by one vortex alone (model used: Burnham-Hallock)



Fig.4: Schematic representation of the flow field induced by an airplane, rotation direction indicated by the arrows (secondary vortices e.g. due to the horizontal tailplane are neglected in this simplified representation)

For other types of phenomena, the level of knowledge or comprehension of these phenomena might not be sufficient to derive simple analytical models. Even when the fundamental physical effects are understood, the nature of the phenomena might also be stochastic, leading to the impossibility to derive such deterministic models. In these cases, a rather commonly used solution is to use a so-called “free-form solution” (second type of physics-based parameterized models): the physical phenomenon is represented by a series of parameters (possibly a very long series) in a given suitable parameter space. For instance, the shape of an object can be represented by a large number of facets: larger numbers of facets implies more freedom and a more precise representation of the object. Another example is the representation of an audio signal by a subset of its frequency components, which is the base of most audio lossy compression algorithms. This latter example is also interesting in the sense that the best audio compression algorithms make use of specific knowledge from the psychoacoustics science to optimize the choice of the combinations of frequency components. This exemplifies that engineers’ knowledge can not only be injected in the model structure itself, but also be integrated during the selection of the model parameter values. Finally, a field (regardless whether

vector or scalar field) can typically be represented by discretizing the space with some kind of mesh and by representing the local field quantities within the mesh cell or at the mesh node locations. With this approach a three-dimensional wind field is represented by a wind vector (three components) for each node of the mesh. Wind vector values for points that are not directly a mesh node are then retrieved by means of a more or less complicated interpolation procedure. Typically, the parameters that will be searched are the wind vector components at each node, but improvement of the node locations might also be considered in some cases.

This approach has been used to generate a free-form parametric representation of a generic wind field for the modelling of turbulence and gusts. To the best of the authors' knowledge there is no generally applicable model of gusts and turbulence fields. Simplified gust shapes (e.g. the so-called 1-cosine gusts) have been defined to help the comparison between results and to express some certification criteria for structural loads. However, the shapes of the gusts that are encountered in the real world shall not be assumed to match one of these simplified shapes.

For the application to active load alleviation, the fact that the most important short-term wind variations in terms of structural loads are connected to the vertical wind variations, the model can be simplified by considering that only the vertical wind components can change from one node to the other. The other components (in flight-path and in the lateral directions) are also present in the turbulence wind field but are far less important from a load point of view. The simplification made here is not really required for the identification process to work: even when confronted to a truly three-dimensional wind field the identification with and without the other components will provide approximately the same vertical wind profile.

Similarly, by neglecting the variations between the wind at the left side and at the right side of the aircraft's symmetrical plane the mesh can be drastically reduced and thereby the number of parameters (vertical wind components) that needs to be determined. The same simplification can be made for the local wind variations between two points located on one vertical line. The mesh also can and should be restricted to the area (in space) of interest. Once again, all these ways of reducing the free-form model formulation should be understood as means to integrate engineering judgement into the model structure. The strongly simplified mesh that has been used for the results on gust and turbulence remote sensing and on characterization presented later in this paper have been obtained with this simplified mesh. This mesh is schematically represented in Fig.5.

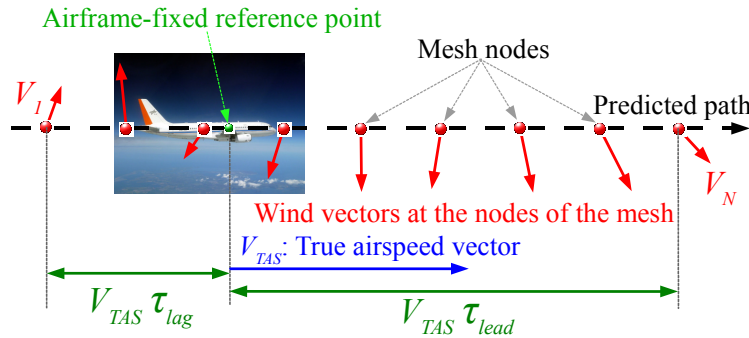


Fig.5: Illustration of the simplified free-form wind field model based on a one-dimensional mesh

The free-form model structure used in this case is consequently reduced to a set of points defined along the predicted aircraft path: the vertical wind components at these points $(P_i)_{i \in \llbracket 1, N \rrbracket}$ define the simplified wind profile. The exact mathematical formulas that define the two extreme mesh points as well as all points in between are:

(11)

$$P_1 = P_{ref} - V_{TAS} \tau_{lag}$$

(12)

$$P_N = P_{ref} + V_{TAS} \tau_{lead}$$

(13)

$$\forall i \in \llbracket 2, N - 1 \rrbracket, P_i = P_1 + \frac{i-1}{N-1} \overrightarrow{P_1 P_N} .$$

Typical values for the parameters shown in Fig.5 and in Equations (11-13) are: $1 s < \tau_{lead} < 2 s$, $\tau_{lag} = 0.5 s$, and $N \approx 30$. This corresponds to a trade-off between the sensor range characteristics, the number of optimization variable (see following sections), and the need to include several nodes behind aircraft's current position (see section 4.1).

The free-form model presented here and used hereafter corresponds to the block called "Parameterized model of the disturbance" in the general architecture shown in Fig.2 and for the application to the gust and turbulence identification. For the wake-vortex identification the analytical wake-vortex models presented at the beginning of this section are used instead.

3.2. Post-processing via maximum likelihood

The goal of the post-processing is typically to interpret the measurements made such that the entire wind field is reconstructed. In practice only restricted information has been gathered through the measurements. Indeed, in both applications the most important wind directions are the vertical wind components. In the case of gust and turbulence they are one of the main causes for structural excitation and loads. In the case of the wake vortex encounter, the difference of vertical wind along the wing span is the main cause for the additional rolling moment and vertical load factor. These vertical wind components cannot directly be measured, which means that the wind field at locations and directions that were not directly measured needs to be reconstructed. This reconstruction is necessarily is partly a guess that is made based on the surrounding measurements, the engineers' knowledge, and some mathematical tools.

The measurements are usually noted with the letter z and indices are used to distinguish them. Let n be the number of measurements currently contained in the database (or buffer). Then, let

$$(14) \quad (z_i)_{i \in \llbracket 1, n \rrbracket}$$

be the n -tuple of measurements. Let $\Theta = [\theta_1, \theta_2, \dots, \theta_p]$ be the vector of all p wind field model parameters. For a given vector $\tilde{\Theta}$ the n model outputs $(y_i(\tilde{\Theta}))_{i \in \llbracket 1, n \rrbracket}$ corresponding to the measurements made (same location and conditions) can be computed and compared to the measurements $(z_i)_{i \in \llbracket 1, n \rrbracket}$. The closer the measurements and the corresponding model outputs, the more likely it is that the model used and the parameter values used are right. More formally for each measurement and each model parameter vector value, a probability density function (pdf) $x \mapsto p(x|\Theta)$ can be defined by the engineer to represent its belief regarding the measurement under the assumption that these model parameters are right.

For the sake of the explanation, consider a simple system being a solid with a given mass m whose mass will be measured using a scale and the relationship between mass and weight: $P = mg$. If the gravity field is perfectly known the measured mass is only affected by the sensor uncertainty/error of the scale. The error usually has several sources (calibration errors, nonlinearities, quantization, etc.) and can usually be characterized. If the model expressed by the equation $P = mg$ is uncertain (e.g. the equation is approximated or the gravity field itself is uncertain), these model errors and the pure sensor errors combine to form the "measurement error". By describing the stochastic properties of each error source, a model of this measurement error can be derived or estimated. This model describes how likely it is to obtain a given measurement value (here the mass that is deduced from the weight measurement and the model equation) provided a given set of system parameters (here the true mass), which can naturally be written as the pdf:

$$(15) \quad \text{measurement} \mapsto p(\text{measurement} \mid \text{system or model parameters})$$

Taking the notations introduced earlier, the pdf that interests us is the following one:

$$(16) \quad (z_i)_{i \in \llbracket 1, n \rrbracket} \mapsto p((z_i)_{i \in \llbracket 1, n \rrbracket} \mid \Theta).$$

In many cases, it can be assumed that the error on each measurement does not depend on the other measurements or that:

$$(17) \quad \forall i \in \llbracket 1, n \rrbracket, p(z_i \mid \Theta) = p(z_i \mid \Theta, (z_j)_{j \in \llbracket 1, n \rrbracket - \{i\}}),$$

and in that particular case:

$$(18) \quad p((z_i)_{i \in \llbracket 1, n \rrbracket} \mid \Theta) = \prod_{i=1}^n p(z_i \mid \Theta).$$

Note that this assumption is often satisfied with noise and quantization effects, but usually not when some sensor calibration biases or model uncertainties are present. Coupled sensor errors (e.g. due to calibration or measurement range uncertainties) are not considered in the Gaussian error model used hereafter. It is assumed that proper calibration of the sensor system is made prior to using them or continuously during flight. Precise characterization of the measurement range error or of biases in the standard air data measurements might be less straightforward but at least the synchronization between these two measurement channels can be continuously monitored and corrected.

When the aforementioned assumption is made and when additionally assuming that the pdf of each measurement z_i is (or is assumed to be) Gaussian with mean $\xi_i(\Theta)$ and standard deviation σ_i , i.e. reads

$$(19) \quad \forall i \in \llbracket 1, n \rrbracket, p(z_i \mid \Theta): z_i \mapsto \frac{1}{\sqrt{2\pi} \sigma_i} e^{-\frac{1}{2} \frac{(z_i - \xi_i(\Theta))^2}{\sigma_i^2}},$$

then the pdf $p((z_i)_{i \in \llbracket 1, n \rrbracket} \mid \Theta)$ reads:

$$(20) \quad \begin{aligned} p((z_i)_{i \in \llbracket 1, n \rrbracket} \mid \Theta) &= \prod_{i=1}^n p(z_i \mid \Theta) \\ &= \frac{1}{(\sqrt{2\pi})^n \prod_{i=1}^n \sigma_i} e^{-\frac{1}{2} \sum_{i=1}^n \frac{(z_i - \xi_i(\Theta))^2}{\sigma_i^2}}. \end{aligned}$$

Note that the assumption made on the proper calibration of the sensor implies that the mean $\xi_i(\Theta)$ is equal to the expected measurements $y_i(\Theta)$ for the currently considered vector Θ of parameter values. Note also that in these last expressions

the Gaussian pdf involves the parameters of the Θ vector only in the expected measurement / mean. The uncertainty itself is assumed to result only from the sensor characteristics and not on the strength or orientation of the vortex (which are parameterized in Θ). This is a reasonable assumption for the considered sensor technology, but could be invalidated for instance if the sensor uncertainty depends on the measured value (e.g. limited measurement range). Regardless of the exact pdf $p((z_i)_{i \in [1,n]} | \Theta)$ that is derived for the problem considered, the maximum likelihood estimation method defines the “most likely parameter vector” $\hat{\Theta}$ as the parameter combination that maximizes the likelihood to have obtained the measurement set $(z_i)_{i \in [1,n]}$ that was indeed obtained. This can mathematically be formalized as:

$$(21) \quad \hat{\Theta} = \operatorname{argmax}_{\Theta} \left(\Theta \mapsto p((z_i)_{i \in [1,n]} | \Theta) \right).$$

Note that the notation p and the abbreviation pdf (probability density function) might lead to think of the functions and values mentioned before are “probabilities”. In a strictly mathematical sense, they are however not the probabilities or pdf themselves but beliefs on what these probabilities or pdf would be. The detailed explanation on this as well as the exact differences can be found in the literature on Bayesian estimation (see for instance [[9]-[10]]) and will therefore not be reminded hereafter.

Quite often, instead of maximizing directly the likelihood function $\Theta \mapsto p((z_i)_{i \in [1,n]} | \Theta)$, this function is modified in a way that does not modify the location of its maximum. For instance, by taking the logarithm of a function f with positive values (i.e. $\forall x, f(x) > 0$) it can be shown that $\operatorname{argmax}_x \ln(f(x)) = \operatorname{argmax}_x f(x)$. Regardless of the function f considered, the function obtained by composing f with a strictly increasing function (which is the case for \ln) always satisfies this property. This kind of transformations is often made to simplify the computation of the cost function (and possibly its derivatives) or to improve the conditioning of the optimization problem. For instance, by composing the function of Equation (19) with the Neperian logarithm it can be shown that maximizing the resulting function:

$$(22) \quad \begin{aligned} \ln(p((z_i)_{i \in [1,n]} | \Theta)) &= \sum_{i=1}^n \ln(p(z_i | \Theta)) \\ &= \sum_{i=1}^n \ln \left(\frac{1}{\sqrt{2\pi} \sigma_i} e^{-\frac{1}{2} \frac{(z_i - \xi_i(\Theta))^2}{\sigma_i^2}} \right) \\ &= -\sum_{i=1}^n (\sqrt{2\pi} \sigma_i) + \left(-\frac{1}{2} \sum_{i=1}^n \frac{(z_i - \xi_i(\Theta))^2}{\sigma_i^2} \right) \end{aligned}$$

The first term is constant since the standard deviations $(\sigma_i)_{i \in [1,n]}$ do not depend on Θ , which finally leads to consider the equivalent least-squares problem:

$$(23) \quad \begin{aligned} \hat{\Theta} &= \operatorname{argmax}_{\Theta} \left(\Theta \mapsto p((z_i)_{i \in [1,n]} | \Theta) \right) \\ &= \operatorname{argmax}_{\Theta} \left(\Theta \mapsto \ln(p((z_i)_{i \in [1,n]} | \Theta)) \right) \\ &= \operatorname{argmax}_{\Theta} \left(\Theta \mapsto -\sum_{i=1}^n \frac{(z_i - \xi_i(\Theta))^2}{\sigma_i^2} \right) \\ &= \operatorname{argmin}_{\Theta} \left(\Theta \mapsto \sum_{i=1}^n \frac{(z_i - \xi_i(\Theta))^2}{\sigma_i^2} \right) \end{aligned}$$

This property can be exploited by using specialized optimization algorithms (e.g. Gauss-Newton) which can usually converge significantly faster than the non-specialized algorithms (see [19] and references therein). On well-conditioned maximum likelihood problems (and which do not exhibit local minima) most optimization algorithms should normally find the right parameters, the main difference between the algorithms will in that case only be the computation time needed to converge.

3.3. Measurement data and metadata handling

In the previous section, the measurement set considered for the maximum likelihood estimation was simply noted $(z_i)_{i \in [1,n]}$. In practice, there are usually the raw measurement data (i.e. what was written here as z_i) but also the corresponding metadata. In the example of the Doppler LIDAR sensor measurements, the measurements are the measured line-of-sight velocities and the corresponding metadata consist of: the measurement location (not just a point, cf. section 2), the line-of-sight direction at measurement time, the sensor’s own velocity (inertial speed with respect to the Earth) at measurement time, and possibly others depending on the level of detail of the model (e.g. laser pulse power, backscattering coefficients, etc.). The metadata are crucial to be able to define the likelihood functions corresponding to the data.

Sensors might be able to produce several measurements simultaneously or only sequentially, which brings two main post-processing options: a series of “one-shot” estimations based on a subset of relevant measurements or a recursive estimation process computing each time a new estimate based on the previous one and the new measurement(s). Good recursive estimation processes (e.g. Kalman filter and variants) are often less computationally expensive (computation time, memory requirements) but defining a good trade-off between robustness and complexity can be very difficult in the presence of strongly nonlinear relationships between parameters and measurements, as in the present case. The

quality of the estimate is also difficult to define in these cases and the estimated error-bounds (e.g. the well-known Cramer-Rao bound [[20][21][22]]) shall not be overinterpreted and always considered with very great caution.

The “one-shot” estimation forces to maintain some kind of “measurement database” containing both the data and the associated metadata and to manipulate and compute more complex mathematical expressions during the estimation process. However, relatively easy metrics can be used for the obtained goodness of fit between the model with the current parameters and all the measurements stored in the database. Here engineers can integrate their domain-specific knowledge and define what they consider to be a match that provides great confidence in the result and what not. Analyzing the plausibility of the result and the level of confidence with which this result can be used in further steps is crucial to ensure that under no condition the overall system will perform undesired or hazardous actions.

In all systems and applications considered here, the model is strongly nonlinear and the system shall be considered as safety-critical. Consequently, the “one-shot” estimation process has been preferred to the recursive estimation techniques.

3.4. Numerical formulation and resolution

In the various applications considered hereafter, the assumptions mentioned in section 3.2 and leading to the formulation of the equivalent least-squares problem of Equation (23) were made. The model used for the gust and turbulence characterization application was the free-form model structure presented in Fig.5 for which the wind velocities at each node must be reconstructed from the measurement.

The model used for the characterization of wake-vortices was a pair of parallel vortices with the Burnham-Hallock tangential velocity distribution models. The scenarios considered are only based on wake vortices that are “young enough” to not be strongly deformed as this typically happens in later stages of the wake vortex decay [[23][25]]. Simplified models of older wake vortices have been developed and used in various studies [[26]-[29]]. Such models could be used in future versions of the OWIDIA system.

With the model used here, the parameters to be determined are the wake vortex circulation Γ , the distance between the vortex lines b , as well as the three-dimensional orientation of these wake vortex lines relative to the aircraft. As shown in the paper [1], but not reminded hereafter several formulations for this orientation have been used in the authors’ previous studies, but besides slight differences in terms of computational cost these formulations are in the end equivalent and straightforward variable changes permits to convert one into the other.

The corresponding maximum likelihood problems were numerically solved with gradient-based local optimization algorithms. The “online” resolutions (i.e. coupled with a full flexible or rigid aircraft simulation program comprising also a flight control system) have usually been performed with a modified Broyden-Fletcher-Goldfarb-Shanno (BFGS) quasi-Newton algorithm. The modification with respect to the standard version consists in using an iterative resolution (with a restricted number of iterations) of the linear problem leading to the new step direction and initial length (before applying a line search). Even though no formal demonstration was attempted, this modification seems to avoid computing very inappropriate descent steps when the Hessian matrix is not well shaped/conditioned (yet), while not impairing the overall convergence property of the algorithm.

As already mentioned, other algorithms could be used for the resolution: the work performed until now focused rather on the physical modelling and the extensive testing in a highly representative simulation environment than on the search for shorter computation time. Nevertheless, the model outputs (in the present case wind velocities at given locations for various sets of parameters) need to be evaluated very often during the process.

Consequently, the time spent evaluating the model outputs is the driving parameter for the overall computational cost and consequently efficient implementations of the model shall be used. For a free-form model as used for the characterization of gust and turbulence fields, it is crucial to use data structures permitting efficient determination of the nodes and weightings that are needed to evaluate the wind field at each point. Mesh modification operations (e.g. insertion, deletion, or even deformation) have only a very little impact on the computational cost and therefore can be implemented with greater focus on flexibility and modularity than on pure performance.

The cost of evaluating a simple wake vortex model such as the Burnham-Hallock one is significantly lower than for the Proctor, Winckelmans, and Jacquin models. This constitute a major advantage in an online wake vortex characterization algorithm, whereas the benefits of these models (possibly higher representativeness around the vortex core region) for this type of online algorithm is rather unclear and expected to be low.

For the application to the characterization of gust and turbulence using a free-form model, it was also found useful to add two Tikhonov regularization terms [30] to the least-squares function, which lead to solve the following optimization problem:

$$(24) \quad \hat{\theta} = \operatorname{argmin}_{\theta} \left(\theta \mapsto \sum_{i=1}^n \frac{(z_i - \xi_i(\theta))^2}{\sigma_i^2} + \alpha_1 \|\tilde{F}_1 \theta\|^2 + \alpha_2 \|\tilde{F}_2 \theta\|^2 \right).$$

The Tikhonov matrices $\check{\Gamma}_1$ and $\check{\Gamma}_2$ shall not be confused with the wake vortex circulation Γ of the application to wake vortex characterization. The used Tikhonov regularization matrices are respectively of sizes $(p - 1) \times p$ and $(p - 2) \times p$ with p being the number of parameters in the vector Θ and respectively penalize the first and the second derivatives of the reconstructed wind profile. To this end $\check{\Gamma}_1$ is based on the coefficients $[-1, +1]$ and $\check{\Gamma}_2$ is based on the coefficients $[-1, +2, -1]$ of the well-known Mexican Hat wavelet / convolution filter (also called Laplacian-of-Gaussian filter) [31] of order two.

$$(25) \quad \check{\Gamma}_1 = \begin{bmatrix} -1 & 1 & 0 & \dots & \dots & \dots & 0 \\ 0 & -1 & 1 & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & -1 & 1 & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & -1 & 1 & 0 \\ 0 & \dots & \dots & \dots & 0 & -1 & 1 \end{bmatrix}$$

$$(26) \quad \check{\Gamma}_2 = \begin{bmatrix} -1 & +2 & -1 & 0 & \dots & \dots & \dots & 0 \\ 0 & -1 & +2 & -1 & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & -1 & +2 & -1 & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & -1 & +2 & -1 & 0 \\ 0 & \dots & \dots & \dots & 0 & -1 & +2 & -1 \end{bmatrix}$$

This choice permits to penalize wind fields containing small-scale variations: the small scale variations are expected to not be well measured by the LIDAR sensor and not be the components of the wind field for which it is beneficial to anticipate and to begin counteracting them very early anyway. The coefficients α_1 and α_2 permit to tune the relative strength between the Tikhonov penalization and the least-squares criterion. It was found that even small values of these coefficients (not massively changing the shape of the profile found on typical wind profiles) were already well penalizing nonsmooth profiles and also helping the BFGS algorithm to converge more quickly.

4. RESULTS ON BOTH GUST AND WAKE-VORTEX IDENTIFICATION SCENARIOS

4.1. Results of the application to gust identification

The application presented hereafter was performed within the framework of the European CleanSky Joint Technology Initiative as part of the Smart Fixed Wing Aircraft (SFWA) Integrated Technology Demonstrator. The final goal of the investigated system was the active load alleviation of gusts and turbulence. For this various technologies and control strategies have been investigated. One of the components or subsystems considered was based on a Doppler LIDAR sensor with which the disturbances are recognized slightly before encountering them. This permits to anticipate (near) future loads and to achieve higher alleviation performance than what can be achieved without anticipation. This idea is not new and previous work in this direction has been performed, see for instance [32]-[40]. The Doppler LIDAR post-processing techniques shown in the present paper represent a very significant improvement compared to the corresponding solutions proposed in these previous works. In the following, the wind reconstruction results are presented. The way the load alleviation itself is performed (based on this reconstructed wind) is not presented here but can be found in [2] and [3].

In order to illustrate the way the wind reconstruction is being performed a simple example is used hereafter. In this example, the aircraft is encountering a well-formed analytical 1-cosine vertical gust. This gust is defined with respect to a geodetic reference frame and is fixed in this frame (no mean wind). Since the aircraft is flying almost at constant air speed, this case does not really differ from the way discrete gusts (as defined in the paragraph CS 25.341 of the CS 25 certification specifications [40]) are usually considered either in the time or in the frequency domain. The definition as a “space-fixed” (fixed with respect to the surrounding air mass) gust is useful to perform the Doppler LIDAR measurement simulation, which requires a location-based access to the “real” wind field in order to be able to produce the simulated measurements which will be the starting point for the gust wind reconstruction algorithm. A time-based simulation of the gust as it is often done is not suitable for integrating a LIDAR sensor model in a consistent way with the flight dynamics and aeroelastics simulation model.

In this application the model parameters defined in Fig.5 and Equations (11-13) were chosen as follows: the lead-time τ_{lead} was set to 1.6 seconds, the lag-time τ_{lag} set to 0.5 seconds, and the number of nodes of the 1-dimensional mesh set to 33. The computation time for the wind reconstruction with a 32-bit single-threaded implementation which was not optimized for speed but for flexibility was between 0.25 and 0.35 seconds on a regular Intel i7-2600 at 3.4 GHz. The variability of the execution time is mainly due to the measurement method which was based on the system clock on a non-real-time environment (Windows 7 Enterprise 64-bit). Another source of slight variation of the execution time is that the quite tight convergence criteria can be reached with less than the maximum allowed number of iterations. Note that the worst-case number of operations and thus the maximum execution time in a real-time environment is bounded. The estimation process was started every 0.3 seconds during the simulation, which means that the current implementation is not running fully in real-time at the moment, but is very close to it. Note that the wind reconstruction

process (focus of the present paper) is only updating the wind information used by the control functions and the update rate is relatively low (here the “estimation update rate” as defined in Fig.2 is set to 3.33 Hz). The control functions that use this information to effectively alleviate the structural loads are running significantly faster: this rate is called “client rate” in Fig.2 and a typical order of magnitude is 50 Hz.

As already mentioned the model outputs computation is by far the largest cost during the wind reconstruction process. These computations can be easily fully parallelized such that with the appropriate hardware, there should be no issue to implement a real-time version even if a significantly higher number of nodes would be used or a higher wind reconstruction execution rate be needed.

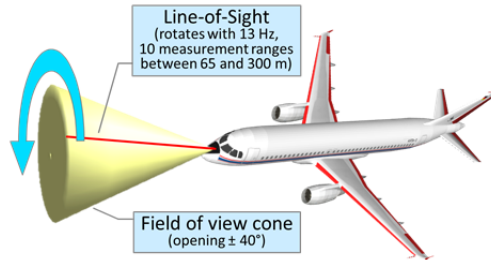


Fig.6: LIDAR sensor scan pattern used for gust and turbulence load alleviation application

The Doppler LIDAR measurement geometry chosen for this application is based on a simple scan mechanism which let the laser beam describe a cone in the aircraft-fixed frame as shown in Fig.6. The line-of-sight rotates continuously and measurements are performed at various ranges between 65 and 300 m.

Fig.7 and 8 present the comparison between the true vertical wind (light red) and the reconstructed wind profiles obtained successively during the encounter simulation (dark blue). Both figures present the exact same results: Fig.7 shows all wind profile results superimposed and permits to see the consistence of the estimation over time, whereas Fig.8 shows the evolution of the wind profile estimates with 300 ms delay between the respective computations. The overall match between true and reconstructed wind is very good and information that is relevant for load alleviation purposes can obviously be extracted from this reconstructed wind profiles.

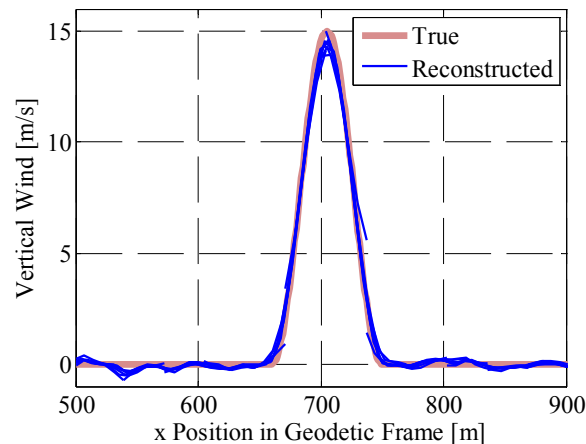


Fig.7: Comparison between the true vertical wind (light coral red) and the reconstructed wind profiles obtained successively during the encounter simulation (blue)

Slight reconstructed vertical wind variations can be observed, especially in the absence of significant vertical wind variations (i.e. before and after the gust). These variations are the consequences of the measurement noise (standard deviation in the order of 1.5 m/s in line-of-sight direction), which is propagated throughout the estimation process and finally slightly impairs the estimation quality. Note that the different wind profiles obtained successively exhibit almost the same deviations with respect to the “true” profile, such that the different blue lines can hardly be distinguished in Fig.7. Each wind profile estimation process was started with the same initial profile, which corresponds to no wind at all. As a consequence, the fact that very similar wind profiles (including the deviations from the true one) have been found cannot result from a reuse of the previously found wind profile. The explanation of the similarity between the results comes from the fact that successive runs of the algorithm use a similar set of measurements. Most of the measurements are the same between both runs. Only a few older measurements were dropped and a few new measurements were added. This results from the fact that the buffer of measurements is larger than the number of new and dropped measurements between two successive calls of the wind reconstruction process.

In Fig.8, it can be noticed that the extremities of the reconstructed profiles often deviates slightly from the true profile and the expectations or hopes that can be formulated for the wind reconstruction module. The Tikhonov regularization that was introduced to ensure the preference for smooth wind profiles and to improve the convergence of the algorithm causes these deviations at the boundaries of the domain. The two first and two last nodes of the mesh are affected and must be either corrected via an additional post-processing step or simply be ignored for further computation steps. This fact is the main motivation for using a mesh that contains nodes located behind the aircraft as it can be observed in Fig.5: thanks to this configuration the current aircraft position is always sufficiently far from the mesh boundaries to prevent the reconstructed wind at the aircraft location to be affected by this effect.

All developments made for the application to the gust and turbulence reconstruction were made with the aim of using the reconstructed wind profile in a feedforward load alleviation function. The Doppler LIDAR sensor spatial resolutions that can be assumed for near future applications are relatively low (at least 5 to 10 m between measurement locations) and the noise levels to be expected are quite high (at least 0.7 m/s in line-of-sight direction), such that the reconstructed wind profile information is significantly more trustworthy for large amplitude variations at low frequencies than for lower amplitude variations or higher frequencies. Consequently the developments presented here focused on designing a particularly robust and effective characterization and load alleviation function for this type of disturbances (large amplitudes, low frequencies). Note that these disturbance characteristics are also the ones for which the anticipation capability of the remote wind sensor are most suited in combination with a feedforward load alleviation concept. With the still relatively limited sensor properties that can be assumed for Doppler LIDAR sensors, it would not really make sense to design a feedforward load alleviation system based only on these sensors. Feedback load alleviation techniques and systems allow increasing the damping of the structural modes and robustly rejecting the remaining disturbances (after the feedforward alleviation). The sensor required by these feedback load alleviation functions is significantly simpler than the Doppler LIDAR sensors. As a consequence, the combination feedback + LIDAR-based feedforward alleviation function has many advantages over the pure feedforward function while being only slightly more complex.

Adding of a feedforward gust and turbulence load alleviation function to a more classical active load alleviation controller permits to greatly reduce the peak structural loads thanks to the anticipation of the near future disturbances. Results obtained in closed-loop with both the feedforward and feedback load alleviation functions will be published in the near future along with the design of the control functions (see [2] and [3]). The wind reconstruction results based on the LIDAR sensors are very promising and the combined results of [2] and [3] show that they are sufficient to enable the design of such an effective anticipation-capable feedforward load alleviation function.

The use of numerous measurements taken at different times to reconstruct a wind field over a domain around the aircraft (or profile when only considering the vertical direction) is a major difference to the approach used in [39]. The work presented in [39] showed a very extensive work combining all aspect from the sensor design to the flight demonstration with active load alleviation. The system as demonstrated in the AWIATOR project and presented in [39] makes use of four different measurement directions to determine the local three-dimensional wind vector (three measurements would be sufficient and the fourth one adds redundancy). Each of the four line-of-sight directions was updated with 60 Hz, leading to a global update rate of 15 Hz for the three-dimensional wind vector. By combining many more measurements than four and by putting the measurements taken at different locations/times and not only taken with different line-of-sight directions, the approach proposed here enables a better recovery of the transversal wind components (perpendicular to the line-of-sight) than by considering the measurements four by four. In [39] a noise amplification factor of 2.9 was found between the noise level of the line-of-sight direction and the noise level of the reconstructed transversal directions. The measurement processing approach proposed here does not lead to a constant amplification factor but the deviations between true and reconstructed profiles in Fig.7 and 8 give an idea of measurement post-processing performance achieved. From a line-of-sight noise level $\sigma_{LOS, GLAREWISE} = 1.5 \text{ m/s}$ the estimated profiles shown in these figures are mostly less than 0.3 – 0.5 m/s apart from the true profile. With other words, instead of amplifying the uncertainty by a factor 2.9, the uncertainty gets reduced by a factor 3 to 4. This difference results from the fact that significantly more (than four) measurements are considered at once and a smoothing of the profile takes place. Please note also, that the smoothing induced in this process does not cause a phase shift as would a low-pass filter placed behind the reconstructed signal based on the method demonstrated in [39] with only four measurements at once.

Though not in the scope of the current paper, the control function that uses the reconstructed wind information ([2] and [3]) are playing a crucial role in determining whether the wind reconstruction results obtained are sufficiently good or not. The designed load alleviation function is not adaptive and is able to prevent the system to generate load cycles in calm air even if the reconstruction algorithm produces a wind profile with some small oscillations around zero, as in Fig.7. This approach differs from those presented in [37] and [38] which present two different adaptive approaches for the load alleviation control. By precisely adapting the load alleviation function to the aeroelastic modes of the aircraft, a greater alleviation performance can be achieved in theory, but the price is difficulty or even incapacity of certifying the corresponding function. The adaptiveness in automatic control has shown very interesting results but open a whole new set of problems and challenges, which were quite well summarized in [41]. In comparison, the feedforward load

alleviation function presented in [2] and [3] focuses on the exploitation of the anticipation capability provided by the LIDAR and the certifiability aspect rather than on “inverting” the flexible modes of the airplane to get the maximum alleviation performance at the price of a lack of robustness and the need for adaptive control.

4.2. Results of the application to wake-vortex identification

The application of the remote wind sensing and of the corresponding post-processing to the characterization of wake vortices presented here is part of a larger system, whose objective is to alleviate the impact of wake vortices. Wake vortex encounters can lead to dangerous aircraft reactions with in particular sudden and strong wake-induced rolling motion. The goal of the complete control system called “OWIDIA” (Online Wake IDentification and Impact Alleviation) is to minimize the wake-induced aircraft motion. The concept of the OWIDIA system is shown in Fig.9 and described in detail in [1]. The LIDAR sensor measures the wind velocities in a short distance (typically 50 to 150 m) in front of the aircraft. An Online Wake Identification (OWI) algorithm is applied to reconstruct the wake vortex disturbance by estimating the most-likely parameters of a Burnham-Hallock wake vortex model considering the measured wind velocities. The principle of OWI was developed in [42]-[44] and extended in [1]. The OWI component is the measurement post-processing algorithm of the OWIDIA system, which is based on the ideas and elements presented earlier in section 3.

On the basis of the wake vortex that was identified by the OWI, the WIAC (Wake Impact Alleviation Control) module, previously published in [44] and [1] and not described in detail hereafter, determines the wake-induced moments affecting the aircraft and generates control commands that countervail these moments. These commands are added to the commands of the basic flight control system, independently from the control mode that is currently active. In all results shown hereafter the basic flight control system of the A320 is always active: in manual flight mode (autopilot disengaged) and in normal law.

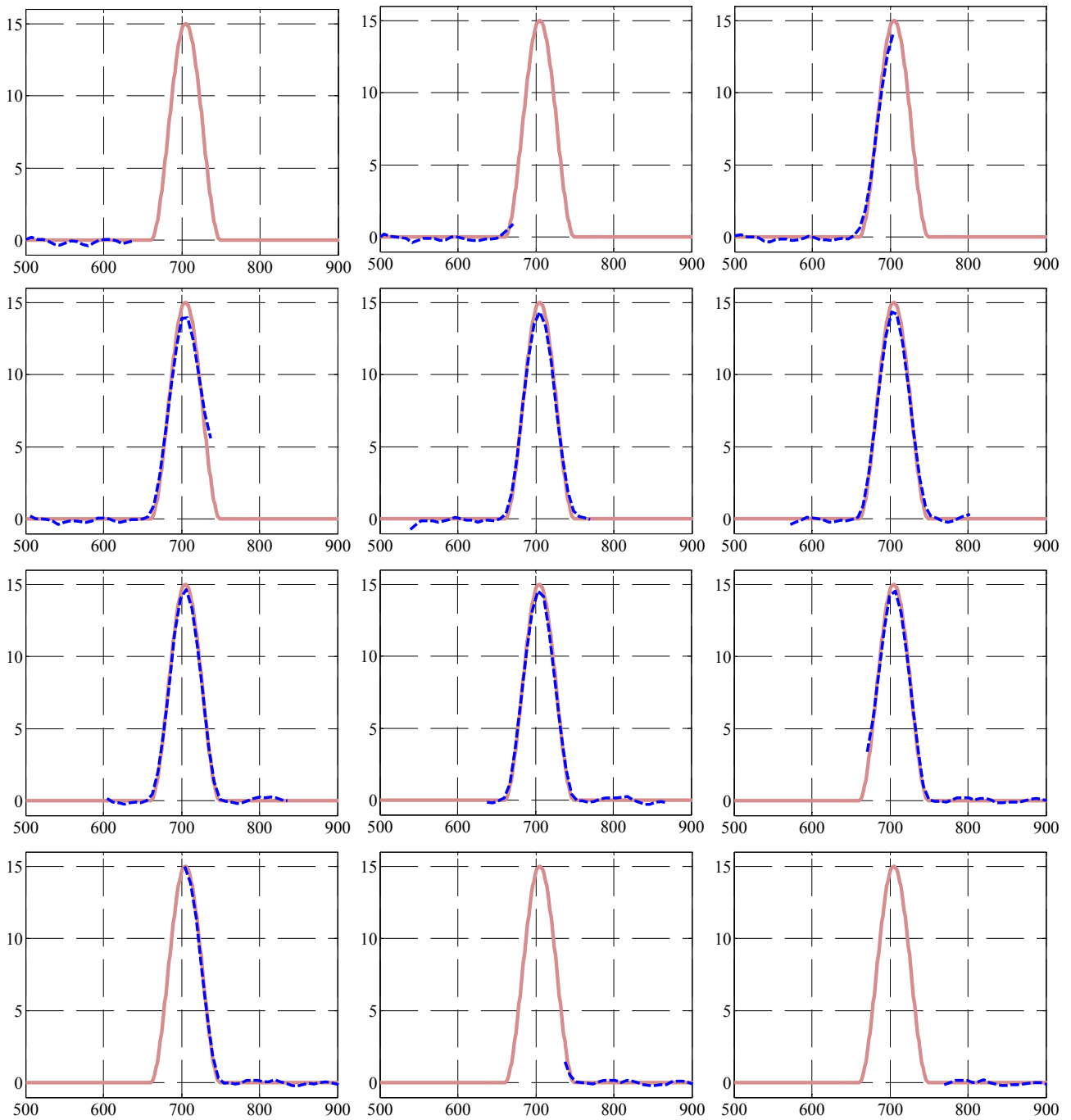


Fig.8 Wind profile after each execution. Axes as in Fig.7: vertical wind in m/s versus geodetic position in meters. Light coral red line represents the “true profile” and the dashed-blue line the reconstructed profile.

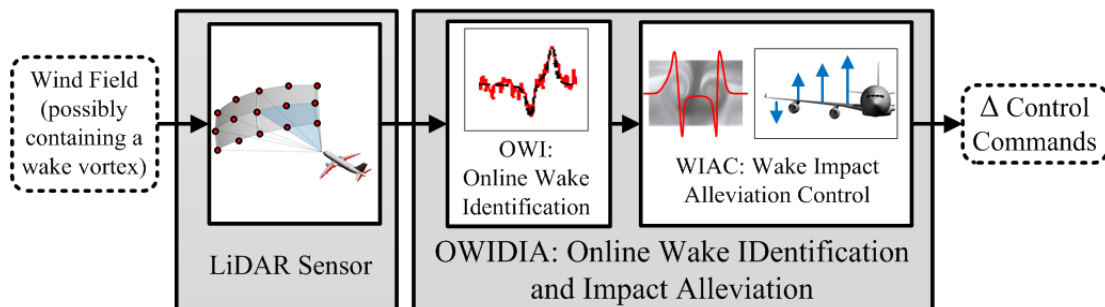


Fig.9 Schematic representation of the Online Wake IDentification and Impact Alleviation (OWIDIA) system

The overall performance of the system is strongly dependent on the characteristics of the LIDAR measurement. As the control surface deflections commanded by the OWIDIA system are generated directly on the basis of the identified flow disturbances, a poor match of the wake vortex model with the actual wake disturbance strongly impairs the alleviation of the wake-induced aircraft response and, in the worst case, can even lead to an increased aircraft reaction. An extensive parameter study analyzing the sensitivity of the wake impact alleviation performance with respect to different parameters of the LIDAR sensor was presented in [1]. The scan pattern of the LIDAR sensor assumed in this study differs from the scan mechanism considered for the gust characterization application in section 4.1. Instead of scanning a cone, the LIDAR sensor measures the wind velocities at measurement points at a fixed range. Consequently the measurement point locations are distributed on a sphere whose center is at the sensor location as illustrated in Fig.10. The line-of-sight directions were defined based on a lateral and a vertical scan angles $\Delta\Psi$ and $\Delta\Theta$. The respective lateral and vertical angles of view Ψ_{scan} and Θ_{scan} are parameters of the sensor system. A regular grid (i.e. regular steps for $\Delta\Psi$ and $\Delta\Theta$) was used to define the line-of-sight directions within the sensor angles of view. The blur depth defines the length of measurement domain (cf. section 2), which is called “measurement point” hereafter for the sake of simplifying the wording used.

The differences between the used scan patterns between both applications is not the result of a particular optimization of these scan patterns for each application, but rather an indirect consequence of having developed both applications in different projects. The experience gathered over the last years on both applications showed the authors that the performance of a particular scan pattern can hardly be predicted without a worst-case search in a fully coupled (including aircraft motion, reaction, etc.) simulation environment. OWIDIA was not tested with the cone-shape scan motion yet and the feedforward active load alleviation was also not tested with the pattern of Fig.10 yet. The respective performance obtained with these patterns on the other application is consequently not known yet.

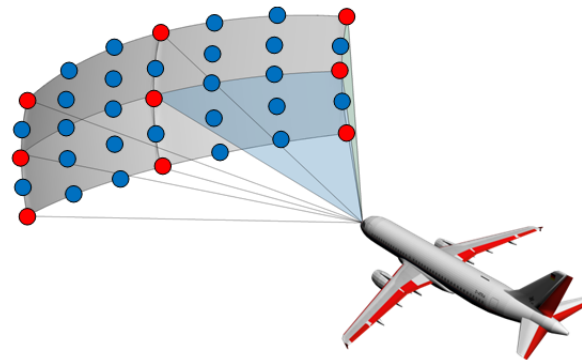


Fig.10 LIDAR sensor scan pattern used for the wake vortex application (only the red points are considered in the 3x3 measurement geometry)

In [1] the authors showed a parameter study involving only four wake encounter geometries were considered but numerous LIDAR measurement geometries (field of view, number of points, refresh rate, blur depth, range) were systematically investigated based on a fully coupled simulation environment (wake, flight dynamics, LIDAR sensor, flight control system). Different sets of adequate LIDAR parameter combinations (variations in measurement geometry and its consequences in terms of noise level) with which the OWIDIA system can reduce the maximum bank angle during the wake vortex encounter by 60-70% could be identified for the encounter scenarios considered in [1]. That means that the maximum bank angle the aircraft experiences during the whole simulation (which includes the flight through the wake vortex) when the OWIDIA system is active is 60-70% lower than the maximum bank angle for the same encounter when OWIDIA is not applied.

In the parameter analysis of [1], only a very limited number of encounter scenarios with a wide range of different LIDAR parameters were considered because the purpose was to get some insight into the sensitivity of the system performance with respect to the LIDAR parameter values. Apart from the LIDAR parameter variations, four different lateral encounter angles between the vortex centerline and the aircraft flight path (i.e. 5°, 10°, 15° and 30°) were simulated. The vertical offset between the vortex centerline and aircraft flight path was always 2 m. A positive altitude difference means that the vortex centerline is located above the center of gravity of the aircraft. Recent analysis results show that this small altitude offset represents a favorable encounter geometry because the wake vortex is located approximately in the center of the field of view of the LIDAR measurements. If the altitude offset between the wake vortex and the aircraft is varied, the OWIDIA performance in terms of maximum bank angle reduction also shows strong variations. Fig.11 shows the reduction of the maximum bank angle (during the whole encounter duration) for horizontal wake vortex encounter (i.e. vortex is horizontal and aircraft initial flight path is also horizontal) with 5° lateral encounter angle and different vertical positions of the wake vortex with respect to the aircraft applying a 3x3 measurement point scan array. In both cases, when the OWIDIA system is active (red crosses) or inactive (blue circles),

the basic control system of the aircraft, which corresponds to the normal law of an Airbus A320, is active. The autopilot is not engaged and there are not pilot inputs during the whole encounter. The LIDAR parameters correspond to a LIDAR set identified in [1] as a LIDAR set with comparably low requirements for the LIDAR sensor but good alleviation performance. The LIDAR sensor has 3 vertical and 3 lateral scan axes at 75 m ahead of the aircraft in a scan field-of-view of $\pm 10^\circ$ in vertical and $\pm 16^\circ$ in lateral direction. The field-of-view update rate of the nine measurement points is 10 Hz, the blur depth is 15 m, and the noise level is: $\sigma_{LoS,3x3} = 0.65 \text{ m/s}$.

It can be seen in Fig.11 that the wake impact alleviation in terms of bank angle reduction is very successful only for 45 to 60% of the altitude offsets tested. In other cases the maximum bank angle is not significantly reduced or even strongly increased in a few cases. The results of [1] gave the impression that this LIDAR parameter set provides adequate performance. The new results, however, show that the performance (with these LIDAR parameters) is quite sensitive to the encounter geometry and insufficiently robust.

In Fig.11, the left-most seven as well as the right-most three simulations correspond to cases for which no or only little effects of the wake vortex was observable through the measurements (vortex too far below or above the aircraft flight path). In these cases, the wake identification algorithm was either never started or did not find a plausible result if started, cf. [1] for further details on the start criteria and on the plausibility checks. The fact that the system is not activated is not critical in these cases, since the influence of the wake vortex is low at these distances.

The next three cases as well as the encounter with an altitude offset of $\Delta H = 23 \text{ m}$ case correspond to situations where the algorithm was started and found at least once a result that seemed plausible. In such a case the wake impact alleviation function uses that information, but it turns out that the information was not good enough and caused a deterioration of the aircraft reaction. Such cases are unacceptable and must be prevented.

The remaining cases show on average more than 50% improvement with negligible improvements or deteriorations in a few of these cases and some significant improvement in the majority of these cases. Even though the average performance is surprisingly good for the considered configuration, the irregularity in the alleviation performance is clearly unsatisfying.

For the parameter study in [1] and for the simulations shown in Fig.11 the LIDAR measurements that have been stored in the data buffer over the last 2 s are considered for the online wake identification. The value of 2 s was selected because it seemed to constitute a good tradeoff between computation time and adequate information about the wake vortex disturbance. An increase in data buffer capacity causes a proportional increase in the computation time required to evaluate the wake model outputs. Consequently, the wake characterization becomes computationally more expensive. Moreover, considering a large timeframe of LIDAR measurements also implies that many measurement locations are located outside the area where the wake vortex has a significant influence. Including many of these measurements without information of the wake vortex but only measurement noise can slightly impair the convergence to a good identification result.

For small encounter angles like the 5° lateral encounter, however, it turned out that considering measurements of the last 2 s only is not sufficient. Due to the small encounter angle the wake vortex remains much longer in the field of view of the LIDAR sensor. Measurements older than 2 s thus still contain information about the wake vortex and would be beneficial to be included in the wake estimation process. Fig.11 shows the 5° lateral encounter for different wake altitudes when the data buffer of the OWIDIA system contains LIDAR measurements over the last 2 s. The blue dots in Fig.12 mark the maximum bank angle when the OWIDIA system is applied with the same LIDAR settings as shown in Fig.11 but with a data buffer containing measurements over 4 s instead of 2 s. It can be noticed that wake impact alleviation is improved compared to the case when only measurement over the last 2 s are considered in the online wake identification. Nevertheless, there are still five altitude offsets between the wake vortex and the aircraft for which the OWIDIA system leads to an increase of the maximum bank angle. In five other cases, the alleviation performance is not very good. Nevertheless, in about 80% of the cases the alleviation performance is really good and certainly well beyond the expected results for this sensor configuration.

The green squares in Fig.12 denote the maximum bank angle which occurs during the wake encounter when LIDAR sensor with a higher spatial resolution is applied. This LIDAR sensor has 5 vertical and 7 lateral measurement directions. The field-of-view update rate for all 35 measurement stays at 10 Hz and the measurement range is set to 90 m. The field of view is increased to $\pm 10^\circ$ in vertical and $\pm 30^\circ$ in horizontal direction. The blur depth is 30 m and the noise level is here higher than in the previous case: $\sigma_{LoS,5x7} = 0.79 \text{ m/s}$. In this case the OWIDIA never aggravates the maximum bank, the evolution of the alleviation performance over the altitude range does not contain outliers anymore, and the achieved bank angle reduction is very significant.

For all wake vortex encounters presented so far, the wake vortex disturbance is modelled as an analytical Burnham-Hallock wake vortex (cf. section 3.1). Real wake vortices are possibly more complex, non-uniform, and can only partially be described with such a simplified model. A more representative way to model wake vortices is to compute the flow field using Large Eddy Simulations (LES) (cf. [25]). This approach can cover more details of the wake physics

like wake deformation and decay. Fig.13 shows 5° lateral encounter with a LES wake vortex. The LES wake vortex is embedded in a three-dimensional field whose geometrical reference cannot easily be compared to the reference system used for the analytical vortex of Fig.11 and 12, leading to about 55 m altitude offset between these coordinates. The overall shape of the results shown in Fig.11 and 12 is nevertheless very similar to those of Fig.13 and eases the comparison between these cases. In Fig.13, the simulated wake vortex has an age of 16 s, which is rather young for a wake vortex encounter but justified here by the fact that the results at this age shall be easier to compare with an analytical vortex because at this age the decay process has hardly begun and the two vortex centerlines are still relatively straight and parallel. Nevertheless the wake vortex differs from the analytical Burnham-Hallock model used inside the online wake identification process, which makes the identification possibly more challenging. The results shown in Fig.13 demonstrate, however, that even in this more challenging case of a more complex model of the wake vortex disturbance the OWIDIA performs very well.

When the OWIDIA system is applied with the lower resolution LIDAR sensor with 3 lateral and vertical measurement axes there are two cases in which the OWIDIA system aggravates the maximum bank angle. Note, however, that these two cases are relatively uncritical looking at the respective amplitudes. More importantly, the average alleviation performance on the other cases is still in the order of 60%, but nonetheless significantly worse than with the analytical Burnham-Hallock wake vortex.

In the case of the higher resolution LIDAR sensor with 5 vertical and 7 lateral measurement axes, the OWIDIA system works very well for the LES wake vortex as well (see Fig.13). At all but two altitudes the maximum bank angle is impressively reduced (more than 65-70%, often even approximately 90%). The exception is for an altitude offset of $\Delta H = 30 \text{ m}$, for which only a slight improvement was achieved. The vortex impact in this case is very low and the vortex is also quite far from the sensor measurement zone. The wake encounters during which the wake alleviation was not activated only induced absolute bank angles lower than 5°. For both types of vortices (Burnham-Hallock in Fig.12 and LES in Fig.13) and for most altitude offsets, the reached bank angle absolute values are well below 5° when the OWIDIA system is applied, compared to maximum bank angles without OWIDIA of 20° or larger. The worst case was obtained with the LES wake vortex (Fig.13) at an altitude offset of 62.5 m. In this case the maximum bank angle did not exceed 11°, which is still a significant reduction compared to the 28° maximum absolute bank angle obtained in the same case without OWIDIA. Note also that with the 5x7 configuration the OWIDIA system is either active and very effective or not active due to insufficient information on the vortex (absolute altitude offset too large). No region with poor performance is observable at the boundary between these domains.

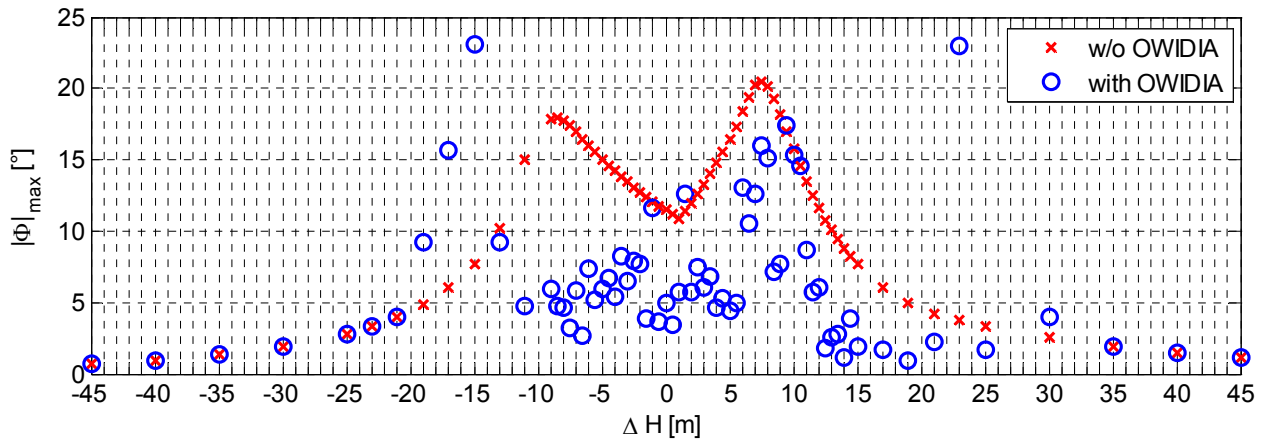


Fig.11 Reduction of maximum bank angle with OWIDIA using LIDAR sensor with a grid of 3x3 measurement points and a 2 s buffer for different wake altitudes. Lateral encounter angle is always 5°. Wake vortex model: Burnham-Hallock.

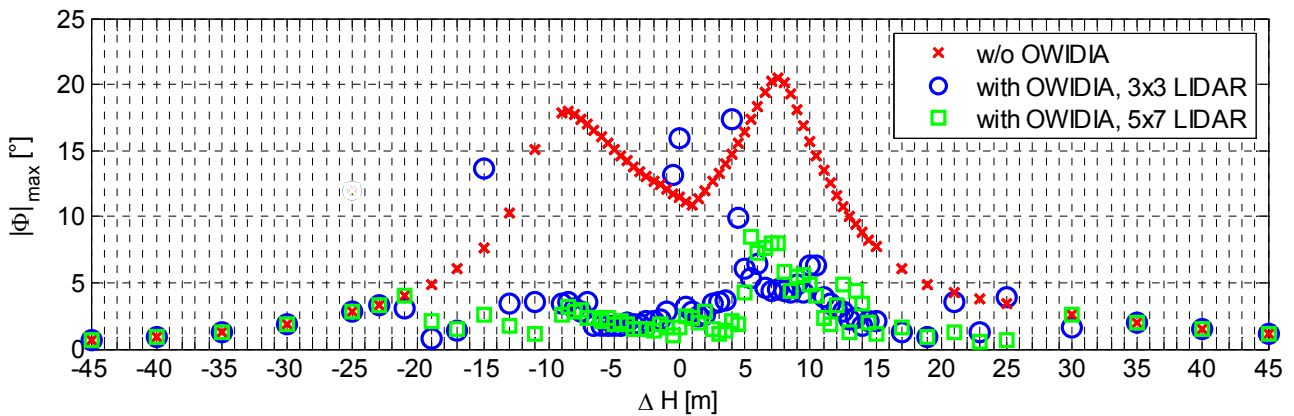


Fig.12 Reduction of maximum bank angle with OWIDIA with 4 s data buffer for different wake altitudes. Lateral encounter angle is always 5°. Wake vortex model: Burnham-Hallock. Blue circles: same sensor as in Fig.11 but with 4 s buffer. Green squares: sensor with higher spatial resolution (5x7 instead of 3x3) also with 4 s buffer.

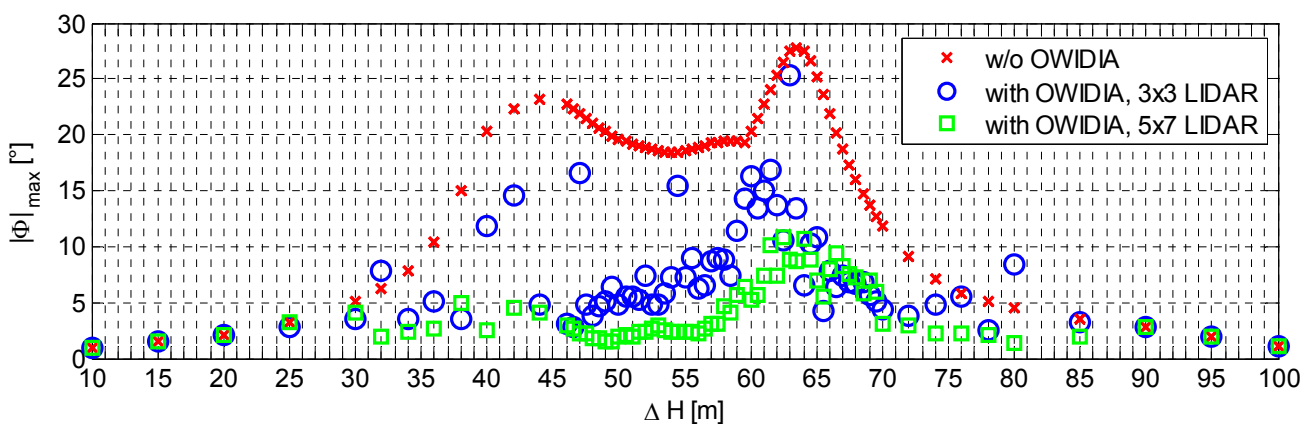


Fig.13 Reduction of maximum bank angle with OWIDIA with 4 s data buffer for encounter with 16-s-old LES wake vortex at different altitudes. Same sensor configurations as in Fig.12: only difference to Fig.12 is the wake model used.

There is a domain for which the alleviation performance is good but slightly worse than for other altitude offsets. Both LIDAR configurations exhibit this behavior in Fig.12 and 13. This effect shall be investigated further in future work. The respective altitude offset intervals are $\Delta H \in [4 \text{ m}, 15 \text{ m}]$ for the analytical vortex (Fig.12) and $\Delta H \in [59 \text{ m}, 70 \text{ m}]$ for the LES vortex (Fig.13). Even in these intervals, for which further improvements might be possible, the current minimum alleviation performance obtained was still a reduction of 50% of the maximum bank angle. The performance of the OWIDIA system should also be assessed for older LES vortices with stronger deformation. The current identification model provides no parameters for wake deformation. Therefore, it is expected that for strongly deformed vortices the model will have to be extended.

It should be noticed that the LIDAR measurement ranges used for this application to wake impact alleviation is significantly lower than theoretically required when considering the flight speed and the delays involved (computation time as well as bus and actuator delay). From a purely geometrical point of view, with shallow encounter angles (wake vortex close to parallel to the flight path) and with a follower aircraft span of approximately 34 m (i.e. size of an A320), the measurement distance should be approximately 150 m. However, the results presented in [1] show that it is very beneficial to measure at a distance of only 60 to 90 m. The reason for that is that in encounter with shallow angles, the induced forces and moments change very slowly at first and the basic flight control system can counteract these small and low frequency disturbance very well. Moreover, by using an analytical model of the wake vortex in the identification process, the forces and moments that will be induced by the wake vortex onto the aircraft can be predicted beyond the actual sensor measurement range. The choice of a sensor range is therefore not a direct consequence of a simple multiplication between delay and flight speed, but results from a trade-off between foresight horizon, spatial resolution, and measurement noise (which increases with the measurement range), as already shown in [1]. All sensor configurations considered in this paper are practically feasible.

To summarize the results on the wake vortex application it can be stated that they are also very good. The use of remote wind sensors with the Online Wake IDentification and Impact Alleviation creates a very large potential for safety and air traffic capacity improvement.

5. OUTLOOK

As it can be seen in the results shown previously, in-flight remote sensing of line-of-sight velocity components (e.g. Doppler LIDAR) can provide useful information, even if the line-of-sight velocity components are not directly the components that contain the most important information on the considered phenomena. Two quite different applications but using the same type of sensors and the same ideas in terms of measurement post-processing were shown, which illustrates the strong commonality between these applications. The results shown are just some examples among others, which all show the remarkable potential for the onboard remote wind sensing technologies. In addition to these two applications (gust/turbulence load alleviation and wake impact alleviation), other applications using these sensors e.g. to increase air data redundancy may also be very interesting.

Testing the wind reconstruction algorithm on realistic gust shapes and turbulence fields would also be very interesting. Unfortunately, the authors presently do not have such realistic gust/turbulence wind fields at their disposal yet in order to investigate the behavior of the algorithm (including also the associated load alleviation function of [2] and [3]) on these cases.

However, even though there are many attractive applications for these technologies, all these applications are distinct enough to be often investigated within different projects/frameworks. For instance, most research activities for active load alleviation are based on airframe research funding (e.g. CleanSky SFWA-ITD and CleanSky 2 Airframe-ITD). Many research activities on wake vortex (encounter prevention measures, impact alleviation) are mainly based on air transportation research funds (e.g. SESAR & SESAR 2020).

This makes it difficult to develop and exploit the synergies between the different potential applications on the airborne remote sensing technologies and to reach the critical funding size to perform maturation activities and in-flight demonstrations. Maturation activities, for instance developing good airframe integration concepts (with respect to aerodynamics, window heating, instrument cooling, etc.), are needed to make the step from research instruments to real prototypes.

Flight demonstration is also required to characterize the capability of these sensors to cope with all kinds of atmospheric conditions (low aerosol concentrations, water drops, ice, etc.) and to demonstrate the capacity of the post-processing algorithms to characterize real-world gust and turbulence fields or strongly deformed wake vortices well enough for the purpose of the corresponding alleviation functions. Such demonstrations are required to permit the evaluation of the level of reliability that can be reached for the whole system and for the targeted applications. Reliability is crucial for aeronautical systems and the conditions that are needed to test the remote sensing technologies cannot, to the best of the authors' knowledge, be reproduced currently in a ground-based testing environment.

A follow-up activity on the application to gust and turbulence load alleviation is starting within the framework of the

European CleanSky 2 initiative (CS2 AIRFRAME-ITD). This activity will involve some optimization of the gust detection and characterization algorithms, their extensive testing with numerous more complex wind fields (if available turbulence fields from LES will be considered), as well as further activities on the load alleviation controllers that make use of the reconstructed gusts and turbulence field (part outside of the scope of this paper but to be found in [2] and [3]).

On both applications, now that the requirements in terms of configuration and the time-consuming parts of the computations are better known, the numerical algorithms used should be optimized such that the real computational cost can be measured. On the gust/turbulence side, the wind reconstruction algorithm and the load alleviation function should be tested with realistic turbulence fields. On wake vortex side, the extension of the model for deformed wake vortices should be made and the whole system (OWIDIA) tested on these cases too. The slightly lower wake impact alleviation performance observed on the cases $\Delta H \in [4 \text{ m}, 15 \text{ m}]$ for the analytical vortex (Fig.12) and $\Delta H \in [59 \text{ m}, 70 \text{ m}]$ for the LES vortex (Fig.13) should be explained and if possible a way to reach the same alleviation performance than in the other cases should be developed.

6. CONCLUSIONS

Two applications of in-flight remote wind sensing technologies were presented in this paper. The first application considers the use of this technology for the recognition of gusts and turbulence, with the aim of using this information for active load alleviation. In the second application the measurements support the characterization of wake vortices. The knowledge gained on the wake vortices permits to alleviate the impact of this phenomenon on the aircraft and thereby to increase the safety. The paper focuses on the remote sensing and measurement processing and shows the strong similarities between the post-processing algorithms that are needed for both applications. The achieved and presented results for both applications are very good.

Though not directly shown in the present paper, but in a complementary work cited herein, the reconstructed wind profiles are good enough to enable their use for active load alleviation. The processing of a large group of measurements to estimate the wind field/profile ahead of the aircraft is more powerful than the approaches found in the literature (e.g. from the AWIATOR project) where only a few measurements closed to each other where locally combined. In the wake vortex case, the wake characterization is already integrated into the wake impact alleviation control system and the results showed reductions of the maximum bank angle up to 92% and between 75 and 90% in the large majority of the cases for the preferred sensor settings.

Further maturation of both systems shall be performed in the near future. Various uncertainties on the technology and on some assumptions underlying the post-processing algorithms should be verified with real data (e.g. collected in flight). Later on in-flight demonstration of the complete systems (including alleviation) should ideally be performed to further mature the whole systems.

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