

1 **IMPROVED TRAFFIC STATE ESTIMATION BY BAYESIAN NETWORK DATA**  
2 **FUSION OF V2X AND VEHICULAR BLUETOOTH DATA**

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**1 ABSTRACT**

2 A recently published probabilistic method for vehicle based traffic state estimation on the basis of  
3 fusing two wireless communication based technologies, i.e. Bluetooth and Vehicle-to-X communi-  
4 cation data, is analyzed in three different scenarios ranging from “academic” to “realistic”. On the  
5 one hand there is accurate, but extremely rare V2X speed data and on the other, there is frequent,  
6 but inaccurate speed data based on a one unit Bluetooth reader approach. Therefore, this analysis  
7 takes into account specific traffic related variables, such as traffic flow and traffic density as well  
8 as traffic light control (TLC), which affect the Bluetooth based detection results. The findings are  
9 used to improve the method. A Bayesian Network (BN) is developed that merges Bluetooth and  
10 V2X based speed detection results to provide an improved speed estimation. The novel BN is  
11 compared to the previous one for different V2X penetration ratios using the open source micro-  
12 scopic traffic simulation package SUMO (Simulation of Urban MObility). The results show that  
13 the novel method can improve the vehicular speed estimation in the academic as well as in the  
14 realistic scenarios.

15

16 *Keywords:* V2X communication, Bluetooth, Bayesian Networks, Data Fusion, Traffic Manage-  
17 ment, Traffic State Estimation, COLOMBO, Digitaler Knoten 4.0

## 1 INTRODUCTION

2 An accurate and reliable estimation and prediction of the traffic state is a key task of Traffic Man-  
3 agement Centers (TMC) to make traffic safer, cleaner and more efficient. Cameras, radar systems,  
4 loop detectors and other sensor technologies have been in use successfully for decades to obtain in-  
5 formation about the number of road users and their microscopic properties like speed, acceleration  
6 and origin-destination behavior. Intelligent Traffic Light Control (TLC) algorithms take advantage  
7 of these information to achieve a local, a section based or even network wide optimized traffic state  
8 adequate TLC algorithm with a minimum of waiting or loss times.

9 In the European funded project COLOMBO<sup>1</sup> (1) the aim was to pay attention to a reliable  
10 traffic state estimation by developing and providing "...a set of methods for traffic surveillance and  
11 traffic control applications that target at different transport related objectives, such as increasing  
12 mobility, resource efficiency, and environmental friendliness" (2). One aspect of COLOMBO was  
13 to adopt data sources for this purpose, which particularly take into account availability, accuracy,  
14 resource efficiency and costs.

15 Some of the established sensor technologies provide accurate and reliable data, but lack  
16 applicability for different reasons. Loop detectors, for instance, are labor-intensive and require  
17 costly installation and maintenance. Camera sensors provide wide-area traffic data, but have to  
18 cope with occlusion phenomena and weather dependencies, such as snow and sun-glare (3, 4).  
19 Radar sensors and loops are traffic state dependent, since they provide less accurate data at low  
20 vehicular speeds. On the other hand there are low price communication based sensors, such as  
21 Bluetooth or even WiFi detectors, which suffer from the equipment ratio of Bluetooth/WiFi devices  
22 on board of vehicles. Although only a fraction of road users can be detected (3% to 50% depending  
23 on urban/suburban area, penetration ratio, street type, amount of trucks, speed limit, etc. (5, 6)),  
24 they have great potential for different traffic management purposes.

25 The fusion of dynamic data of connected vehicles, e.g. on board diagnostic and sensory  
26 data, with static road data, e.g. map and road geometry data, is state of the art (7). In contrast,  
27 fusing vehicular data with dynamical infrastructure based data for automation purposes is cur-  
28 rently intensively under research, e.g. estimation of the risk of collision between right turning mo-  
29 torists and straight driving cyclists (8, 9). Also, self-organizing TLC algorithms were developed,  
30 which make use of sparse traffic data provided by cooperative communication based sensors, such  
31 as Vehicle-to-Infrastructure (V2I) or Vehicle-to-Vehicle (V2V) (10, 11). The abbreviation V2X  
32 (Vehicle-to-X communication) combines them to a single term. Vehicles equipped with V2X tech-  
33 nology periodically exchange information via Cooperative Awareness Messages (CAM) with other  
34 vehicles or Road Side Units (RSU) on a vehicular-specific extension to the WiFi ad-hoc mode  
35 IEEE802.11p (12). These information could be used to feed a TLC algorithm to obtain a maxi-  
36 mum of traffic safety taking into account a maximum of efficiency in traffic flow. However, car  
37 manufacturers expect to take years to achieve sufficient V2X penetration ratios of 1% to 3%, which  
38 makes powerful TLC algorithms on the basis of accurate speed data a real challenge (13). This  
39 motivates the fusion of Bluetooth and V2X data for speed estimation.

40 In regards of the COLOMBO project Junghans and Leich (13) showed that accurate ve-  
41 hicular speed data can be obtained by fusing extremely rare, but rather accurate V2X data, with  
42 frequent, but less accurate Bluetooth data. Although these results cannot be used for TLC yet at  
43 very low V2X penetration ratios, they proved their usefulness. In regards to the project "Digitaler

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<sup>1</sup>Cooperative Self-Organizing System for low Carbon Mobility at low Penetration Rates

1 Knoten 4.0" (14) this method is reviewed in detail and its improvement makes use of the recent  
 2 findings in (15), which may be the basis for traffic adaptive TLC algorithms on the basis of V2X  
 3 and vehicular Bluetooth data. These investigations are obtained by coupling the microscopic traffic  
 4 simulator SUMO (Simulation of Urban MObility) with a probabilistic speed estimator on the basis  
 5 of Bayesian Networks (BNs).

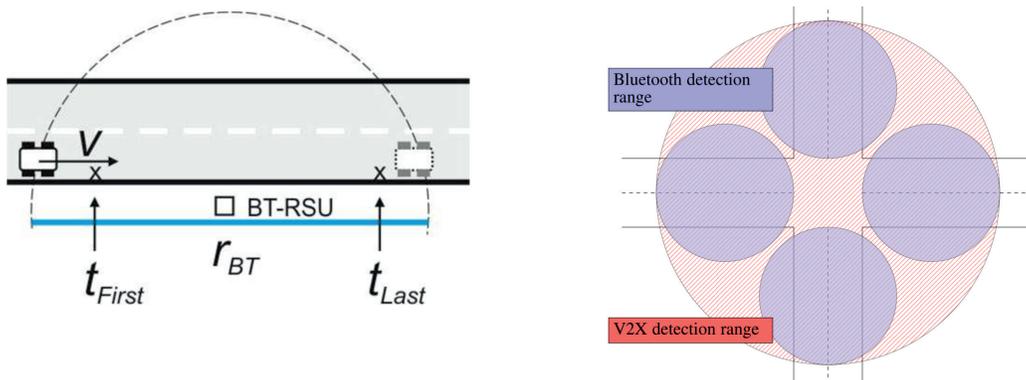
6 The paper is organized as follows: In the next section the methodical approach of traffic  
 7 state estimation with Bluetooth and V2X is described and analyzed with regard to specific bound-  
 8 ary conditions. Then, the general simulation setup and the experimental results are described.  
 9 Finally, conclusions and future prospects are given.

## 10 PROBLEM ANALYSIS

11 In this section the methodical approach is described how speed data can be obtained by a one unit  
 12 Bluetooth reader. Then, BNs are applied to formulate the fusion task of Bluetooth based speed  
 13 sensor with a V2X based one. Further, this BN is analyzed in detail. Finally, on the basis of novel  
 14 findings the resulting BN is created. Further simulative analyses follow.

### 15 Methodical Approach

16 As stated in (13), RSUs for V2X communication receive the broadcast speed information by CAMs  
 17 of the vehicles equipped with V2X technology. Due to the expected extremely low penetration  
 18 ratios of V2X vehicles it is challenging to obtain reliable speed estimations for the remaining road  
 19 users. On the other hand, they frequently use Bluetooth devices (e.g. Bluetooth speakers, hands-  
 20 free equipment, navigation systems) and thus, their occupancy can be detected by their device  
 21 identification number, e.g. MAC address, within a specific detection range. This is due to the  
 22 Bluetooth inquiry process (16), which characterizes the handshaking procedure between Bluetooth  
 23 sender and receiver. It results in the exchange of the device IDs of the communication partners.  
 24 Typically, two Bluetooth detectors are applied to obtain accurate and reliable speed information:  
 25 One detector is mounted at position 1, the other at position 2. Knowing the distance between  
 26 both positions and the time interval needed for road users to pass positions 1 and 2 enables the  
 27 determination of the journey time.



**FIGURE 1 Left: Principle of Bluetooth based speed detection with a one unit Bluetooth reader (13); right: Schematic diagram of V2X and Bluetooth based detection ranges (15)**

28 In (13) it was shown that speed information  $v_{BT}$  can also be obtained by a single Bluetooth  
 29 reader unit taking into account the time of first  $t_{first}$  and last detection  $t_{last}$  of the road user as well

1 as the detection range  $r_{\text{BT}}$  (see left side of figure 1):

$$2 \quad 3 \quad v_{\text{BT}} \approx \frac{r_{\text{BT}}}{t_{\text{last}} - t_{\text{first}}}. \quad (1)$$

4  
5 These assumptions are rather idealistic, since detection ranges of such Bluetooth/WiFi readers  
6 strongly depend on their antenna characteristics, environmental and other influencing factors. On  
7 the other hand those assumptions serve to find out whether the method is promising and what as-  
8 pects have to be considered further. Looking again at equation (1), we can state that the slower a  
9 road user passes through  $r_{\text{BT}}$  the more accurate the speed estimation is. Fast moving road users will  
10 be detected only once or not at all, which consequently leads to problems in speed estimation. Fur-  
11 ther,  $v_{\text{BT}}$  is always over-estimated, since the Bluetooth inquiry process will neither instantaneously  
12 detect a Bluetooth device the first time it enters  $r_{\text{BT}}$  nor the last time before it leaves  $r_{\text{BT}}$  (15).  
13 Consequently, the estimation of  $v_{\text{BT}}$  is rather rough. However, such a rough speed estimation re-  
14 sult can be improved by merging Bluetooth based speed observation results with highly accurate  
15 V2X speed data. Obviously, analyzing traffic in detail seems to be a reasonable way to improve  
16 the quality of the Bluetooth based speed estimation and consequently the fused speed estimation  
17 results. In order to understand how V2X and Bluetooth signals could be merged we first want to  
18 show the different detection ranges of Bluetooth and V2X—on the right hand side of figure 1 the  
19 detection ranges of V2X ( $\approx 200$  meters) and Bluetooth ( $\approx 30$  meters in case of Bluetooth class 2  
20 readers<sup>2</sup>) are depicted taking into account an idealized Bluetooth and V2X road side unit (RSU)  
21 placed in the middle of the intersection.

## 22 Bayesian Network based Data Fusion

23 Bayesian Networks (BNs) are well-established to quantify cause-effect relationships by conditional  
24 probability density functions and make diagnoses by inferring expert knowledge or observation re-  
25 sults of the applied sensors and combining them with stationary or instationary a-priori knowledge.  
26 The authors recommend to refer to (17–19) for detailed insights in BNs, their structure, computa-  
27 tional characteristics and applications.

28 In figure 2 (left hand side) a naïve BN is depicted. It consists of the node  $V$  as un-  
29 known speed variable and the two sensor nodes  $V_{\text{BT}}$  and  $V_{\text{V2X}}$  observing  $V$ , i.e. measuring speed.  
30 Clearly, the realizations  $v \in V$  where  $V$  denotes the set of all  $n$  possible discrete speed classes  
31  $V = \{v_1, \dots, v_n\}$  cause the observation results  $v_{\text{BT}} \in V_{\text{BT}}$  and  $v_{\text{V2X}} \in V_{\text{V2X}}$  with  $V_{\text{BT}}$  and  $V_{\text{V2X}}$  de-  
32 fined similarly. The joint probability density function is given by equation (2) taking into account  
33 the structural Markov property of BNs (17):

$$34 \quad 35 \quad P(v, v_{\text{BT}}, v_{\text{V2X}}) = P(v) \cdot P(v_{\text{BT}}|v) \cdot P(v_{\text{V2X}}|v). \quad (2)$$

36  
37 If observation results have occurred at the nodes  $V_{\text{BT}}$  and  $V_{\text{V2X}}$  these diagnostic evidences are  
38 spread through the BN to affect  $V$ , i.e. to diagnose what to expect at  $V$  given the values of  $v_{\text{BT}}$  and  
39  $v_{\text{V2X}}$ . This can be computed by the a-posteriori probability density function with normalization  
40 constant  $\alpha^{-1} = P(v_{\text{BT}}, v_{\text{V2X}})$ :

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<sup>2</sup>Note that there are three classes of Bluetooth readers, which vary in their detection ranges, i.e. class 1:  $\approx 100$  meters, class 2: 10-50 meters, class 3: 1-10 meters.

1

$$2 \quad P(v|v_{\text{BT}}, v_{\text{V2X}}) = \alpha \cdot P(v) \cdot P(v_{\text{BT}}|v) \cdot P(v_{\text{V2X}}|v). \quad (3)$$

3

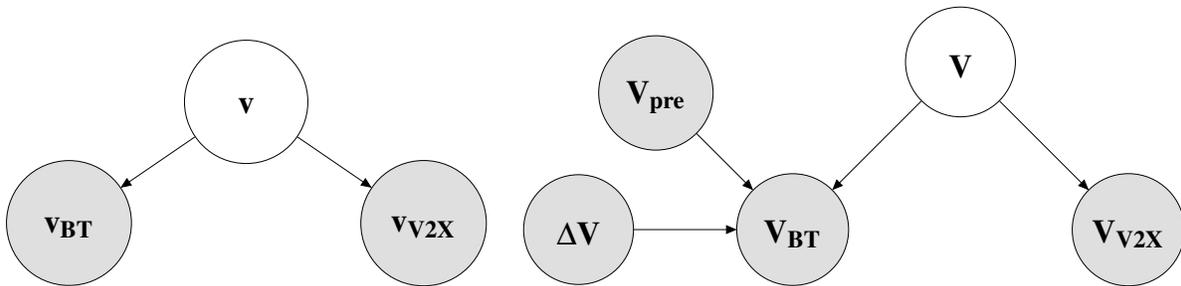
4 where

- 5 •  $P(v|v_{\text{BT}}, v_{\text{V2X}})$  is the a-posteriori probability density function needed to estimate  $v$  given the observation results  $v_{\text{BT}}$  and  $v_{\text{V2X}}$ ,
  - 6 •  $P(v)$  is the a-priori probability density function of the underlying speed variable characterizing the stationary expectation on  $V$ ,
  - 7 •  $P(v_{\text{BT}}|v)$  and  $P(v_{\text{V2X}}|v)$  are the corresponding sensor likelihoods for Bluetooth and V2X.
- 8 These sensor likelihoods are conditional probability density functions that quantify the behavior of the sensors with regard to  $v$ .

9 In the next subsection these equations are used to derive accurate speed estimations by inferring observation results of the Bluetooth and V2X sensors. In general, it can be stated that BNs are capable of probabilistically combining several sensors in order to provide reliable and accurate data of some stochastic variable as shown in (20–22).

### 16 Analysis of the BN

17 On the right hand side of figure 2 a BN is shown that was used for first investigations for accurate speed estimations (13). It contains variables that have an influence on the traffic state and hence, may affect speed estimation. Node  $V$  expresses the unknown mean instantaneous speed of a vehicle passing through the common detection area of Bluetooth and V2X sensors; node  $V_{\text{V2X}}$  represents the V2X sensor node observing speed and  $V_{\text{BT}}$  represents the Bluetooth sensor node observing speed as well. The nodes  $V_{\text{pre}}$  and  $\Delta V$  represent the mean instantaneous speed of the preceding vehicle equipped with a Bluetooth sensor and the difference of the current speed with the previous one, respectively, thus  $\Delta V = V_{\text{pre}} - V_{\text{BT}}$ . Therefore, the nodes  $V_{\text{pre}}$  and  $\Delta V$  were considered to affect the speed observation results of the Bluetooth sensor, due to the assumption that traffic conditions do not change quickly in case of two vehicles following each other.



**FIGURE 2 Naïve BN (left) and improved BN from (13) (right)**

27 In (13) the BN on the right of figure 2 was adopted for optimal speed estimation of an academic intersection (figure 4 left) for changing V2X penetration ratios of [0; 1; 2; 5; 10; 20; 50; 100] % and a constant Bluetooth penetration ratio of 30%. The authors obtained speed estimation accuracies between an RMSE of [1.7; 5.3]m/s and completeness values of [33.6; 38.6] % at a V2X penetration value of only 1% at the four arms of this intersection. Klüber (15) analyzed this BN to identify influencing factors, which improve the speed estimation quality. The following traffic process related variables were taken into account to have an influence on the Bluetooth based speed

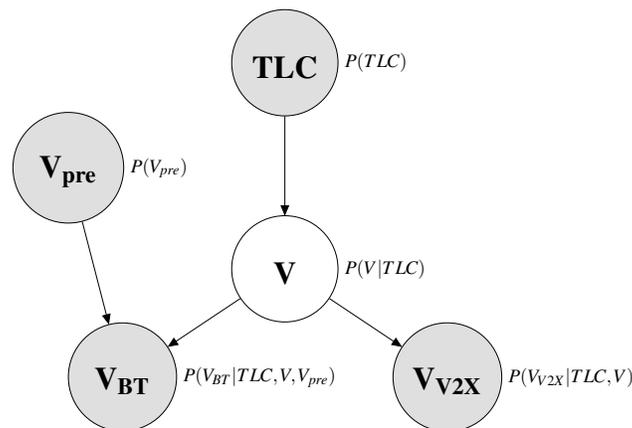
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1 estimation:

- 2 • **Traffic flow  $Q$  and density  $D$ :** Both variables correspond with each other by the funda-  
 3 mental flow relation  $Q = v \cdot D$  in case of an ergodic traffic process (4).  $D$  and  $Q$  affect  $V_{BT}$ .  
 4 In the experimental results it appeared that although  $D$  and  $Q$  have an influence on  $V_{BT}$   
 5 the effect was marginal; only for heavy traffic it made sense to consider them in the BN.  
 6 Therefore  $Q$  and  $D$  were not considered for later analyses.
- 7 • **Traffic light control  $TLC$ :** In the investigations made a fixed-time TLC program was  
 8 running. Since vehicles accelerate to their desired speeds and then constantly continue at  
 9 that speed in case of green light and decelerate to zero for red light, it seems reasonable to  
 10 model TLC as a separate node in the BN. Further, the Bluetooth based speed estimation  
 11 is dependent on the vehicles' speeds. The slower a vehicle is the more accurate the  
 12 Bluetooth based speed detection. Finally, in all investigations it turned out that modeling  
 13 the BN with an additional TLC node had a significant influence on the quality of  $V_{BT}$ .  
 14 Experiments using a TLC node have shown that results improve when splitting the green  
 15 phase in an accelerating phase *green1* in the first seconds of the green phase and a free  
 16 flow phase *green2*. Best results were obtained when splitting the phases after 7.5 s of  
 17 green light.
- 18 • **Preceding Bluetooth speed  $V_{pre}$ :** As described above, it is assumed that traffic condi-  
 19 tions change over time slowly, thus it seems reasonable to assume that the speeds of  
 20 leader and follower vehicles should not be too dissimilar. Therefore, it is assumed that  
 21  $V_{pre}$  affects  $V_{BT}$  as well. Our experiments showed that it is indeed reasonable to model  
 22 this variable in the BN.
- 23 • **Speed difference  $\Delta V$ :** The speed difference of the current Bluetooth vehicle with its  
 24 preceding is a redundant information, thus this node was deleted from the BN. The ex-  
 25 perimental results confirmed this.

## 26 Final BN and Fusion equation

27 On the basis of (15) the final BN for merging rare but accurate V2X speed data with frequent but  
 28 rather inaccurate single unit Bluetooth based speed data is depicted in figure 3.



**FIGURE 3 Improved BN taking into account the node TLC. Additionally, the probability density functions are shown**

1 This BN consists of the hidden physical speed node  $V$  and the two sensor nodes  $V_{BT}$  and  
 2  $V_{V2X}$  for speed estimation of the Bluetooth and V2X based sensors as in the BNs applied before.  
 3 As shown in figure 3 the speed of the preceding Bluetooth vehicle affects the current Bluetooth  
 4 based detection. In addition the node  $TLC$  with its realizations  $tlc \in TLC$  models the traffic light  
 5 control.

6 The joint probability distribution of the BN shown in figure 3 can be derived easily:

$$8 \quad P(v, v_{BT}, v_{V2X}, v_{pre}, tlc) = P(v|tlc) \cdot P(v_{pre}) \cdot P(v_{BT}|v) \cdot P(v_{V2X}|v). \quad (4)$$

10 The resulting fusion equation  $P(v|v_{BT}, v_{V2X}, v_{pre}, tlc)$  can be computed with the normalizing con-  
 11 stant  $\alpha^{-1} = P(v_{BT}, v_{V2X}, v_{pre}, tlc)$  by applying message passing, as described in (18):

$$13 \quad P(v|v_{BT}, v_{V2X}, v_{pre}, tlc) = \alpha \cdot P(v|tlc) \cdot P(v_{pre}) \cdot P(v_{BT}|v, v_{pre}) \cdot P(v_{V2X}|v). \quad (5)$$

15 In equation (5)  $P(v|v_{BT}, v_{V2X}, v_{pre}, tlc)$  is the a-posteriori probability density function of the desired  
 16 speed taking into account the a-priori knowledge about the unknown physical speed with regard to  
 17 the state of the traffic light  $P(v|tlc)$ , the sensor likelihood of V2X  $P(v_{V2X}|v)$  and the sensor like-  
 18 lihood of Bluetooth  $P(v_{BT}|v, v_{pre})$  considering the influence of the previously detected Bluetooth  
 19 vehicle on the current measurement.

## 20 EXPERIMENTAL RESULTS

21 In this section experimental setup and road network scenarios are analyzed and the obtained results  
 22 of speed estimation are presented. The open source microscopic traffic simulator Simulation of  
 23 Urban MObility (SUMO) was used (23). SUMO enables the integration of traffic flows on custom  
 24 road networks as well as the simulation of Bluetooth and V2X detectors. Various combinations of  
 25 Bluetooth and V2X penetration ratios are examined.

### 26 Experimental setup

27 The experiments were conducted using the following core parameters and methods in three differ-  
 28 ent scenarios ranging from “simply academic” to “realistic”:

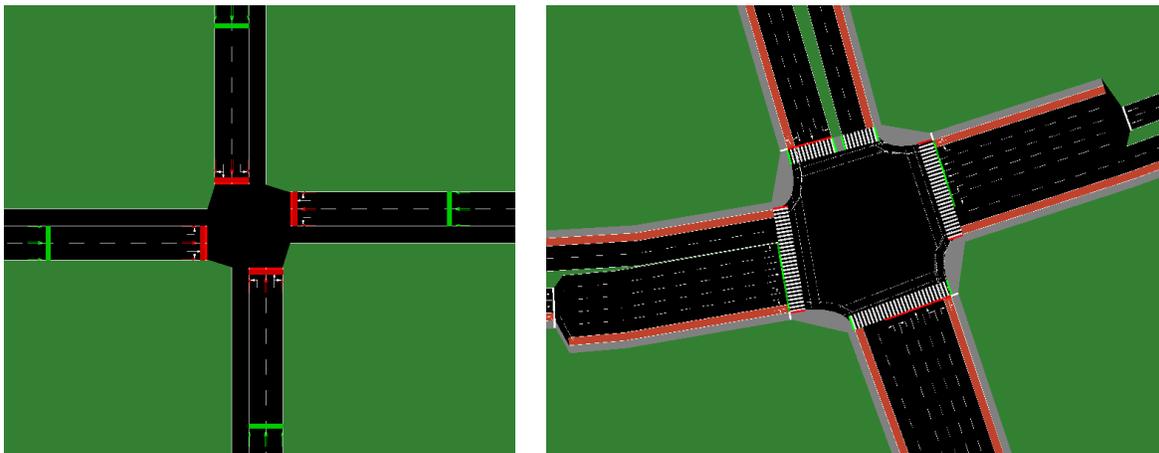
- 29 • *Training*: Data from 500 detection runs were used to quantify the sensor likelihoods
- 30 • *Simulation time*: 3600 s
- 31 • *Detection ranges*: Bluetooth: 30 m, V2X: 200 m
- 32 • *Penetration ratios*: Bluetooth: [0, 30, 50, 100]%, V2X: [0, 1, 5, 10, 20, 50, 100]%
- 33 • *Maximum speed*: 50 km/h ( $\approx 13.89$  m/s) due to urban scenario analyses
- 34 • *Traffic conditions*: Varying traffic flows between 100 and 1500 veh/hour, in scenario 1  
 35 up to 2160 veh/hour
- 36 • *Sensors*: Vehicles are equipped with Bluetooth and/or V2X at random
- 37 • *Data fusion*: Simulation is run 100 times
- 38 • *Speed estimator*: Maximum-a-posteriori estimator (MAP) is applied on equation (5) to  
 39 estimate speed as  $\hat{v} = \arg \max P(v|v_{BT}, v_{V2X}, v_{pre}, tlc)$
- 40 • *Evaluation measures*: Accuracy determined by root mean square error (RMSE) and mean  
 41 absolute error (MAE); completeness determined by percentage.

42 Three scenarios have been chosen such that basic characteristics of the BN could be determined  
 43 while realistic applications were also tested:

1 *Scenario 1* It contains a straight, one-directional road (not shown here) equipped with V2X and  
2 Bluetooth detectors. It serves as a basic example to examine the fusion results according to equa-  
3 tion (5) depending on the true speed and traffic flow yet free from influencing factors such as  
4 intersection geometry or TLC phase. Since there is no intersection the TLC node in the BN in  
5 figure 3 was dropped.

6 *Scenario 2* A simple intersection with TLC is considered. Again, roads that meet at 90 degree  
7 angles and constant traffic flows are used for simplicity. The intersection is shown on the left of  
8 figure 4. The traffic is controlled by a TLC with a fixed-time control with 72 s cycle time. The  
9 green phases on the North-South axis lasts for 12 s, on East-West axis for 40 s. It is followed by a  
10 3 s amber phase and a 7 s red phase. This scenario combines a high traffic volume of approximately  
11 1000 veh/hour (600 vehicles going straight and 200 each turning left/right) East-West and West-  
12 East and a lower traffic volume of approximately 300 veh/hour from North-South and South-North  
13 heading equally distributed to all three directions. The volumes are chosen such that usually no  
14 traffic tailback remains after a green phase.

15 *Scenario 3* This “realistic” scenario is a replication of a real intersection in the town Brunswick,  
16 Germany, sharing its geometry and traffic demand from real traffic counts compiled in August  
17 2014. It is more complex than the previous one and enables an evaluation of the BN for speed  
18 estimation further away from academics. The right hand side of figure 4 shows the intersection’s  
19 model in SUMO. In the simulation altogether 364 vehicles are simulated in the Northern arm,  
20 586 in the Eastern, 645 in the Southern and 472 in the Western arm. In contrast to the previous  
21 scenario 2 a constant traffic flow cannot be assumed. The vehicles are inserted into the simulation  
22 at their actual occurrence. The traffic lights again follow a fixed-time control containing a 33 s  
23 green, 9 s of left-turn and 3 s of amber phase.



**FIGURE 4** SUMO view on academic scenario 2 (left) and realistic scenario 3 (right)

#### 24 **Process chain**

25 The simulation of each scenario contains three steps relevant for speed estimation by fusing data  
26 of V2X and Bluetooth. The first prepares the fusion framework, the second realizes data fusion  
27 and the the third evaluates the results.

1 *1. Training* During the training, the simulation is run 500 times to collect data on the vehicles in  
 2 the scenarios. The data recorded are then used for BN parameter learning, i.e. for quantification of  
 3 the sensor likelihoods and the a-priori probability distributions. Here, simple event counting on the  
 4 basis of Dirichlet density functions can be applied as described by Neapolitan (17). The real-time  
 5 traffic control interface TraCI (24) is adopted to enable detector placement and real-time tracking  
 6 of vehicles and detector data during simulation.

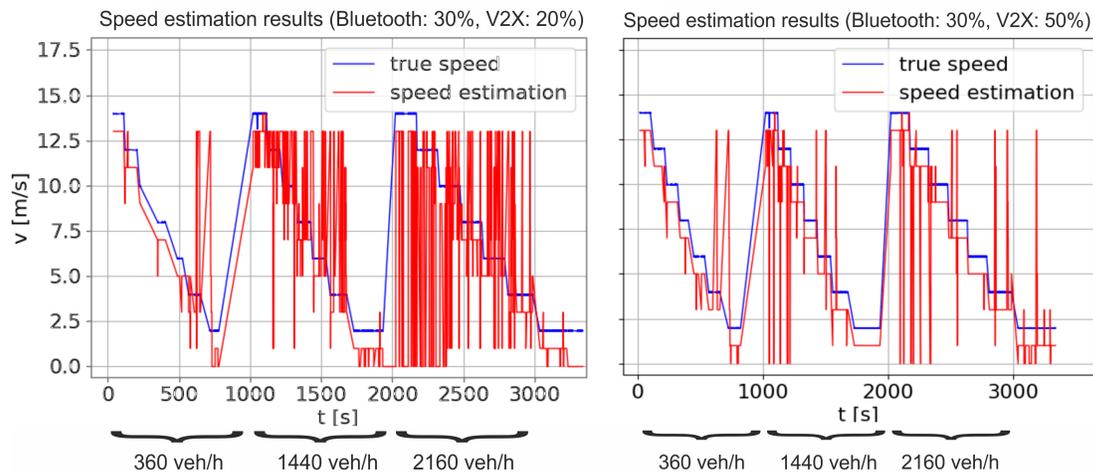
7 *2. Data fusion* Similar to the training step the simulation is executed while a speed estimation  
 8 is computed for each simulation step by computing equation (5) and evaluating it by MAP. To  
 9 analyze the performance of the BN in question the data fusion step is run 100 times.

10 *3. Evaluation* An evaluation framework is available to assess the logged true physical and esti-  
 11 mated speed data as well as Bluetooth and V2X speed and TLC state information.

## 12 Results

13 The overall quality of estimation is characterized by accuracy and completeness of the data. The  
 14 influence of the V2X and Bluetooth detection ratios on the speed estimation are of special interest.

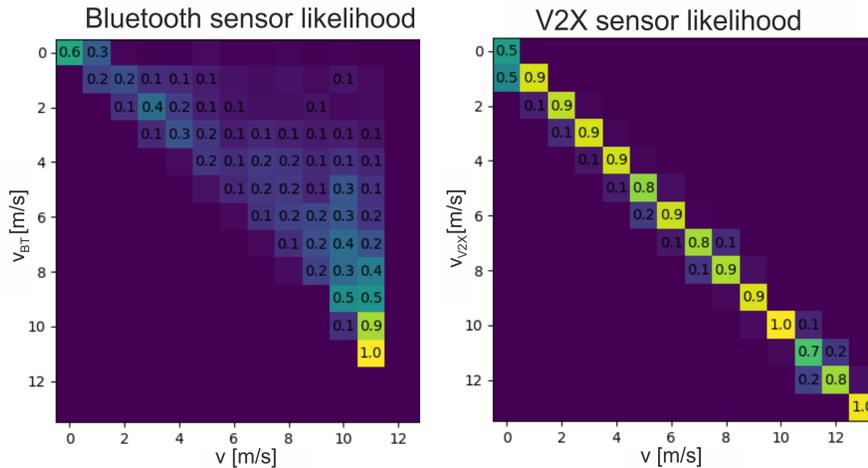
15 *Scenario 1* The first scenario's main purpose was to analyze the estimation for different combi-  
 16 nations of speed and traffic volume. The speed decreases stepwise from 14 m/s to 2 m/s while the  
 17 traffic flow changes between 360, 1440 and 2160 veh/hour. The estimation works better for lower  
 18 traffic volumes; an example is shown in figure 5. In general an overestimation of speed is obvious.  
 19 When increasing the V2X penetration ratios from 20% to 50% the estimation results improve. In  
 20 the first row of table 1 MAE, RMSE and their standard deviations as well as completeness are  
 21 depicted for V2X penetration ratios of 0, 1, 5, 10, 20, 50 and 100%.



**FIGURE 5** Example for the comparison of estimated and real speeds for a Bluetooth penetration ratio of 30% and a V2X penetration ratio of 20% (left) and 50% (right) respectively.

1 *Scenario 2* To elaborate further on the importance of the V2X penetration ratio, experiments with  
 2 differing penetration ratios were conducted. The results (MAE, RMSE, their standard deviations  
 3 and completeness) are shown in the middle row of table 1. Both quality measures, accuracy and  
 4 completeness, increase as the V2X penetration ratio increases. A V2X penetration ratio of only  
 5 20% is needed to obtain a completeness value of more than 80%. The accuracy is nearly constant  
 6 for penetration ratios between 0 and 10% with an MAE of approximately 1.71-1.72 m/s and an  
 7 RMSE of approximately 2.68-2.72 m/s, but higher than in case of lower or even higher V2X  
 8 penetration ratios. In case of V2X penetration ratios of more than 20% MAE and RMSE decrease  
 9 to 1.26 m/s and 2.1 m/s respectively.

10 Interesting findings regarding the sensor likelihoods of Bluetooth and V2X can be obtained.  
 11 The Bluetooth sensor likelihood depicted on the left in figure 6 shows the expected behavior at  
 12 TLC phase *green2* due to the measuring principle: While the likelihoods for lower speeds tend to  
 13 be close to the actual speed the results get worse as the true speed increases. For this Bluetooth  
 14 sensor a mean speed greater than 11 m/s cannot be measured.



**FIGURE 6** Sensor likelihoods for Bluetooth and V2X at traffic light green phase *green2*.

15 The sensor likelihood for V2X as shown in figure 6 right has its maximum at the true speed  
 16 class for each speed detection class. Our expectation that V2X provides more accurate speed  
 17 detections than Bluetooth can be confirmed.

18 *Scenario 3* The speed estimation results are depicted in the third row of table 1. For low V2X  
 19 penetration ratios the “academic” scenario (scenario 2) performs better than the “realistic” one  
 20 (scenario 3). But once a 20% V2X penetration ratio is reached, results are even better than in the  
 21 previous scenario. For instance, a MAE of 1.20 m/s (RMSE: 2.06 m/s) is reached at 50% and  
 22 0.98 m/s (RMSE: 1.63 m/s) at 100% V2X penetration ratios.

23 The influence of the Bluetooth penetration ratio was examined at a constant V2X pene-  
 24 tration ratio of 10%. Ratios of 0, 30, 50 and 100% were used for Bluetooth equipment. Results  
 25 are shown in table 2 where completeness increases quickly when the penetration ratios are raised.  
 26 Without Bluetooth data only 40.0% completeness can be reached, whereas at 30% Bluetooth pen-  
 27 etration already 74.6% completeness can be obtained. In contrast, the accuracy decreases with

	V2X penetration ratio [%]	MAE [m/s]	$\sigma_{MAE}$	RMSE [m/s]	$\sigma_{RMSE}$	completeness [%]
Scenario 1	0 (Bluetooth only)	5.27	0.51	6.65	0.55	48.8
	1	4.94	0.50	6.38	0.56	50.6
	5	4.10	0.50	5.67	0.64	56.0
	10	3.35	0.42	4.96	0.59	61.5
	20	2.37	0.25	3.87	0.43	72.2
	50	1.28	0.08	2.02	0.24	89.7
	100	0.98	0.00	0.98	0.01	99.7
Scenario 2	0 (Bluetooth only)	1.71	0.64	2.68	0.56	63.1
	1	1.71	0.63	2.68	0.56	64.3
	5	1.72	0.60	2.71	0.56	68.6
	10	1.72	0.57	2.72	0.55	73.5
	20	1.68	0.52	2.68	0.53	81.1
	50	1.50	0.40	2.44	0.45	93.1
	100	1.26	0.26	2.10	0.25	99.6
Scenario 3	0 (Bluetooth only)	2.37	0.23	3.69	0.45	64.3
	1	2.30	0.21	3.62	0.43	65.7
	5	2.07	0.15	3.36	0.33	70.2
	10	1.86	0.16	3.08	0.28	74.6
	20	1.59	0.13	2.71	0.20	81.6
	50	1.20	0.09	2.06	0.12	92.8
	100	0.98	0.06	1.63	0.07	99.8

**TABLE 1 Evaluation results of scenario 3 with fixed Bluetooth penetration ratio of 30%**

- 1 increasing Bluetooth ratio, which is in line with our expectations. The Bluetooth equipment serves
- 2 the role to improve completeness, but increases the speed estimation error compared to V2X data.

Bluetooth penetration ratio [%]	MAE [m/s]	$\sigma_{MAE}$	RMSE [m/s]	$\sigma_{RMSE}$	completeness [%]
0 (V2X only)	1.32	0.11	2.22	0.18	40.0
30	1.86	0.16	3.08	0.28	74.6
50	1.94	0.15	3.17	0.24	84.6
100	2.05	0.14	3.29	0.20	94.8

**TABLE 2 Evaluation results of scenario 3 with fixed V2X penetration ratio of 10%**

- 3 It further appeared that similar to the findings in (13) the results differ greatly depending on
- 4 the intersection arms, which is shown in table 3. Very likely we can assume that the different traffic
- 5 volumes  $Q \in [364, 645]$  veh/hour in connection with the driven mean speeds cause this behavior.
- 6 Thus, for low V2X penetration ratios we can expect MAEs of up to approximately 2.1 m/s, 2.5 m/s,
- 7 2.6 m/s and 2.3 m/s for the Eastern, Southern, Western and Northern arms, respectively. In case of
- 8 the Northern and Eastern arms the MAEs are significantly lower than in the Southern and Western
- 9 arms. In case of fully V2X equipped vehicles we obtain MAEs between 0.88-1.04 m/s on all
- 10 intersection arms.

V2X penetration ratio [%]	MAE [m/s]			
	North	East	South	West
0 (Bluetooth only)	2.32	2.05	2.46	2.64
1	2.28	2.01	2.38	2.53
5	2.02	1.89	2.09	2.29
10	1.80	1.73	1.79	2.09
20	1.54	1.55	1.49	1.76
50	1.18	1.24	1.08	1.30
100	0.98	1.02	0.88	1.04

**TABLE 3 MAE under consideration of the intersection arms and the V2X penetration ratio. The Bluetooth penetration ratio is 30%**

1 Comparing the obtained results to previous research (13) (see table 4) the mean RMSE  
 2 over all intersection arms can be used. For low V2X penetration the results in scenario 2 show the  
 3 lowest errors and the RMSE values in scenario 3 are slightly worse than those obtained in (13).  
 4 At a V2X penetration ratio of 20% the RMSEs for all scenarios are similar. For V2X penetration  
 5 ratios higher than 20% the errors in scenario 3 are the lowest.

V2X penetration ratio [%]	Scenario 2	Scenario 3	Junghans and Leich (13)
1	2.68	3.62	3.50
5	2.71	3.36	3.25
10	2.72	3.08	3.08
20	2.68	2.71	2.78
50	2.44	2.06	2.38
100	2.10	1.63	1.90

**TABLE 4 RMSE [m/s] of the scenarios 2 and 3 in comparison with results obtained in (13). The Bluetooth penetration ratio is 30%**

## 6 CONCLUSION & FUTURE PROSPECTS

7 In this paper a recently published method for fusing rare, but accurate V2X data with frequently  
 8 used, but rather inaccurate one unit Bluetooth reader data of vehicle speeds was analyzed and  
 9 improved. This analysis included the investigation of (i) specific traffic related variables, such as  
 10 traffic flow and traffic density and (ii) the consideration of the traffic light control (TLC) influencing  
 11 the Bluetooth based speed detection. Hence, an improved Bayesian Network (BN) was developed  
 12 with regard to its applicability for speed estimation in three different traffic scenarios ranging from  
 13 “academic” trials (i.e. artificial traffic areas and traffic data) to “realistic” (i.e. real intersection  
 14 model and real traffic demand).

15 The microscopic traffic simulation SUMO was used. It appeared that the BN had to be  
 16 modified twofold, to be reduced by some redundant variable and to be extended by an additional  
 17 variable modeling the TLC behavior. The newly added TLC node was taking into account free  
 18 flow and stop-and-go characteristics of the vehicles passing the intersections. Further, it turned out  
 19 that the green phase had to be separated into two different states modeling vehicles that cross the  
 20 intersection in free flow and vehicles that accelerate due to phase switches.

1           The results obtained show that the newly developed BN improved the speed estimation re-  
2 sults in case of 1-20% V2X penetration ratios in academic example scenario 2 taking into account  
3 a fixed Bluetooth penetration of 30%. However, it is not clear, why the accuracy decreases in case  
4 of moderate V2X penetration ratios between 5-20% in scenario 2. Additionally, the application  
5 of the proposed BN in the realistic example improved the speed estimation results in case of V2X  
6 penetration ratios greater than 20%. Particularly, the inclusion of a TLC node greatly improved  
7 the estimation results. Even this rather idealistic approach shows that we can expect a cost ef-  
8 ficient application for traffic light control in cases of moderate V2X penetration ratios. Further,  
9 the application of this method emphasizes the suitability of Bayesian Networks for data fusion  
10 purposes, especially in case of communication based sensor technologies in traffic and transporta-  
11 tion. However, it is still unclear, whether low price solutions, such as one unit Bluetooth readers  
12 in combination with accurate V2X sensors, can substitute current sensor technologies, particularly  
13 invasive technologies like inductive loop detectors for adaptive traffic traffic light control. But  
14 we are on the way to find out what the limits of these technologies are. Currently, we are quite  
15 sure that the V2X penetration ratio has to reach approximately 20% to achieve satisfactory speed  
16 estimations, which we expect the car manufacturers to take some years.

17           Our future work will deal with the problem of decrease in accuracy for moderate V2X  
18 penetration ratios. Further, since the investigations were made under idealistic assumptions, we  
19 will consider the method under more realistic conditions, e.g. changing detection ranges depending  
20 on the weather conditions, different antenna designs and propagation characteristics. Further, this  
21 proposed methods can be improved by using two Bluetooth detectors instead of one only. Tests on  
22 a real intersection are also part of our future work.

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## 26 **AUTHOR CONTRIBUTION STATEMENT**

27 The authors confirm contribution to the paper as follows: study conception and design: M. Jung-  
28 hans, K. Klüber; data collection: K. Klüber; analysis and interpretation of results: K. Fackeldey,  
29 M. Junghans, R. Kaul, K. Klüber; draft manuscript preparation: M. Junghans, K. Klüber.

30           All authors reviewed the results and approved the final version of the manuscript.

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# Improved Traffic State Estimation by Bayesian Network Data Fusion of V2X and Vehicular Bluetooth Data

Kim Klüber, Marek Junghans, Konstantin Fackeldey, Robert Kaul

## Motivation

### Objectives

- Cleaner, safer and more efficient traffic
- Intelligent V2X based traffic light control (iTLC): Quantify, what is currently possible using V2X!

### What traffic data quality level can be obtained in case of V2X based traffic detection?

- Sparsity of the data due to extremely low V2X penetration ratios (1 – 3%) within the next years
- Combine data with other wireless technologies, e.g. vehicular WiFi / Bluetooth ( $\approx 3 - 50\%$ )
- Analyze and improve the existing method

## Bayesian Networks (BN)

- BN are a graphical representation of cause-effect relationships quantified by conditional probability density functions
- Satisfy the structural Markov property
- Allow to handle and quantify uncertainty
- Allow to take into account hard and soft evidences at each node to infer the true, and usually unknown realization of stochastic variable
- Common usage of BN:
  - Modelling cause-effect relationships
  - Monitoring and diagnosing: drawing conclusions from observations on their causes

## Initial BN analysis

- The initial BN and particularly node  $V_{BT}$  was analyzed with regard to:
  1. Traffic flow ( $Q$ ) and density ( $D$ )
  2. Traffic light control (TLC)
  3. Preceding Bluetooth speed ( $V_{pre}$ )
  4. Speed difference ( $\Delta V$ )

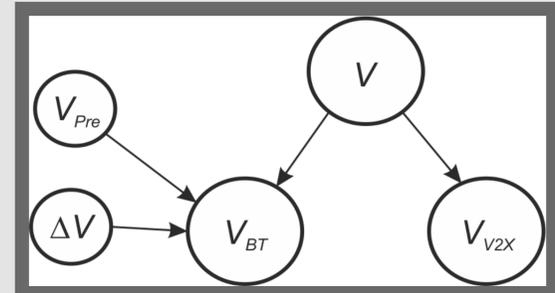


Figure 2: Initial Bayesian Network for fusing V2X and Bluetooth based vehicular speed estimates. (Junghans & Leich)

## Simulation of Urban Mobility (SUMO)

- [sumo.dlr.de](http://sumo.dlr.de)
- Open source package
- Microscopic traffic simulation also allowing mesoscopic analyses
- Main applications:
  - traffic and transportation management (intermodal, multimodal)
  - car following
  - vehicle communication (V2X)
  - (analysis of safety-related traffic situations)

### Resulting fusion equation

$$P(v|v_{BT}, v_{V2X}, \Delta v, v_{pre}) = \alpha \cdot P(v|tlc) \cdot P(v_{pre}) \cdot P(v_{BT}|v, v_{pre}) \cdot P(v_{V2X}|v)$$

- $TLC$  – traffic light control
- $V$  – true physical speed of the vehicle
- $V_{BT}$  – Bluetooth-based speed estimate
- $V_{V2X}$  – V2X based speed estimate
- $V_{pre}$  – speed estimate of the preceding Bluetooth equipped vehicle

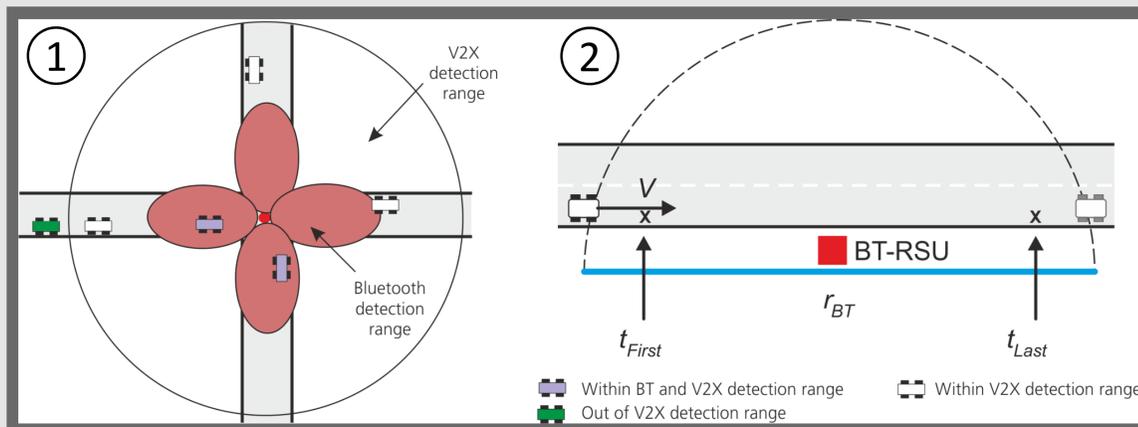


Figure 1: Bluetooth and V2X based detection ranges (1.1) and principle of speed estimation with a single unit Bluetooth reader (1.2).

## Method

- Single unit Bluetooth speed estimation:
 
$$V_{BT} \approx \frac{r_{BT}}{t_{Last} - t_{First}}$$
- V2X based speed estimation  $V_{V2X}$
- Fusing the speed estimates by Bayesian Network (BN) taking into account
  - $V_{pre}$ : speed of the preceding Bluetooth equipped vehicle
  - $\Delta V$ : speed difference of the currently detected and the preceding Bluetooth equipped vehicle

### Conclusions

- $V_{BT}$  is strongly speed-dependent
- Speed dependence should be modeled

### Results

- Marginal effect of traffic flow and density on node  $V_{BT}$
- TLC node should be added to model the required speed dependence of the Bluetooth-based speed estimator
- Node  $\Delta V$  contains information of node  $V_{pre}$  and is redundant

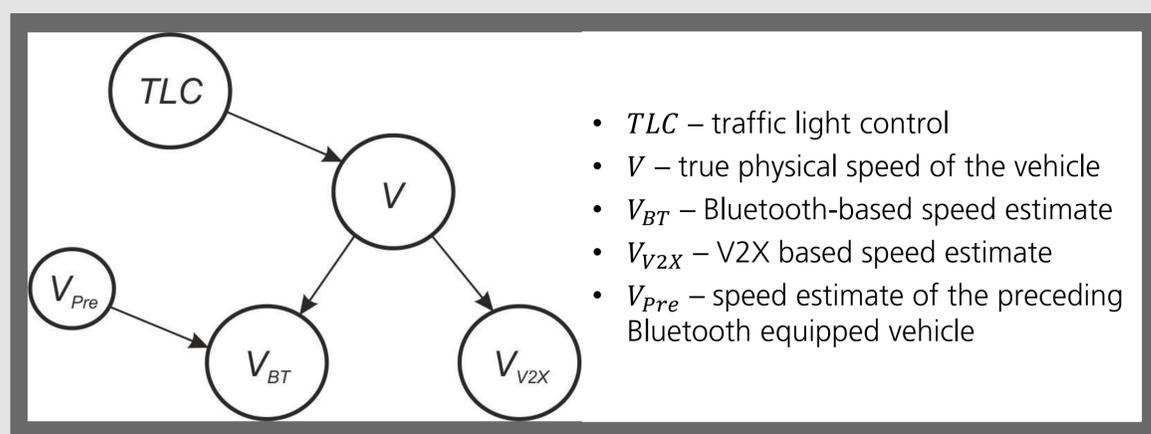


Figure 3: Final Bayesian Network to fuse vehicular single unit Bluetooth-based speed estimates with V2X speed estimates. Note that the node  $TLC$  complements the initial BN.

# Improved Traffic State Estimation by Bayesian Network Data Fusion of V2X and Vehicular Bluetooth Data

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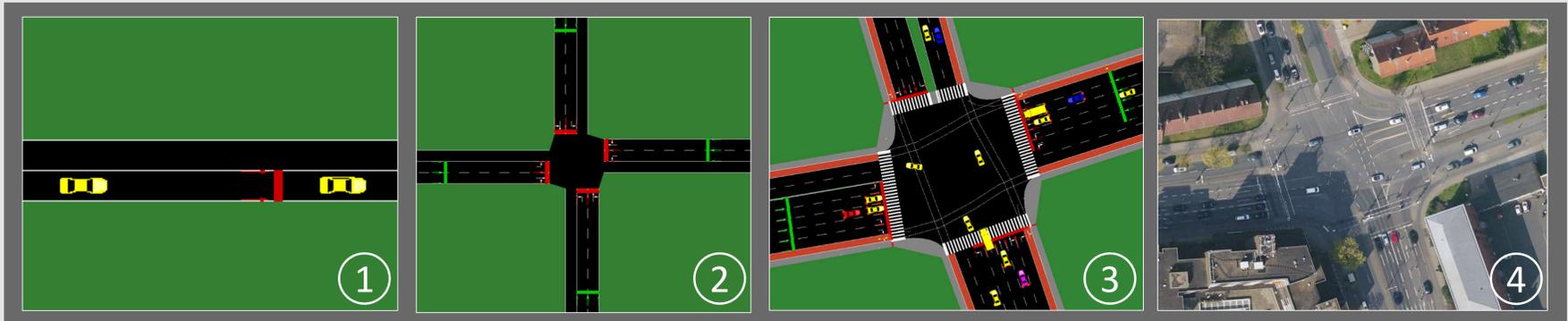


Figure 4: SUMO view on the scenarios 1, 2 and 3: Analysis on (4.1) an intersection free straight road, (4.2) academic intersection with fixed TLC and different traffic volumes, (4.3) real world intersection (Brunswick, Germany) with real traffic demand and fixed TLC and (4.4) aerial photograph of this real intersection.

## Experimental results

### Setup

- Microscopic traffic simulator SUMO (Simulation of Urban MObility)
  - Simulation time: 3600s
  - Detection ranges:
    - Bluetooth: 30m
    - V2X: 200m
  - Penetration ratios:
    - Bluetooth: [0, 30, 50, 100]%
    - V2X: [0, 1, 5, 10, 20, 50, 100]%
  - Traffic conditions: 100 – 1500 (2160) veh/hour
  - Training runs: 500
  - Simulation runs: 100
  - Speed estimator: MAP
- Evaluation metrics:
    - MAE [m/s]
    - RMSE [m/s]
    - completeness [%]

### Three Scenarios

1. Straight road (Figure 4.1): Speed decreases from 14 m/s down to 2 m/s while increasing traffic flow from 360 to 2160 veh/hour
2. Academic intersection (Figure 4.2): Identified two “green” traffic light phases for the TLC-node in the BN
3. Real intersection (Figure 4.3): Real traffic demand data used for analysis

## General results

### Scenario 1

- Speed estimation better for lower traffic volumes

### Scenario 2

- MAE and RMSE for low V2X (0 – 10%) penetration ratios approximately 1.7 m/s and 2.7 m/s, respectively

### Scenario 3

- MAE and RMSE for low V2X (0 – 10%) penetration ratios approximately 2.2 m/s and 3.5 m/s, respectively
- Increasing the Bluetooth penetration ratio increases the traffic state estimation error

## Conclusions & Future prospects

### Conclusions

- Single unit Bluetooth speed estimation overestimates speed
- Due to Bluetooth equipped vehicles the completeness of the speed data increases, but the accuracy of traffic state estimation decreases. In contrast, an increase of V2X equipped vehicles increases the accuracy
- Only about 20% V2X penetration is needed to achieve 80% completeness
- TLC node needed to handle free flow and stop-and-go traffic
- Method gives an idea what can be expected in case of wireless, vehicular speed estimation data
- Possibly estimated 20% V2X penetration needed to realize a good TLC algorithm

### Future Prospects

- Find out the cause of the increased speed estimation error in case of moderate V2X penetration ratios
- Analyze more realistic conditions

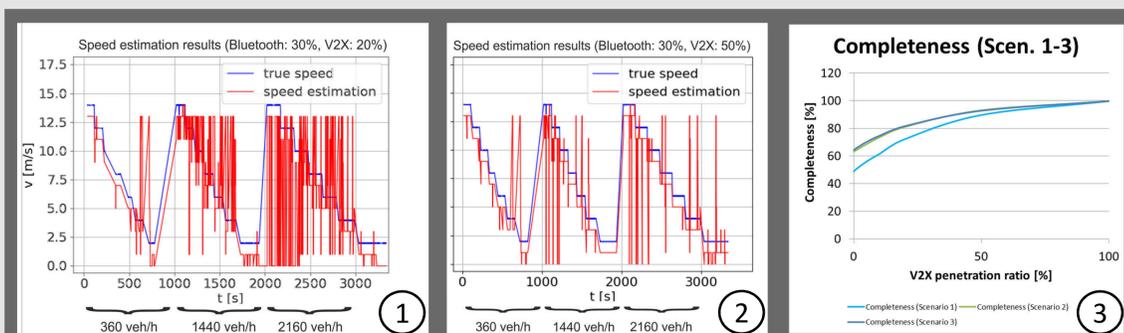


Figure 5: Comparison of estimated with real speeds in case of a Bluetooth penetration ratio of 30% and a V2X penetration ratio of 20% (5.1) and 50% (5.2); completeness value of fusing Bluetooth with V2X (5.3).

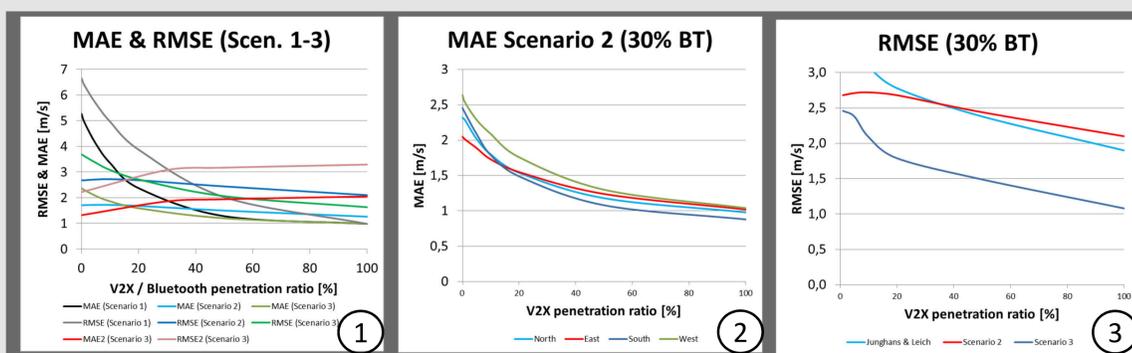


Figure 6: Evaluation results: MAE and RMSE for all scenarios (6.1), MAE for scenario 2 considering the different intersection arms (6.2) and RMSE compared for scenario 2, 3 and Junghans & Leich (6.3).

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