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## Reducing computing times in optimizing energy system models – challenges and opportunities

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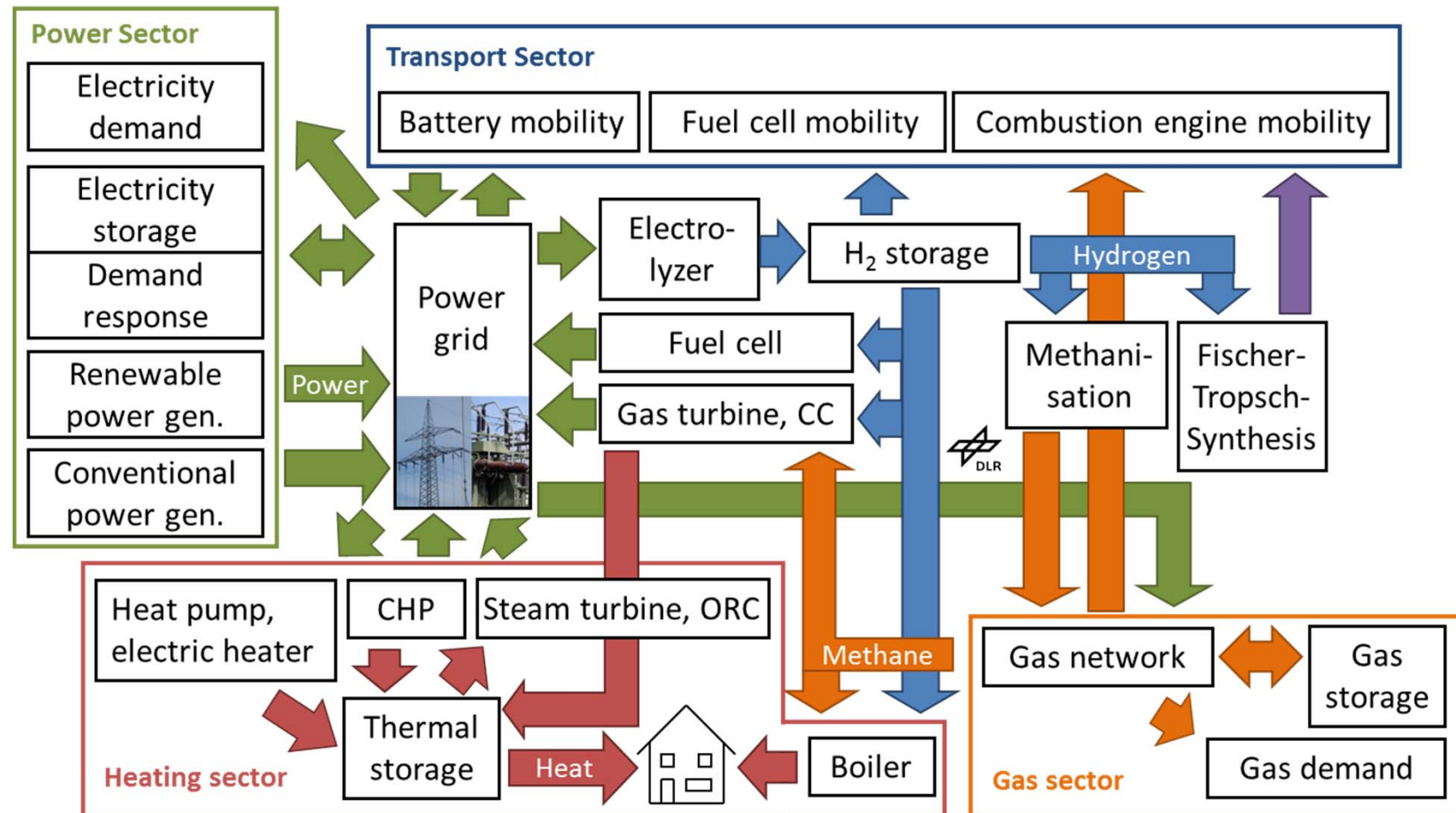


1. Introduction: challenges & motivation
2. Energy system model (ESM) REMix
3. Types of speed up methods for ESM
4. Results (speed up, quality of results)
  - a) Best practice GAMS modeling
  - b) Spatial clustering
  - c) Technological simplifications
  - d) Rolling horizon dispatch
5. Conclusion & outlook

# Challenges & motivation

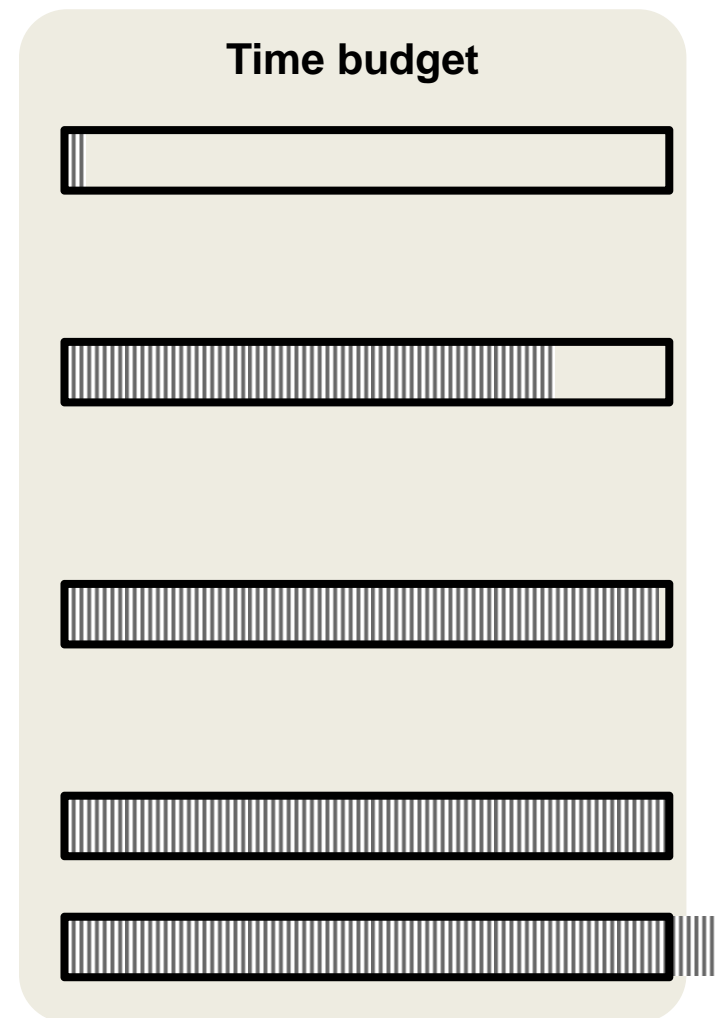
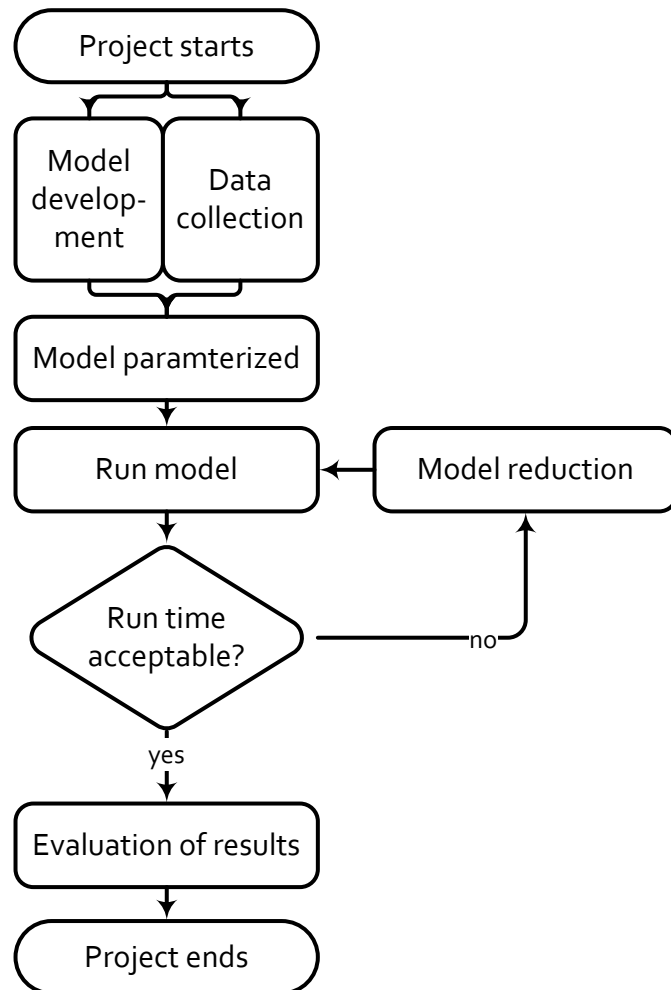
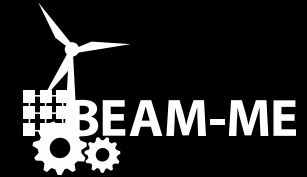
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# Challenges I: complex energy systems



Time steps (8760) x Mile stone years (7) x Regions (28) x Technologies (20)  $\approx$  35 Mio. variables

# Challenges II



How can we **decrease** calculation times while retaining a **good quality** of the results?

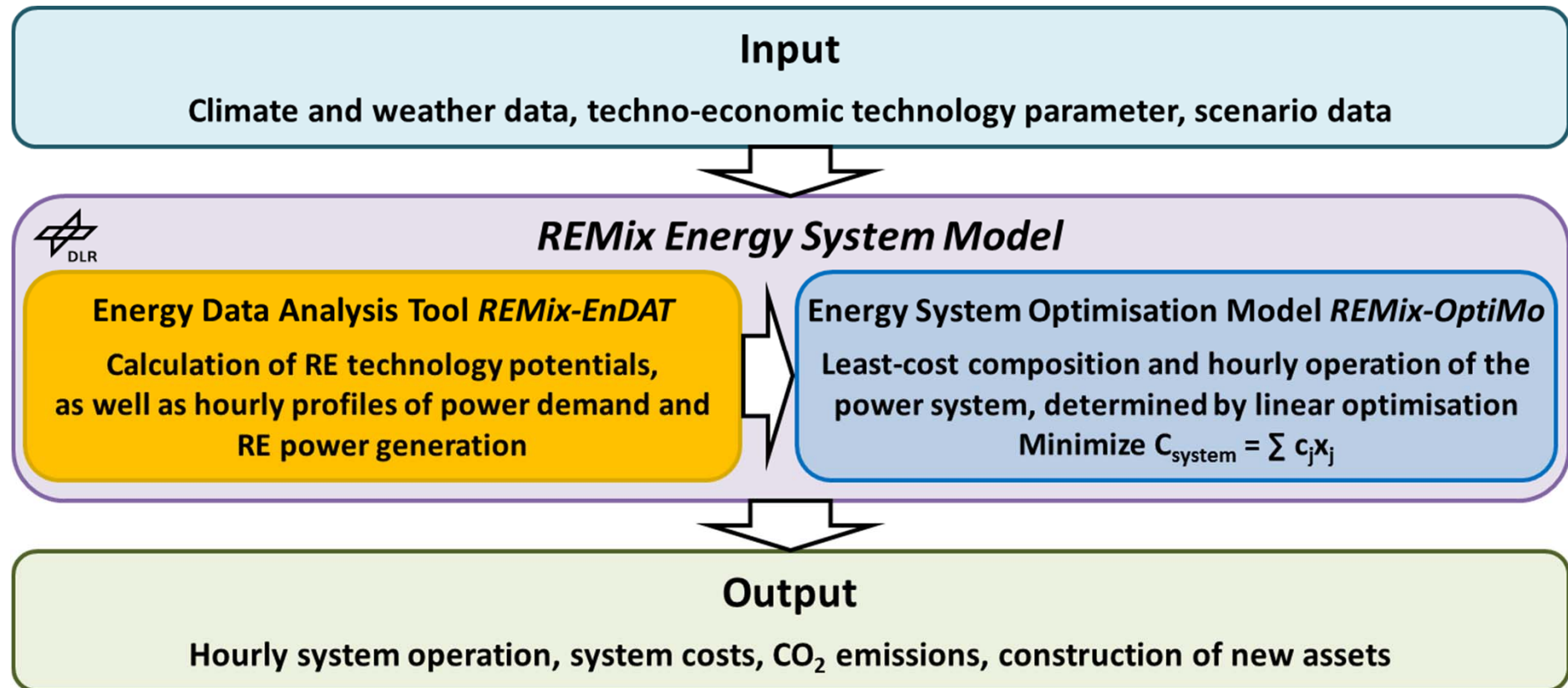
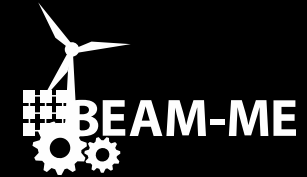
How much speed up can we achieve?

What is a good quality?

# The energy system model REMix

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# REMix\* energy system model



- Deterministic linear optimisation model realised in GAMS
- Assessment of investment and hourly system dispatch during one year

\* H. C. Gils et al., "Integrated modelling of variable renewable energy-based power supply in Europe," *Energy*, vol. 123, pp. 173–188, 2017



# Acceleration strategies for linear programs

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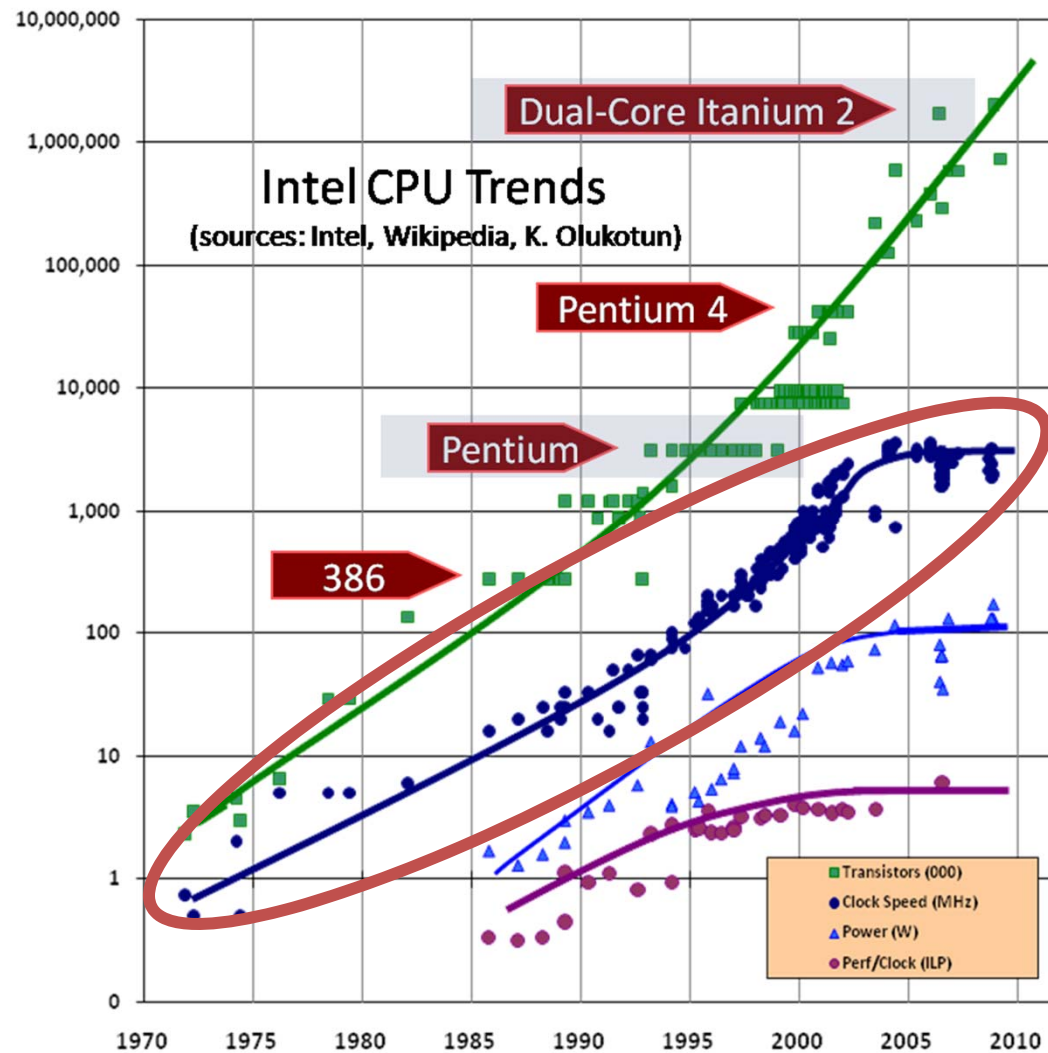
# Approach I (the probably most popular one)

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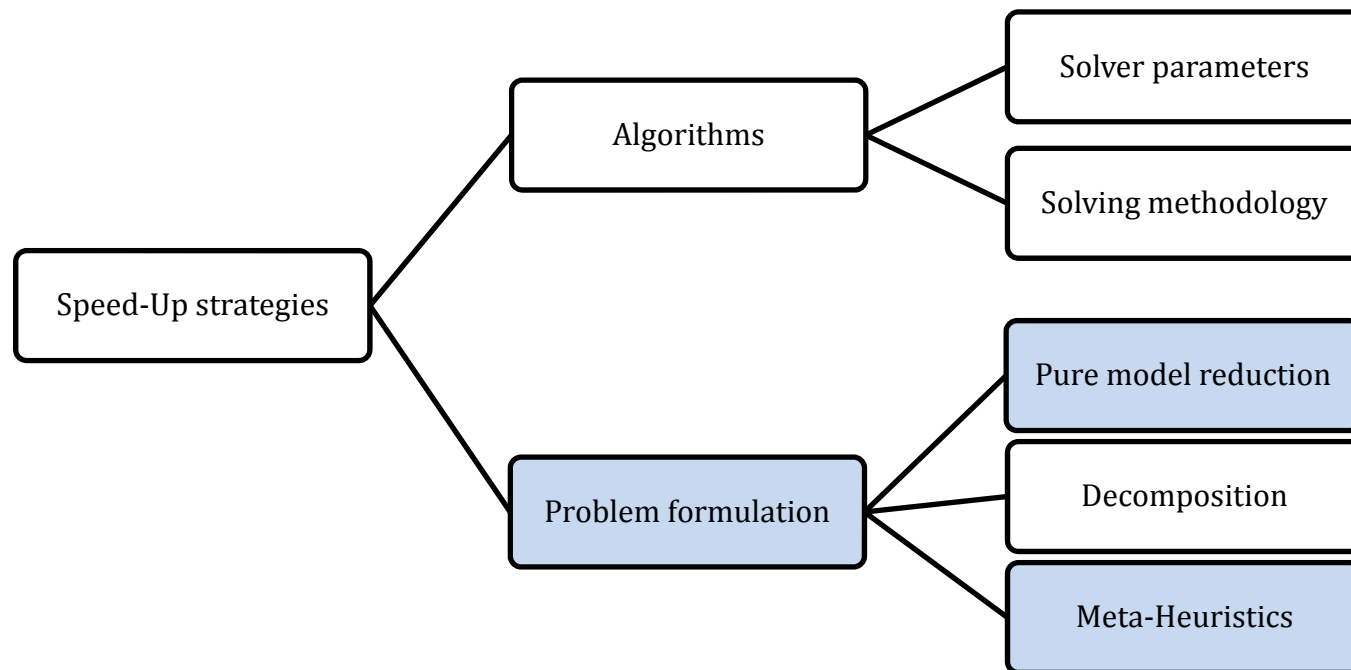
# „The free lunch is over“



Herb Sutter (2005):  
The Free Lunch Is Over. A Fundamental Turn Toward Concurrency in Software, Dr. Dobbs's Journal, 30(3), March 2005,  
<http://www.gotw.ca/publications/concurrency-ddj.htm>

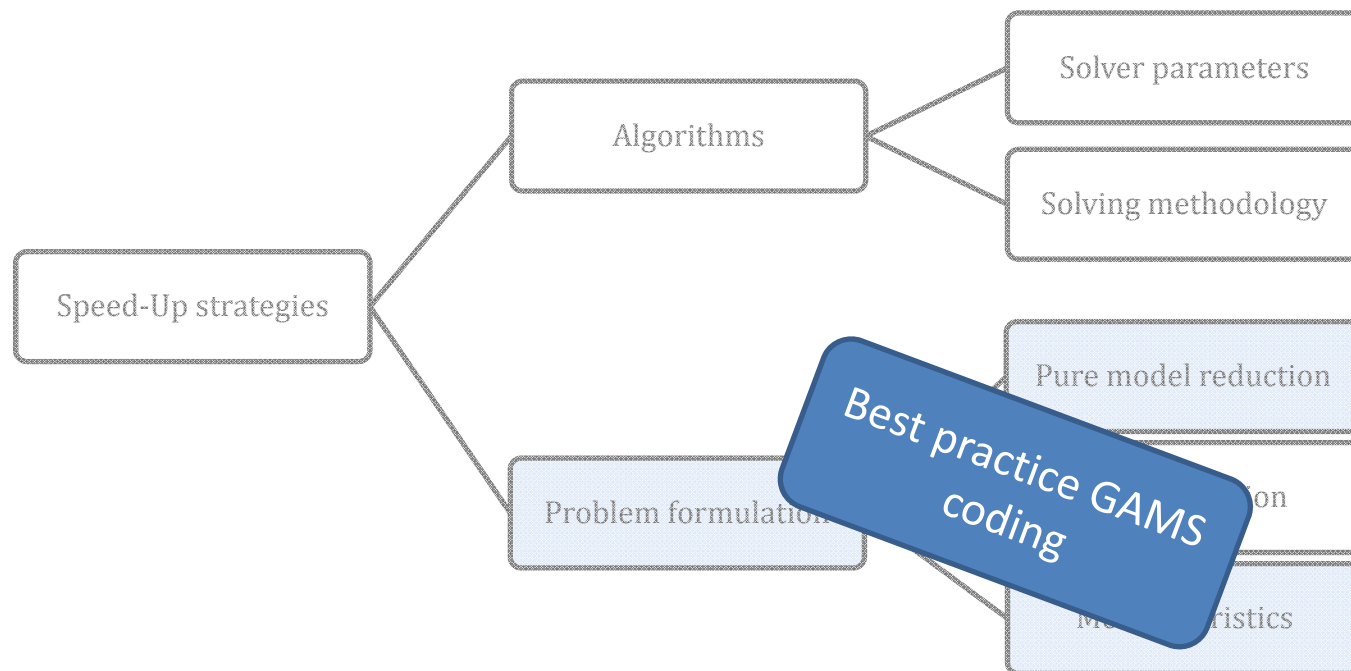
## Approach II: Software related speed-up strategies

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# „Low Hanging Fruits“

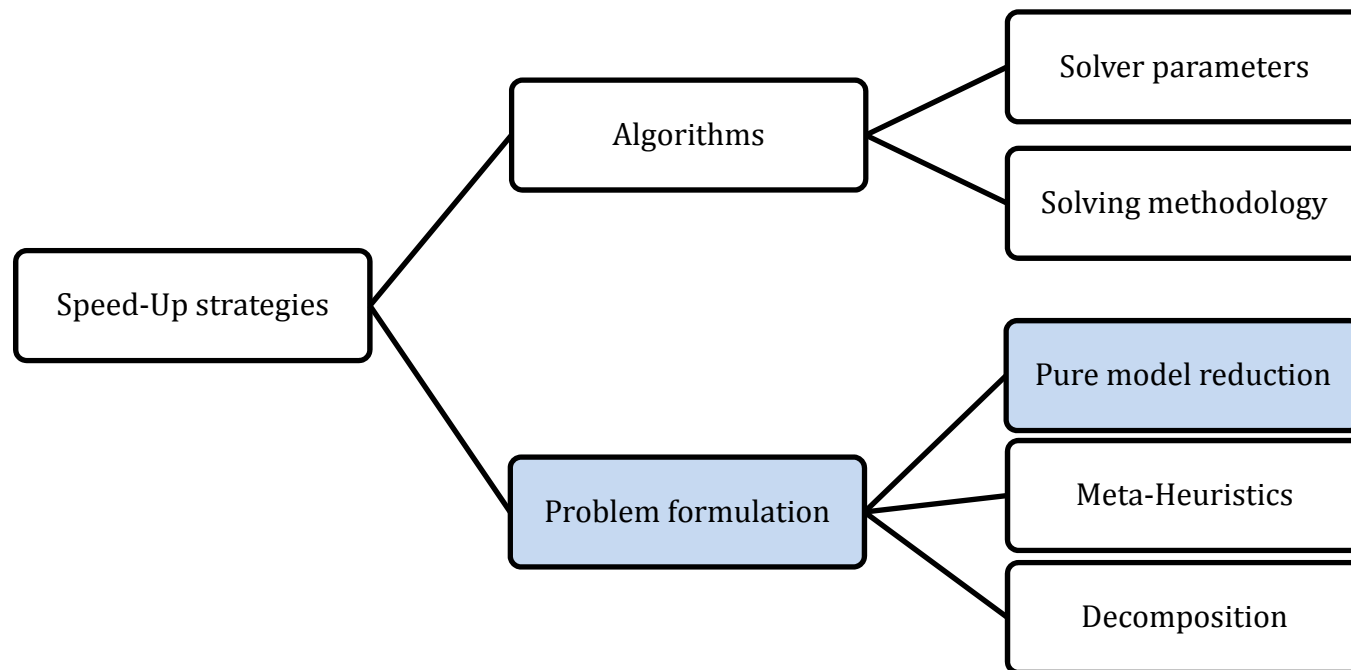
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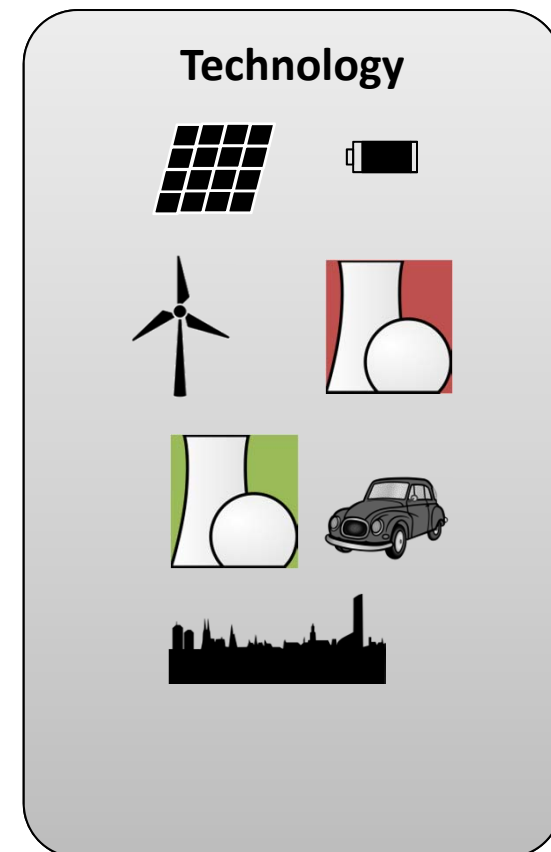
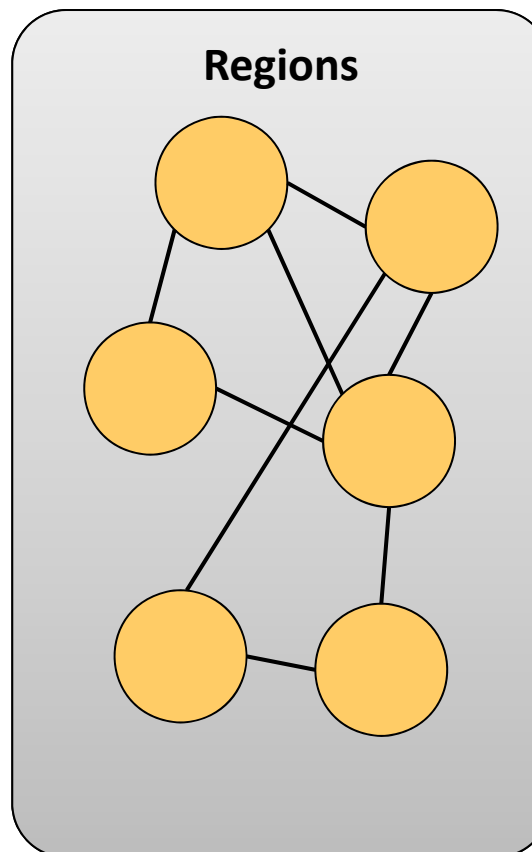
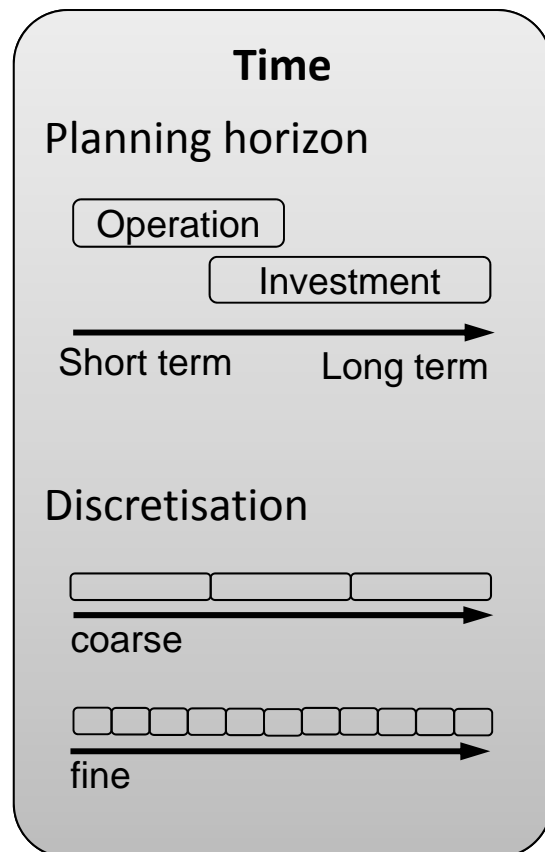
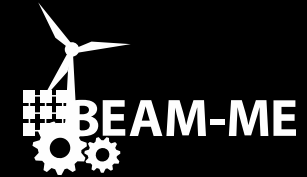
- Selection of measures (also useful for decrease memory need):
  - Input data should not differ much in its order of magnitude
  - Index order influences computing time
    - Useful, but not necessarily faster
    - Assignment statements with a different set order can be faster
    - It can be better to place large index sets at the beginning
  - Use of “option kill” , e.g. for long time-series input parameters saves memory
  - Abundant use of “Dollar Control over the Domain of Definition”
  - Consistent (and limited) use of defined variables
  - Avoidance of the consideration of technologies providing the same service at the same costs
  - Consideration of alternative formulation of model constraints (dense vs. sparse)
- Helpful references: “Speeding up GAMS Execution Time”  
by Bruce A. McCarl <https://www.gams.com/mccarl/speed.pdf>

# Conceptual strategies

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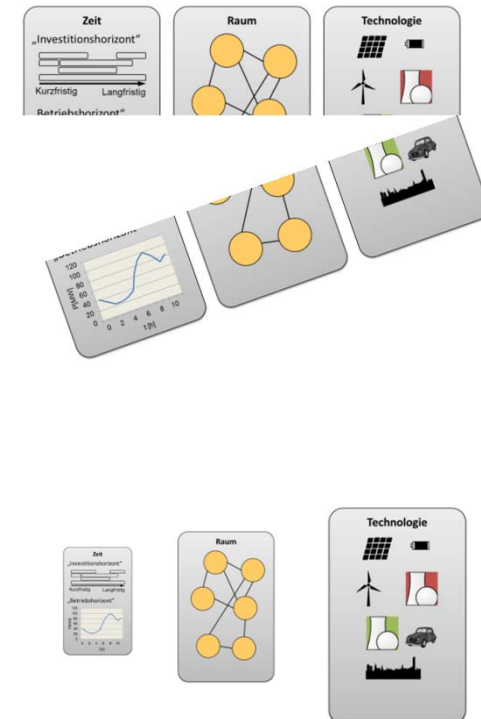
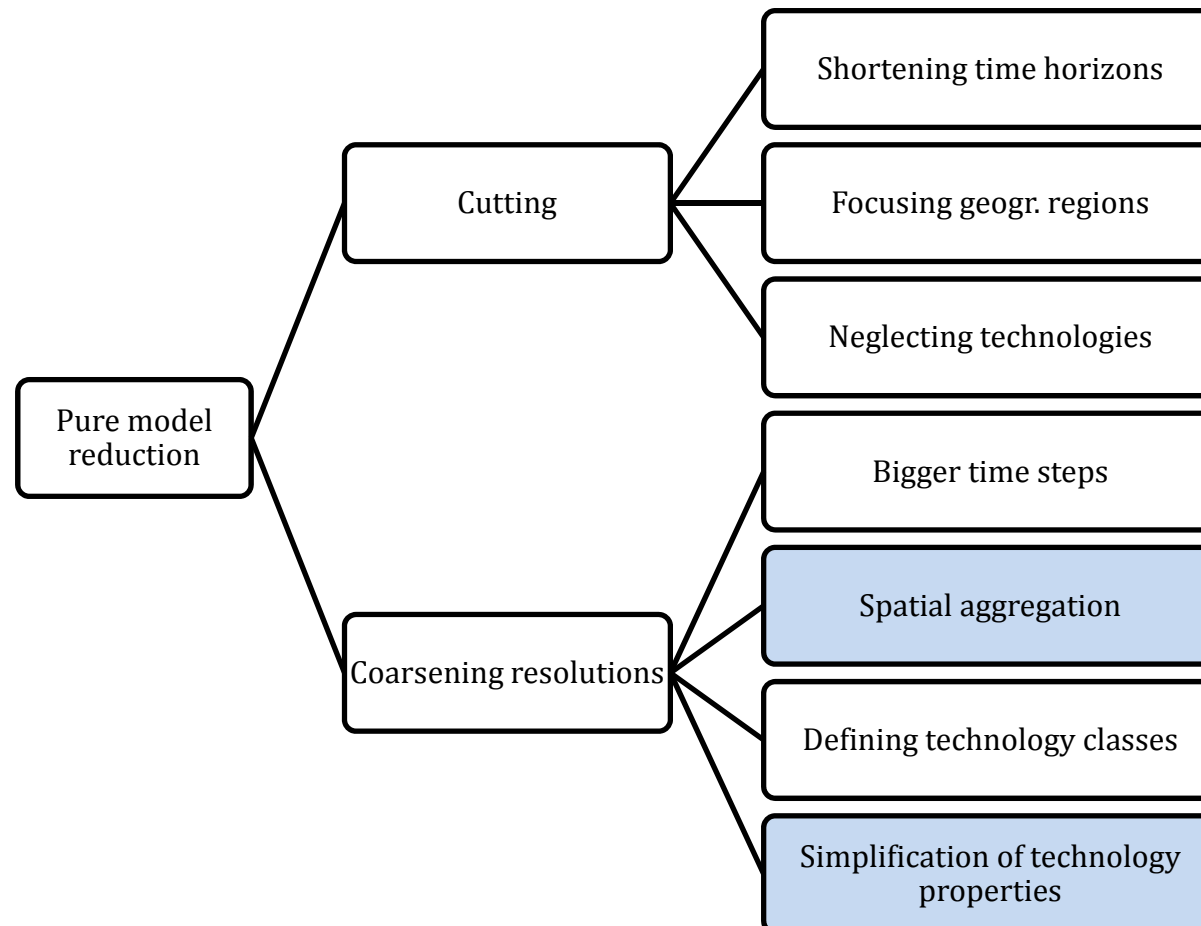


# Typical model dimensions







# Types of model reductions in ESM



## What we know...

- Everybody does it (and hopes it's sufficient)
- We often do not know the **error** (and the speed up) caused by throwing away information

Implementation cost	Speed-up capability
	

## What we already learnt...

- Changing model resolution is preferable to cutting , but harder to implement

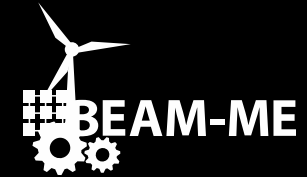
## What we estimate...

- Methods aiming at reducing the „biggest dimension“ might be the most effective ones

## What we want....

- A systematic (and representative) benchmark of the speed-capability
- Error estimation

# Spatial aggregation I



## Idea and implementation

- Reference model: 500 regions
- Aggregation of regions using spectral clustering
- Criterion: grid bottleneck between regions, i.e. small delta of marginal costs
- Comparison of system costs, power generation, grid utilisation and calculation times

6 regions



50 regions



500 regions



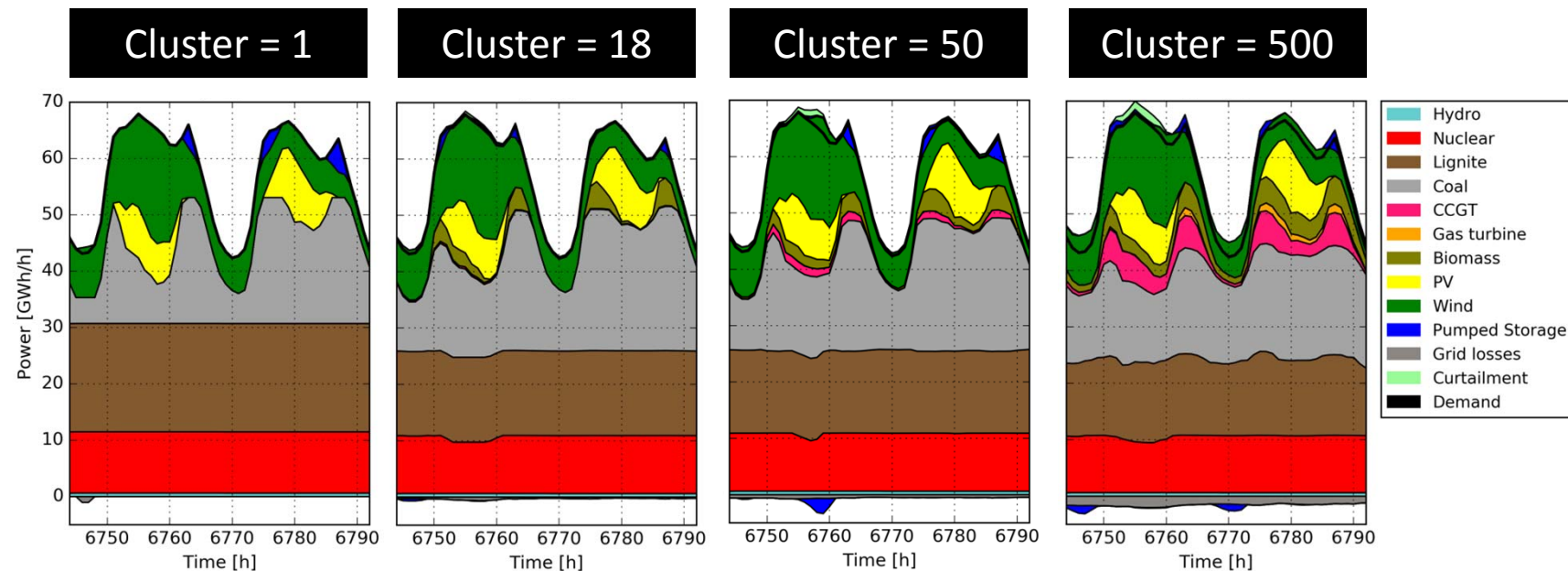
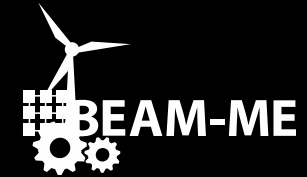
## Results

- Hypothesis: computing times increase with approx. **linearly** (further evaluation needed)
- However, significant effects on model accuracy

Number of clusters	1	6	18	30	50	75	100	500
Cplex time [s]	1	4	28	41	150	167	171	3784
System costs [M€]	751	758	839	843	854	869	926	968
Lignite power generation [TWh]	13.12	13.14	10.69	10.44	10.36	10.29	9.23	8.88
Hard coal power generation [TWh]	7.44	7.51	9.85	9.66	9.97	10.11	10.39	9.86

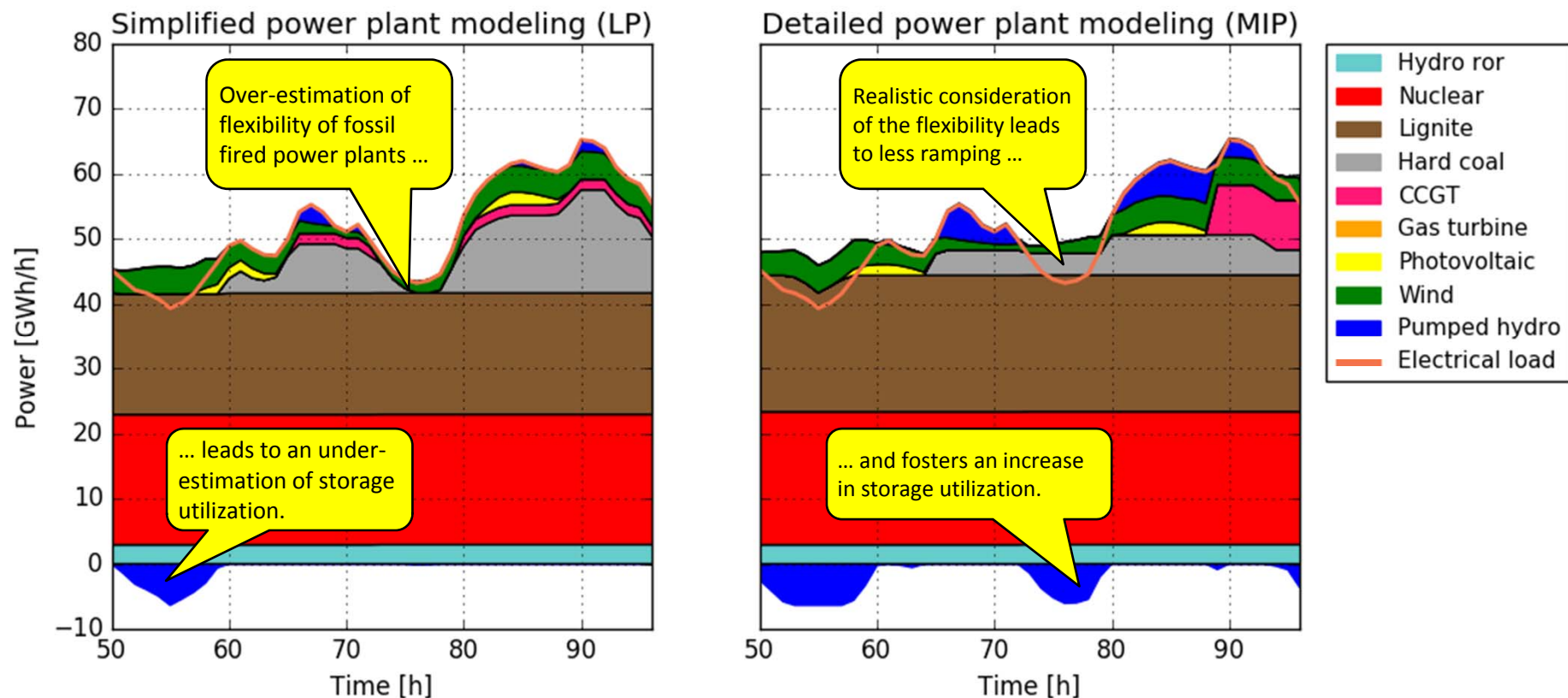
References: Metzdorf, J.: "Development and implementation of a spatial clustering approach using a transmission grid energy system model", University Stuttgart, 2016

# Spatial aggregation II



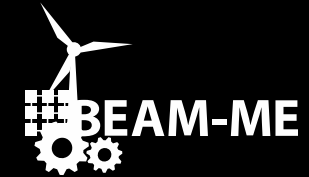
- Cluster = 1 equals large copperplate, no grid congestion, a lot of flexibility to cover the electrical load
  - Total amount of electricity in the copperplate scenario the lowest, since no grid losses of grid lines (i.e. most grid losses in 500 clusters)
- Technology ratios
  - Decreasing utilization of base load power plants (lignite, nuclear), low operational costs (fuel costs)
  - Increasing utilization of peak load plants (CCGT, GT) and storage

## Influence of power plant modeling approach\* LP versus MIP



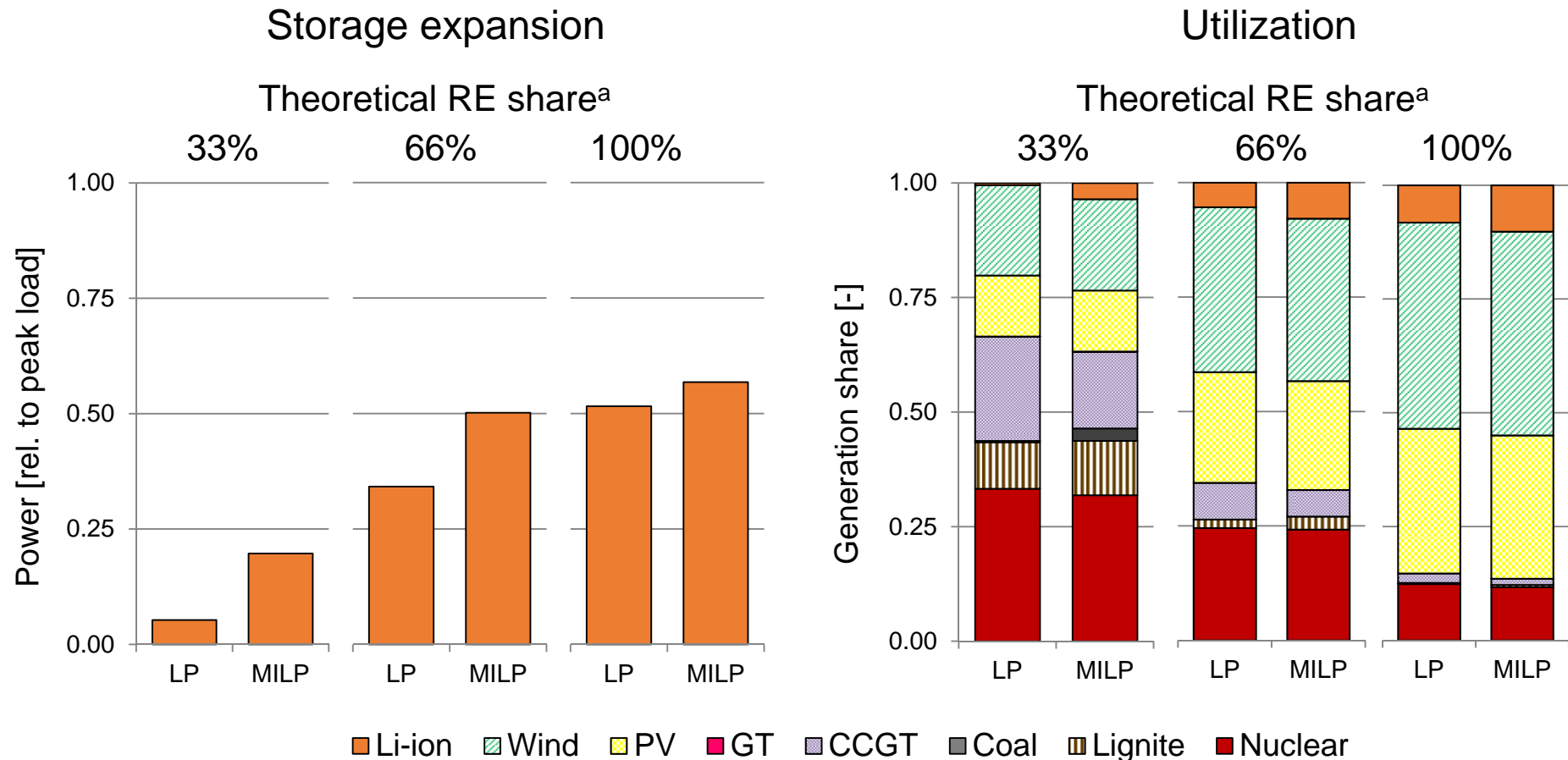
\* F. Cebulla and T. Fichter, "Merit order or unit-commitment: How does thermal power plant modeling affect storage demand in energy system models?," *Renewable Energy*, vol. 105, pp. 117–132, 2017

# Technology simplifications II



## Influence of power plant modeling approach\*

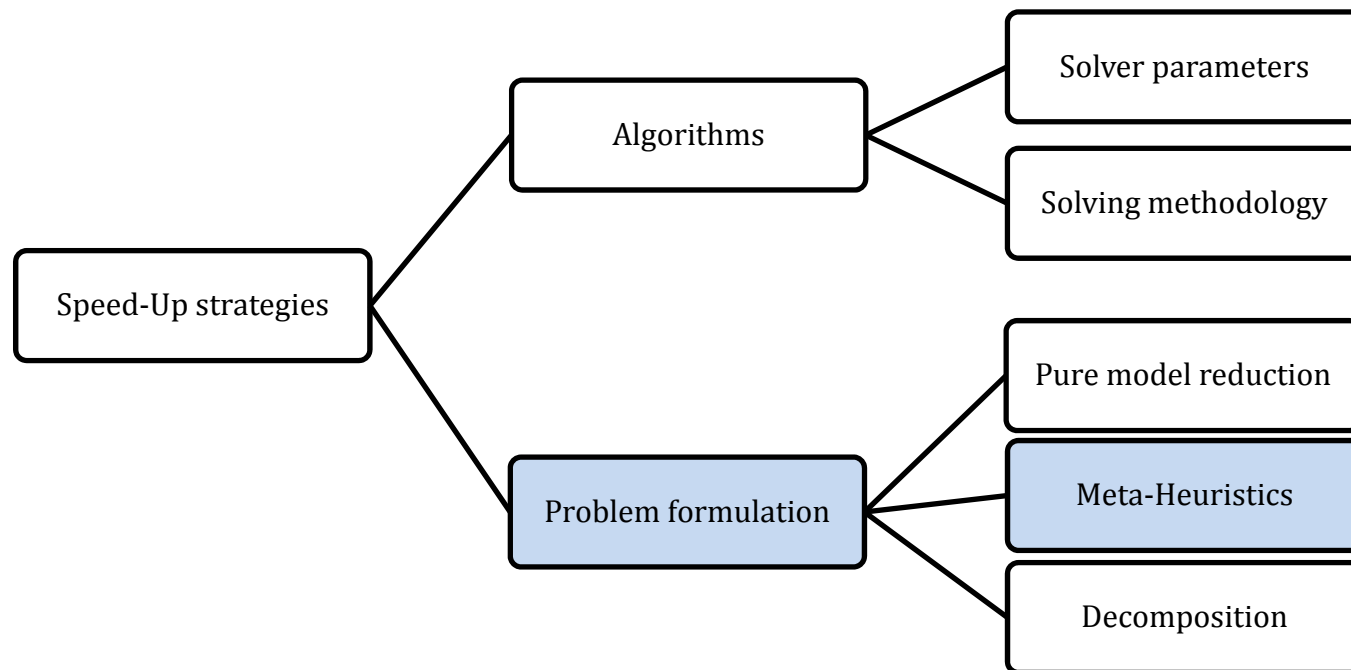
LP versus MILP



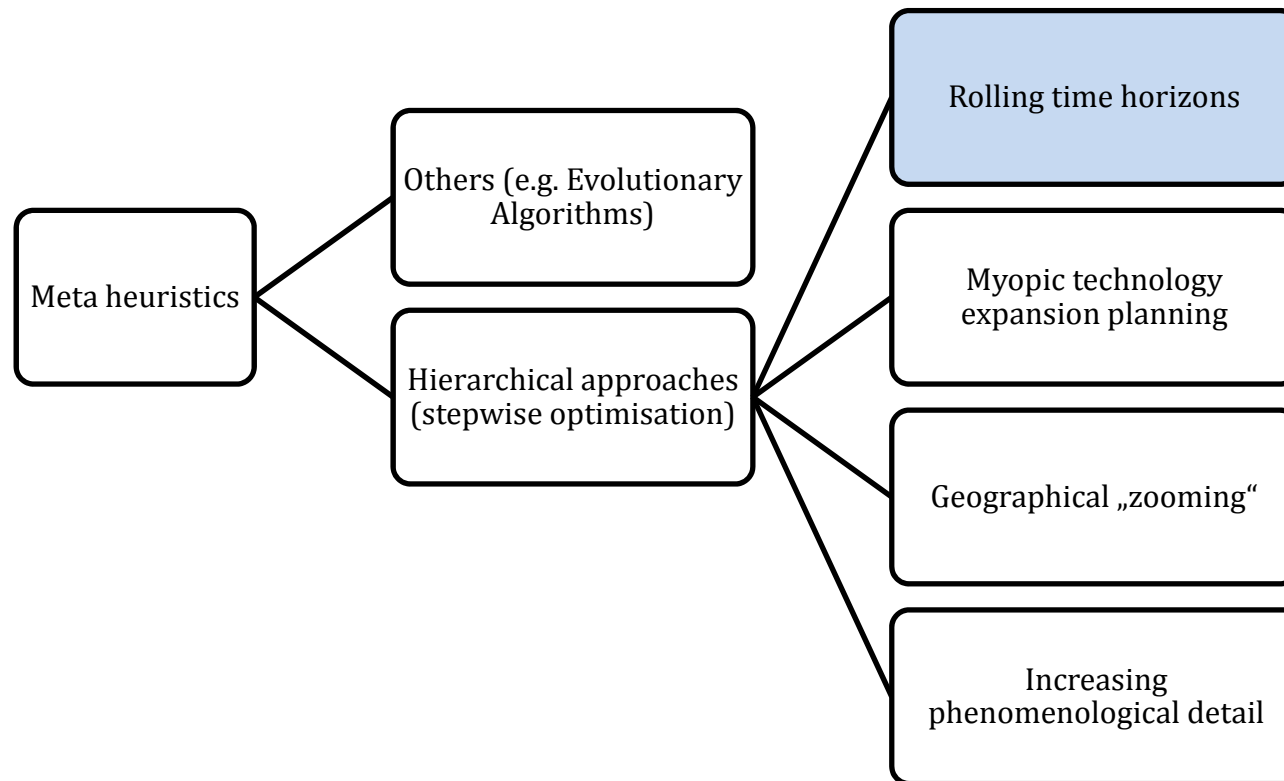
<sup>a</sup> Before curtailments, storage- and transmission losses

# Conceptual strategies

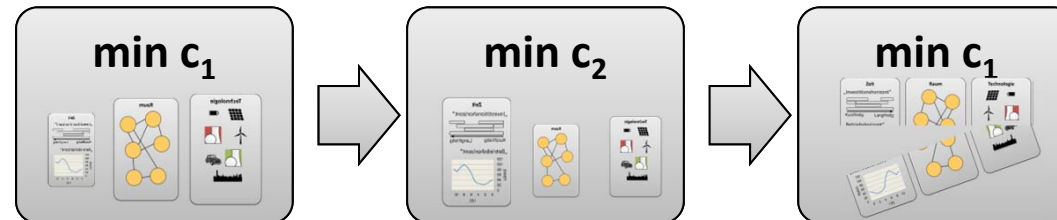
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# Meta heuristics

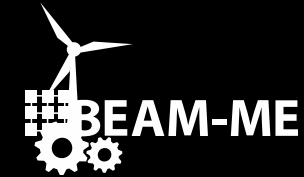


Hierarchical approaches



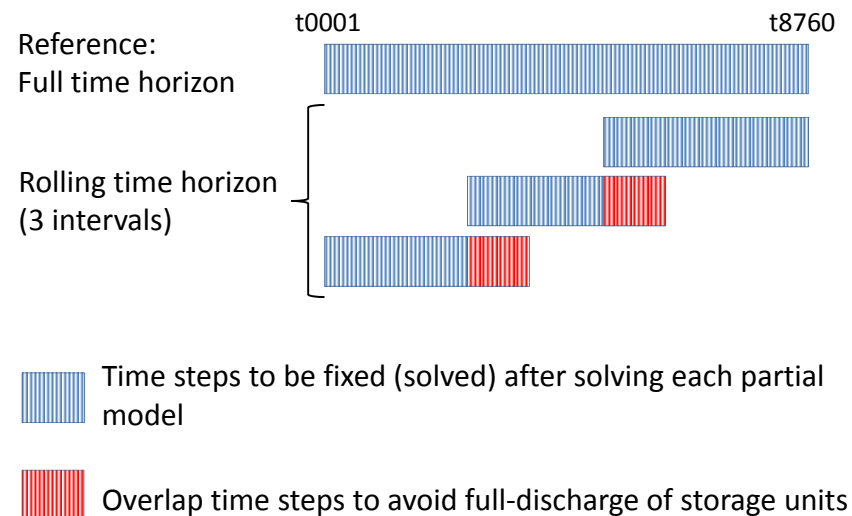


# Heuristics: Rolling horizon dispatch



## Idea and implementation

- Splitting of the optimisation time horizon into several *intervals*, using different *overlaps*
- Test influence of *intervals* and *overlaps* w.r.t. computing time and solutions accuracy (e.g. deviation in system costs, CO<sub>2</sub> emissions)
- time steps to be fixed after solving an interval

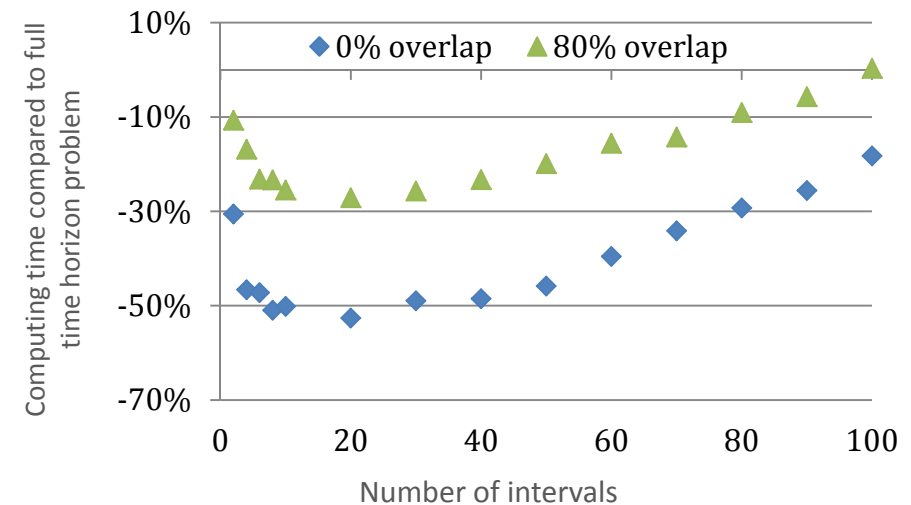


References:

Schreck, S: "Implementation and Analysis of a Rolling Horizon Approach for the Energy System Model REMix", University Stuttgart, 2016

## Results (medium-size ESMs)

- Reduction of computing times up to 53%



- Deviation of objective value usually <1%

Overlap-size [%]	2	4	6	8	10	20	30	40	50	60
0	0.13	0.98	1.02	1.03	1.48	1.69	2.30	2.76	2.90	3.19
20	0.09	0.06	0.24	0.28	0.32	0.59	1.02	1.17	1.46	1.54
40	0.10	0.05	0.07	0.10	0.12	0.28	0.47	0.64	0.78	0.81
60	0.03	0.04	0.06	0.08	0.10	0.21	0.34	0.52	0.54	0.58
80	0.02	0.04	0.05	0.07	0.09	0.19	0.30	0.38	0.56	0.61
100	0.02	0.03	0.05	0.06	0.07	0.18	0.28	0.30	0.48	0.54

Number of intervals

Challenge: Treatment of time integral constraints

- Storage balance: 
$$\begin{aligned} & \mathbf{P}_{stor,charge}(\tau_{stor}, y, n, t) - \mathbf{P}_{stor,discharge}(\tau_{stor}, y, n, t) - \mathbf{P}_{loss}(\tau_{stor}, y, n, t) \\ &= \frac{\left( \mathbf{S}(\tau_{stor}, y, n, t) - \mathbf{S}(\tau_{stor}, y, n, t_{-1}) \right)}{t_{sten}} \end{aligned}$$

$$\forall \tau_{stor} \in TEC_{stor}, \forall y \in Y, \forall n \in N, \forall t \in T$$

- Resource limit 
$$\sum_{\tau_{gen}, t} \mathbf{P}_{fuel}(\tau_{gen}, y, n, t, f) \leq R(y, n, f)$$

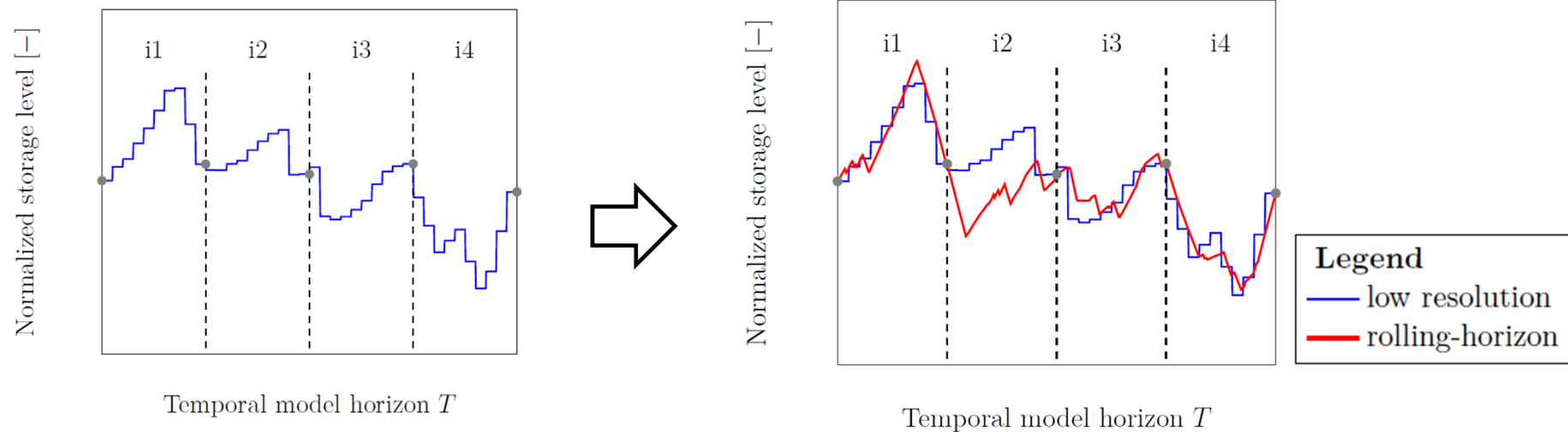
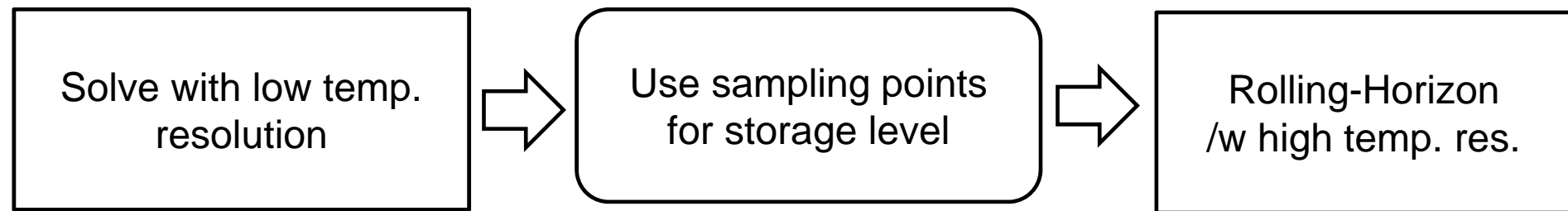
$$\forall \tau_{gen} \in TEC_{apl}, \forall y \in Y, \forall n \in N, \forall f \in F$$

- Emission limit 
$$\mathbf{G}(\tau_{gen}, y, n, f, e) = 1000 \cdot t_{ilen} \cdot \eta_{fe}(f, e) \cdot \sum_t \mathbf{P}_{fuel}(\tau_{gen}, y, n, t, f)$$

$$\forall \tau_{gen} \in TEC_{gen}, \forall y \in Y, \forall n \in N, \forall f \in F, \forall e \in E$$

## Heuristics to improve modeling of time integral constraints

e.g. seasonal storage, CO<sub>2</sub>-caps, biomass potential





## What we know...

- There is a whole bunch of them
- ESM often apply rolling time horizon approaches
- No guarantee for getting the global optimum

## What we already learnt...

- Require additional knowledge about the system
- Trade-off between speed and loss of accuracy

Implementation cost	Speed-up capability
	

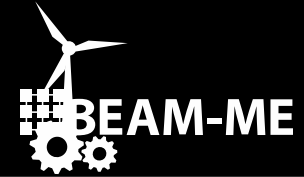
## What we estimate...

- Meta heuristics will still occur in ESM for other reasons (e.g. better approximation of reality)

## What we want....

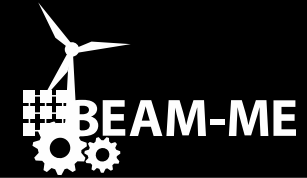
- Keep them in mind, but we would like to get exact solutions.

# Summary and Conclusions

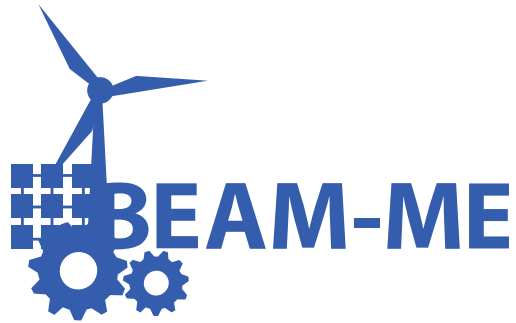


- Waiting for the next generation of processors is no reasonable option
- Best-practice usage of GAMS already helps a lot
  - take “low hanging fruits”
- Detailed evaluation of the impact of model aggregation has high value
  - do systematic benchmark of speed-capability and error estimation
- Evaluation of required technological detail important (e.g. MIP vs. LP in power plant dispatch)
  - What detail is required? How do results change?

# Next steps



- Systematic evaluation of conceptual speed-up strategies
  - Quantification of advantages
  - Evaluation of scaling behaviour
- Implementation of different decomposition techniques in REMix
  - Performance tests
  - Comparison with other ESM using LP
- Further evaluation of the requirements of using HPC
- Preparation of REMix for the application of HPC



# Thank you!

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