

# Modeling SEI Formation and Morphology

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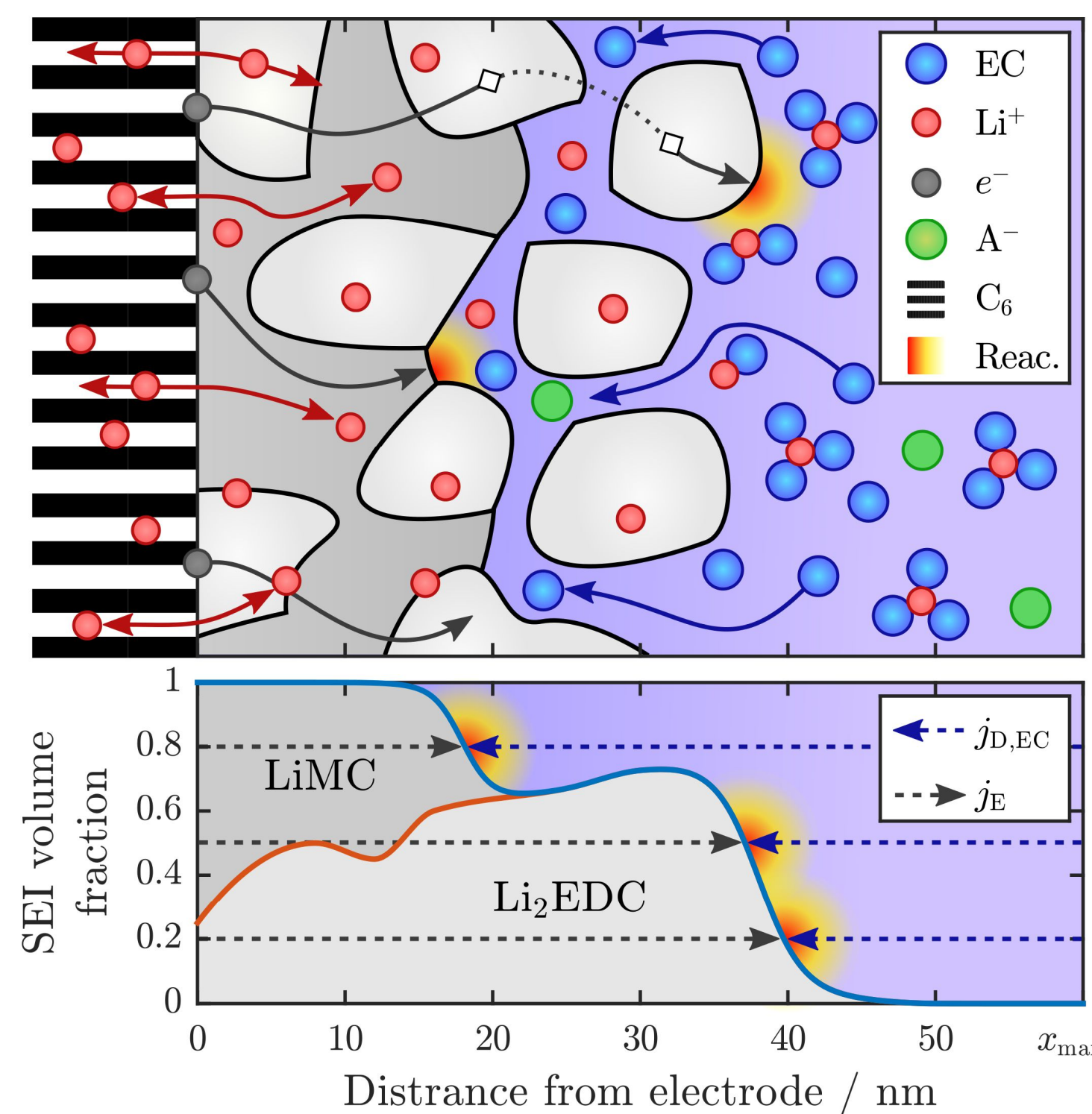
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## Introduction

- Modeling growth of nano-porous SEI
- 1D model, model axis perpendicular to electrode
- Transport of electrons and solvent [1-3]
  - Electrons: solid SEI
  - Binary electrolyte in pores, EC/DMC 3:7
- Up to two electrolyte reduction reactions forming different SEI compounds



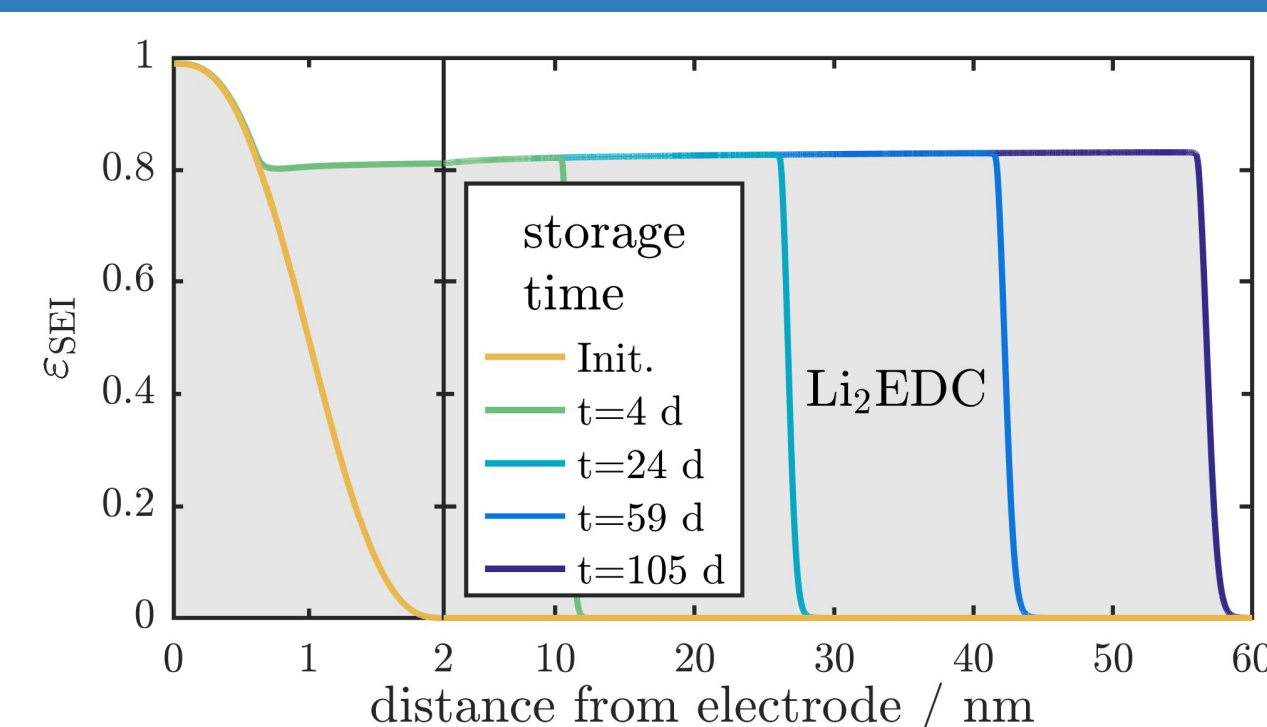
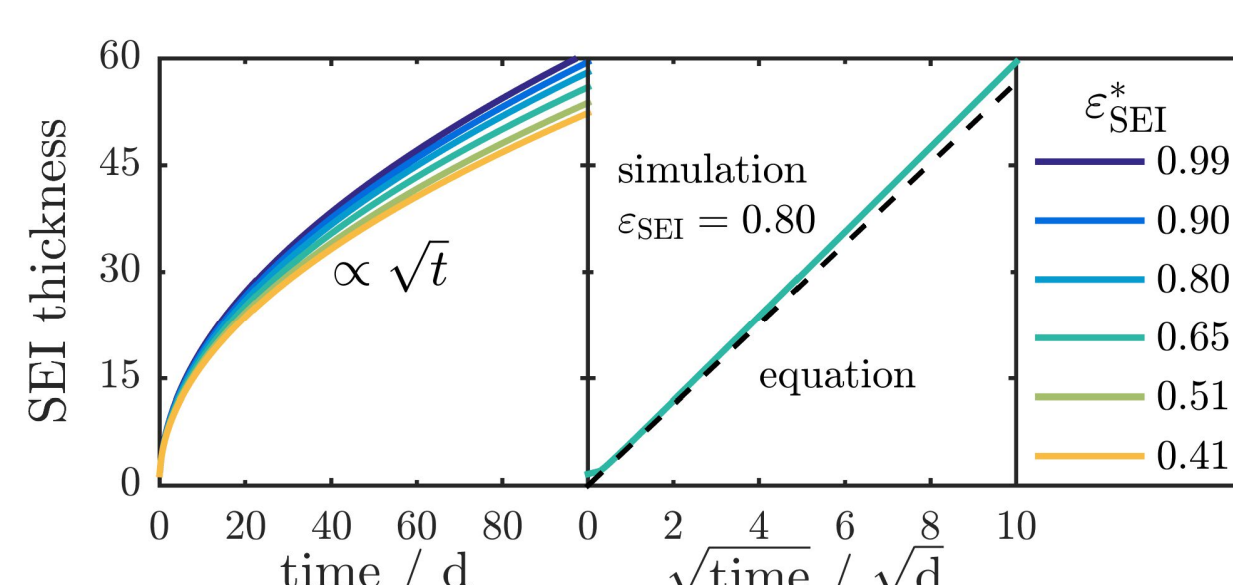
## SEI Growth Model

- SEI volume fraction evolution along an axis perpendicular to the electrode surface
 
$$\partial_t \varepsilon_i = V_i \dot{s}_i - \text{div}(\varepsilon_i \tilde{v})$$
  - Solvent diffusion and convection in the electrolyte phase (binary mixture)
 
$$\partial_t(\varepsilon c_i) = -\text{div}(j_{D,i} + j_{c,i}) - v_i \dot{s}_i$$
  - Electron conduction within the solid SEI phase
 
$$0 = -\text{div}(j_E) - F \dot{s}_i$$
  - Convection velocity from incompressibility ( $V_i^{\text{sol}} c_i = 1$ )
 
$$\text{div } v = \sum (2V_i - v_i V_i^{\text{sol}}) \dot{s}_i$$
  - Solid convection
 
$$\text{div } \tilde{v} = \alpha(\varepsilon) \dot{\varepsilon}_{\text{SEI,C}} / \varepsilon_{\text{SEI}}$$
- | Bruggeman relation                                      | Flux densities                          |
|---|---|
| $D = \varepsilon^\beta D_{\text{Bulk}}$                 | $j_{c,i} = c_i v$                       |
| $\kappa = (1 - \varepsilon)^{1.5} \kappa_{\text{Bulk}}$ | $j_{D,i} = -D \cdot \text{grad } c_i$   |
|   | $j_E = -\kappa \cdot \text{grad } \Phi$ |
- Butler-Volmer:  $\dot{s}_i = A(\varepsilon) \Gamma \frac{k_B T}{h} \exp\left(\frac{-E_A}{k_B T}\right) (c_i / c_i^0)^{\frac{v_i}{2}} 2 \sinh\left(\frac{RT}{F} \eta_i\right)$ 

$$\eta_i = -(\Phi - \Phi_i^0) + v_i \ln\left(\frac{c_i}{c_i^0}\right)$$
  - Specific surface area:  $A(\varepsilon) = \frac{1}{a_0} \varepsilon \left( \varepsilon_{\text{SEI}} + \frac{a_0^2}{6} \frac{\partial^2 \varepsilon}{\partial x^2} \right)$

## Simulations: Inert Co-Solvent

- Formation of porous SEI
- constant SEI porosity**  
 $\varepsilon^* = 1 - \varepsilon_{\text{SEI}}^*$
- SEI thickness **growth with  $\sqrt{t}$**



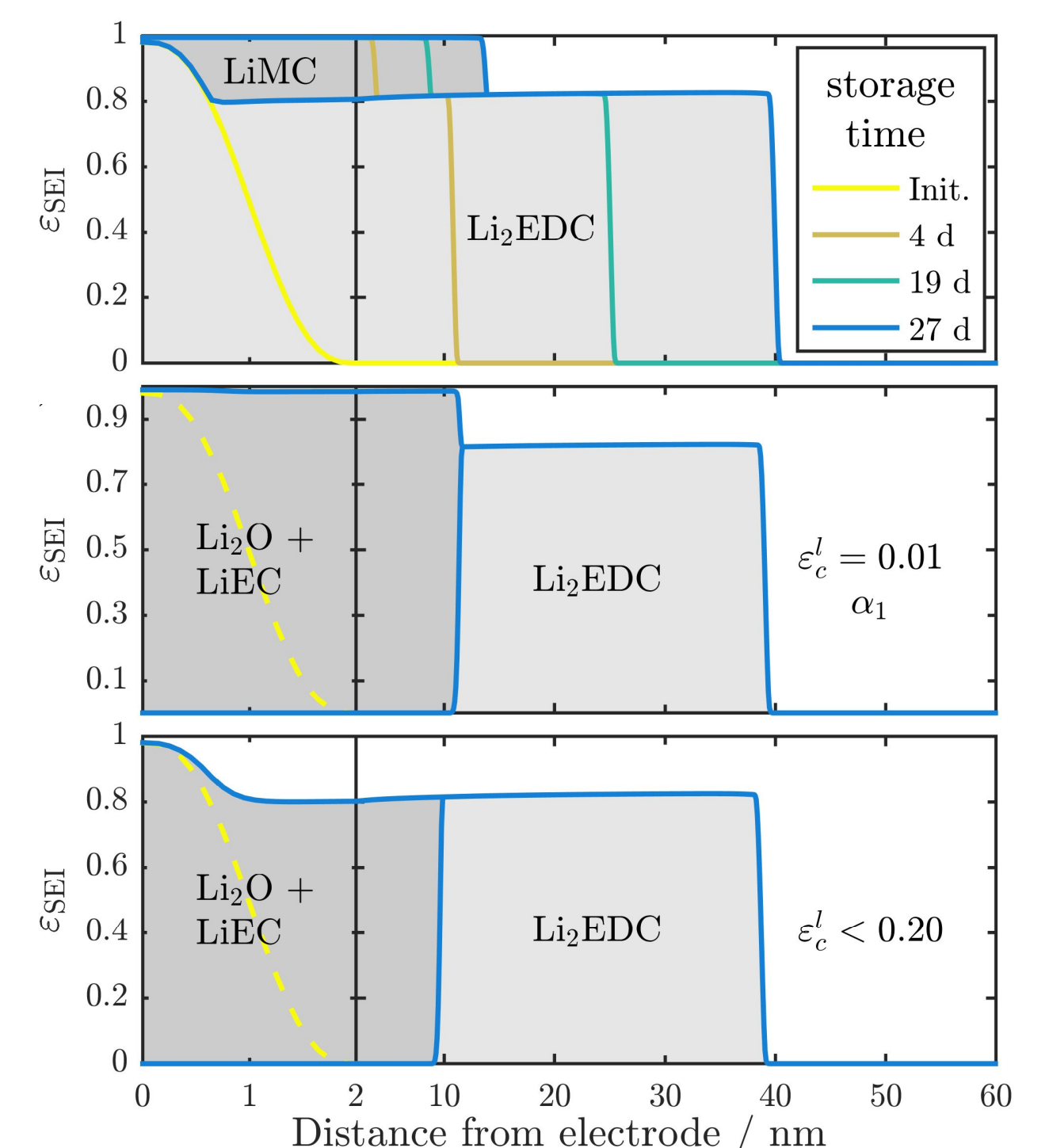
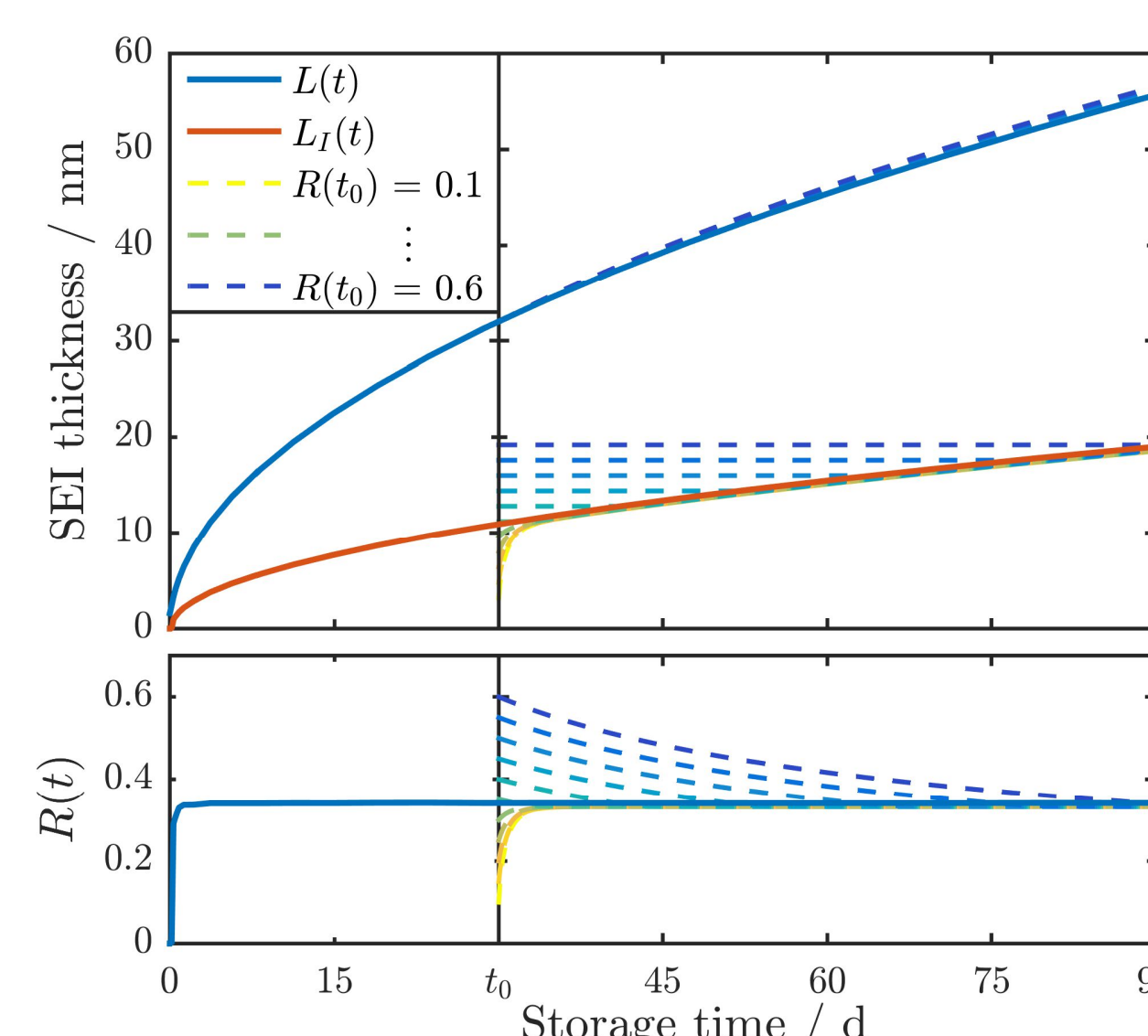
$$L(t) \approx \sqrt{V_1 \kappa^* \Delta \Phi_1 / 2 F \varepsilon_{\text{SEI}}^* \sqrt{t}}$$

- Electronic conductivity from fit to experiment [1,2]
 
$$\sigma_{\text{Bulk}} = 0.3 - 4.5 \text{ pS/m}$$
- Analytic expression for porosity
 
$$\frac{\kappa^*}{D^*} = \frac{F^2 c_1^0}{RT} \left( \frac{1}{2} + \beta \frac{1 - \varepsilon^*}{\varepsilon^*} \right)$$

## Simulations: Dual-Layer SEI

- Second reduction reaction
  - Active co-solvent
  - Conversion of Li2EDC

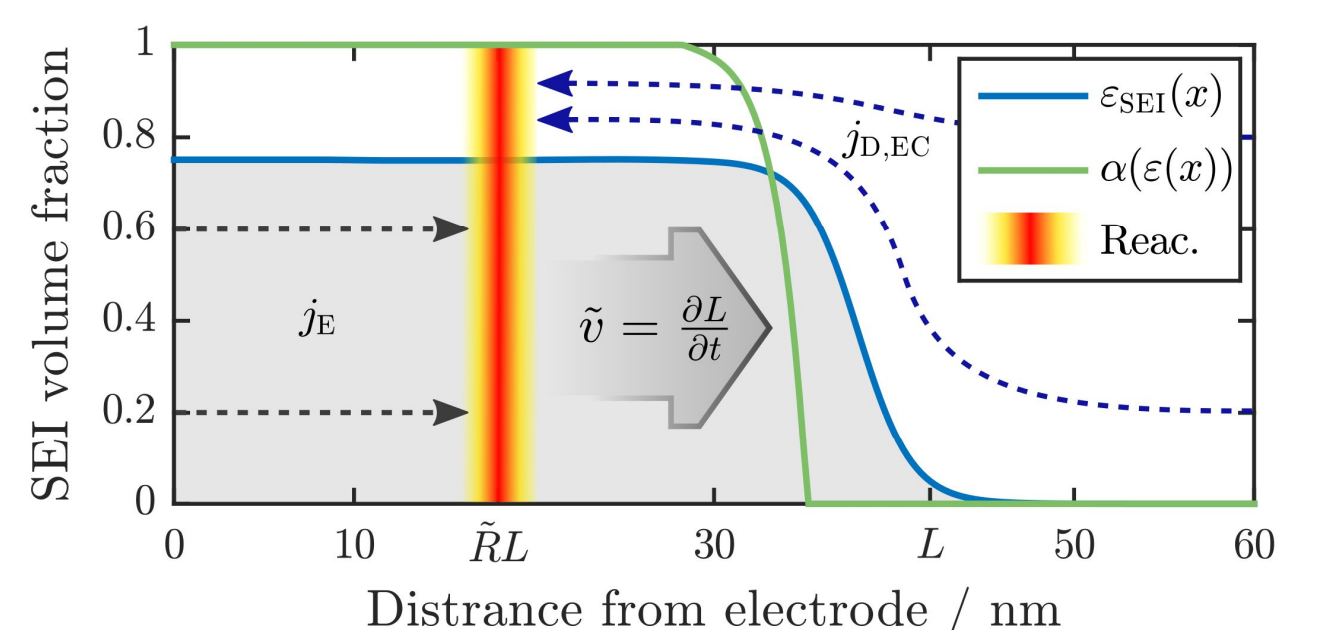
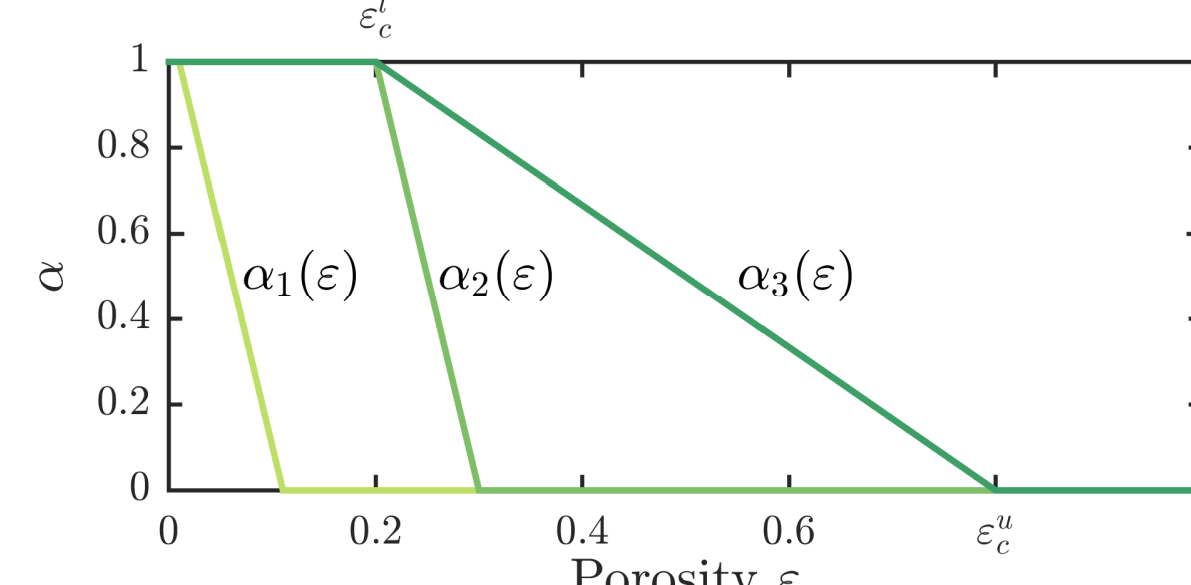
### Dual-layer SEI



- Inner and outer layer thickness ( $L_I$  and  $L$ ) are related
 
$$R(t) = \frac{L_I(t)}{L(t)} \rightarrow R_{\text{stat}}$$

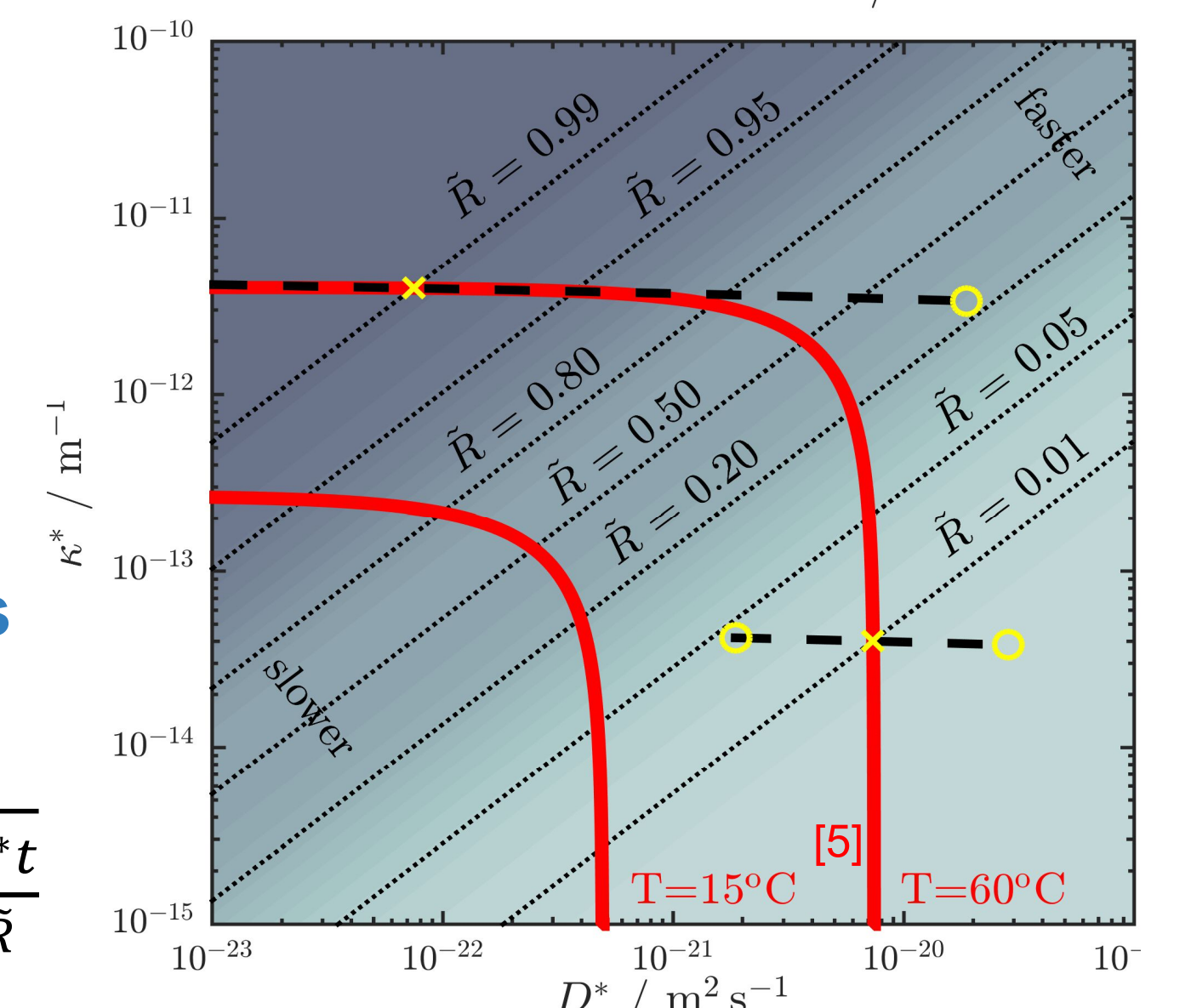
## Simulations: Self-Shaping SEI

- Assumption: SEI porosity is a material property
  - Set porosity with  $\alpha(\varepsilon)$



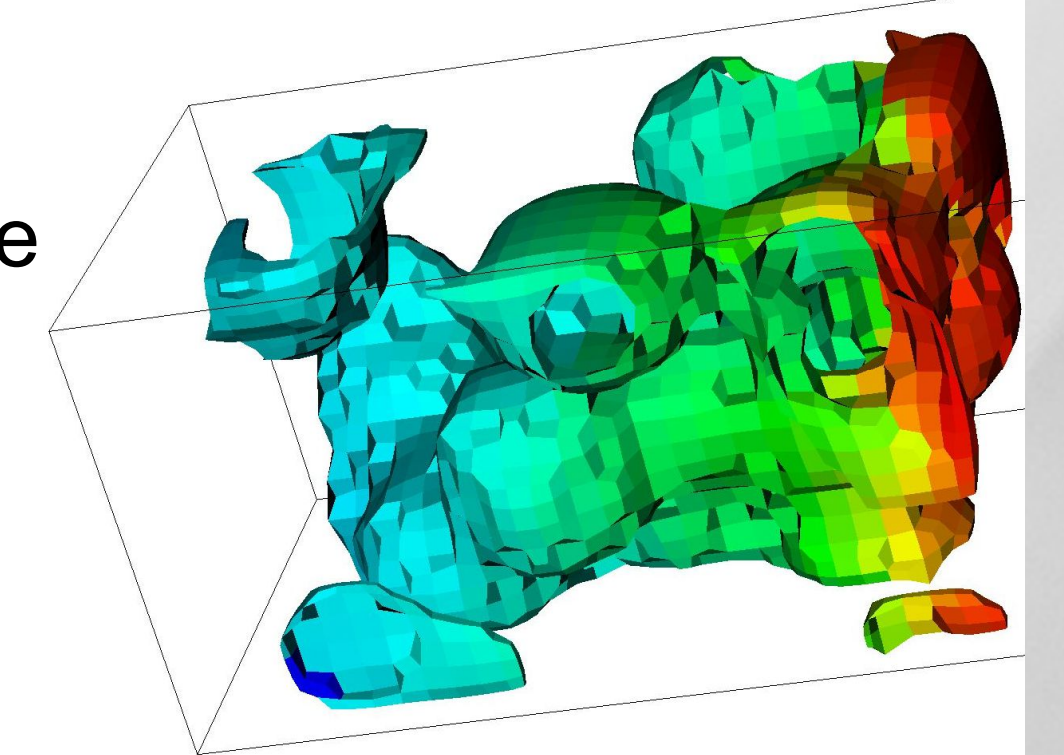
- Reaction interface inside the SEI, located at  $x = \tilde{R} \cdot L$
- Both transport mechanisms contribute**

$$\tilde{R} = \left( 1 + \frac{D^* F c}{\kappa^* \Delta \Phi} \right)^{-1}, \quad L(t) \propto \sqrt{\frac{\kappa^* t}{\tilde{R}}}$$



## 3D Electrode Simulation

- BEST: 3D transport simulation with porous electrodes [6]
- Simple SEI growth model on the graphite surface
  - Prediction of inhomogeneous SEI thickness
  - Understanding intercalation through SEI and lithium loss during cycling



## References

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- [2] Christensen, J., Newman, J. *Electrochem. Soc.* **151** (11), A1977 (2004).
- [3] Jorn, R et al. *J. Phys. Chem. C*, **117** (8), 3747-3761. (2013)
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- [5] Liu, P., Wang et al. *J. Electrochem. Soc.*, **156**, A499, (2010).
- [6] ITWM, BEST - Battery and Electrochemistry Simulation Tool, <http://itwm.fraunhofer.de/BEST>

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