

Gefördert durch:



aufgrund eines Beschlusses  
des Deutschen Bundestages

# Getting linear energy system models ready for High Performance Computing

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**A PROJECT BY**



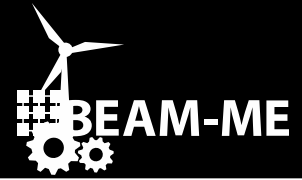
H L R I S



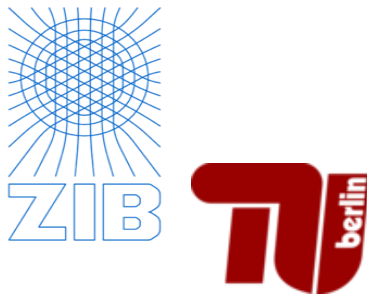
DLR

Deutsches Zentrum  
für Luft- und Raumfahrt  
German Aerospace Center

# Interdisciplinary Project Partners



- German Aerospace Center (DLR),  
Department for System Analysis and Technology Assessment



- Zuse Institute Berlin (ZIB),  
Department for Mathematical Optimization and Scientific Information
- Technical University Berlin,  
Institute for Mathematics



- GAMS Software GmbH

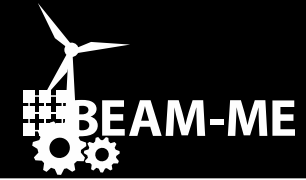


- Forschungszentrum Juelich (FZJ),  
Juelich Supercomputing Centre (JSC)

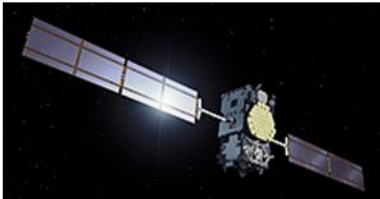


- High Performance Computing Center Stuttgart (HLRS)

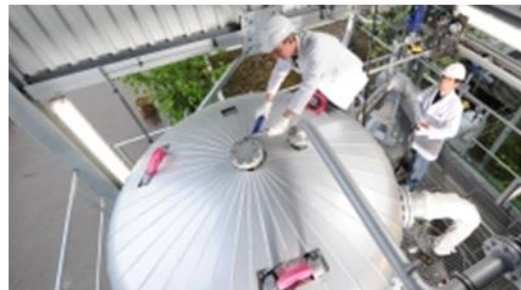
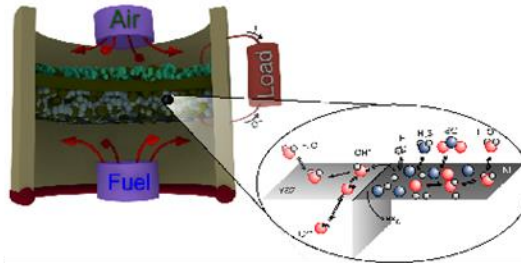
# It is not all about rocket science in DLR...



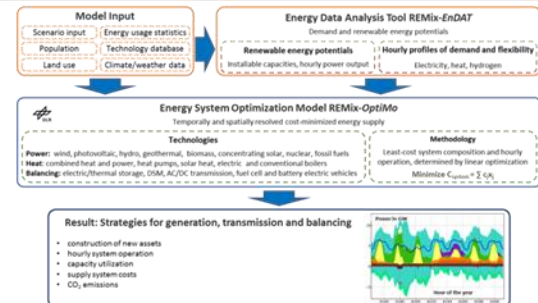
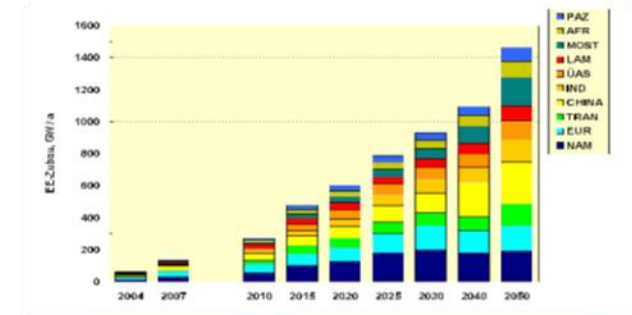
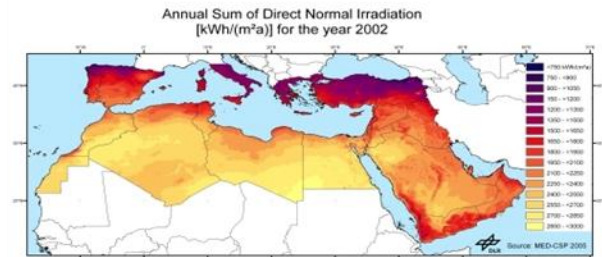
DLR



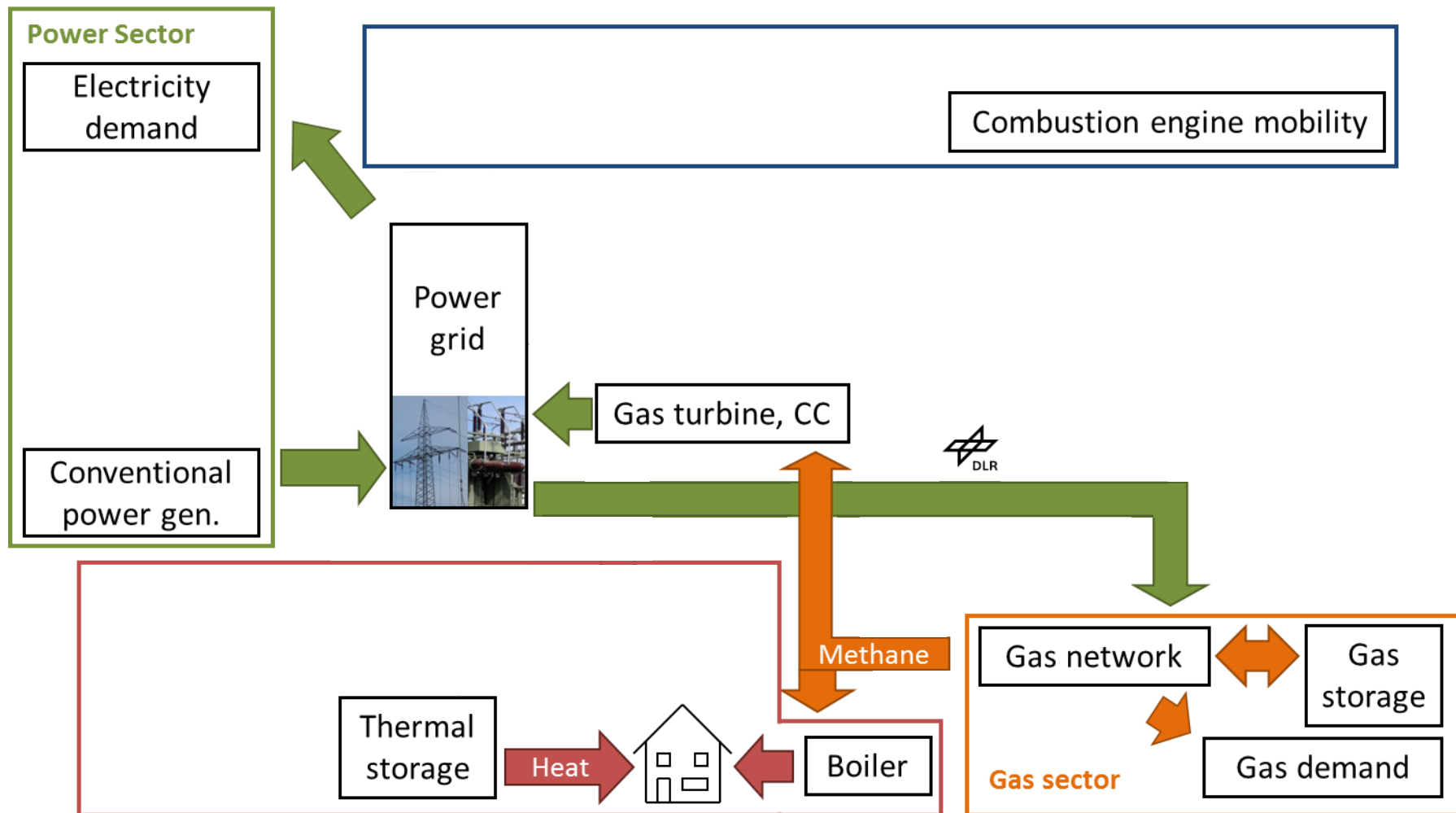
Institute of Engineering Thermodynamics



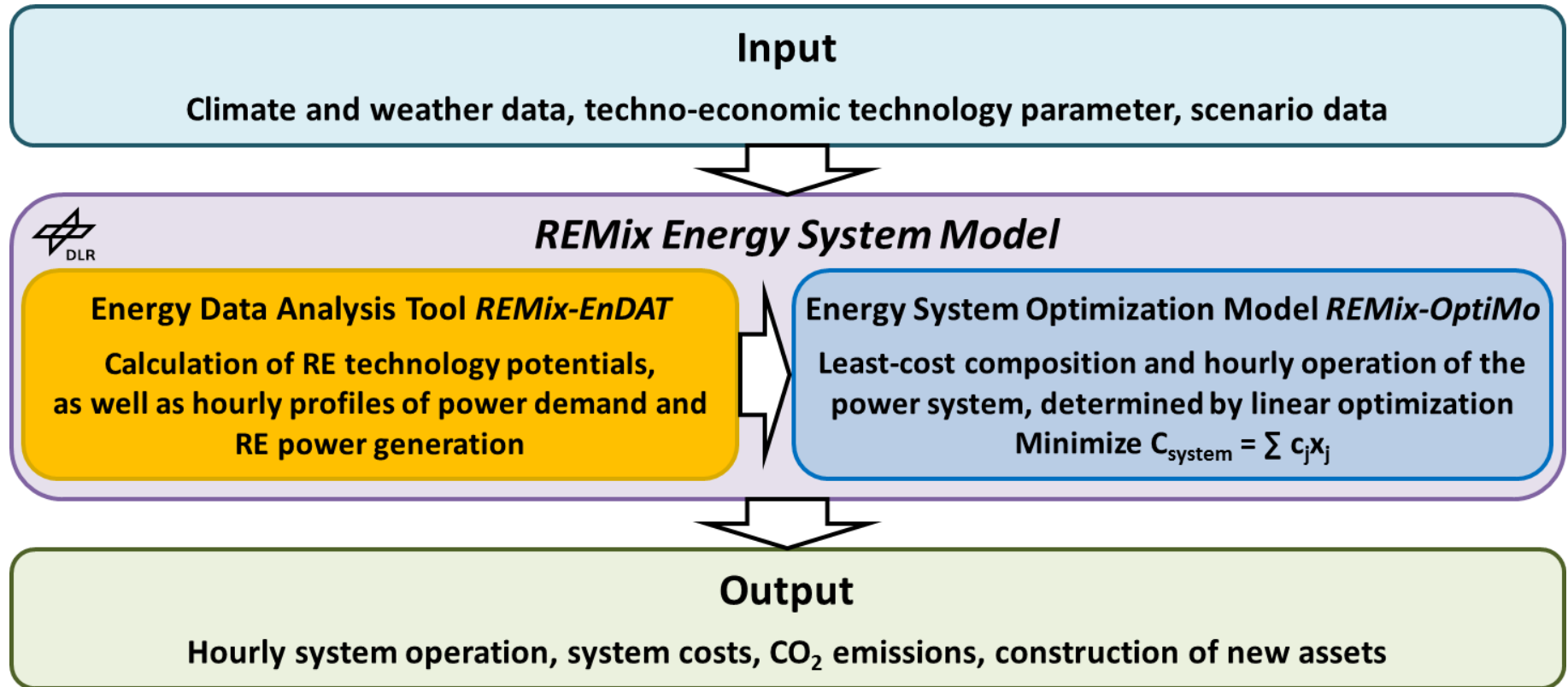
Systems Analysis and Technology Assessment



# Energy Sector Integration



Ongoing transformation drastically increases complexity of the energy system

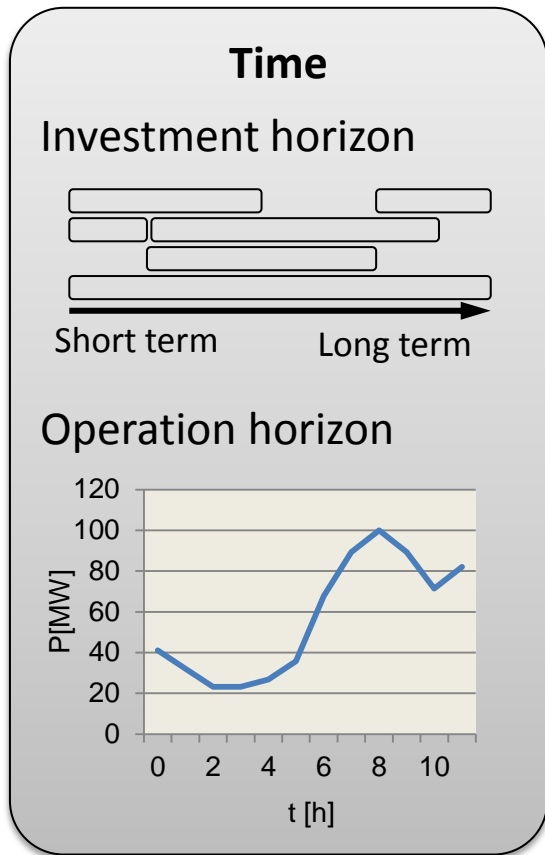


Reduction of solution times urgently needed to enable the reflection of energy system complexity in state-of-the-art models

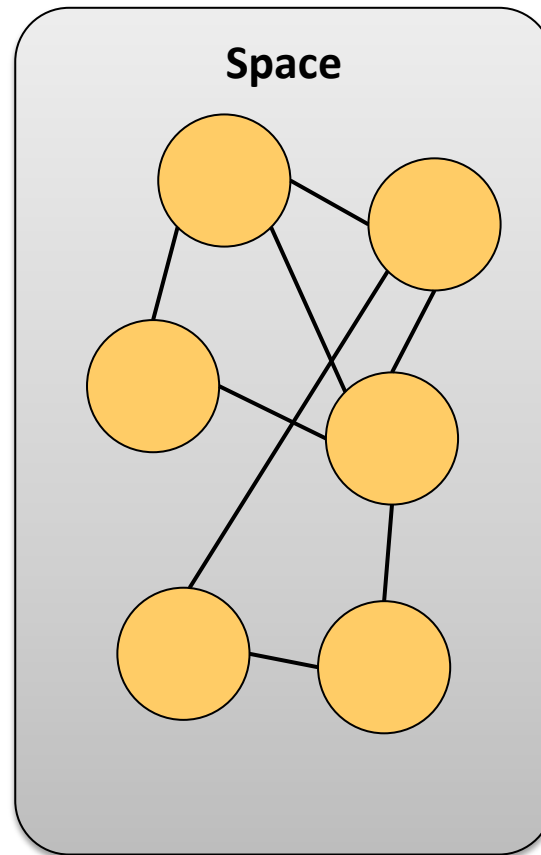


- Evaluation of different approaches to reduce model solution times
  - Increased modelling efficiency
  - Higher computing power
- Implementation of selected approaches into REMix
- Assessment of the transferability to other models
- Definition of best-practice strategies

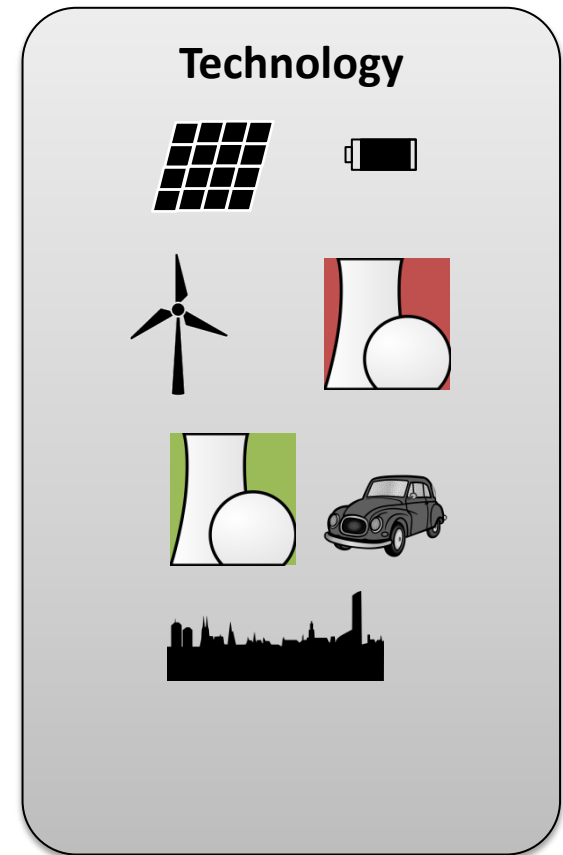
# Typical energy system model dimensions



8760 time steps



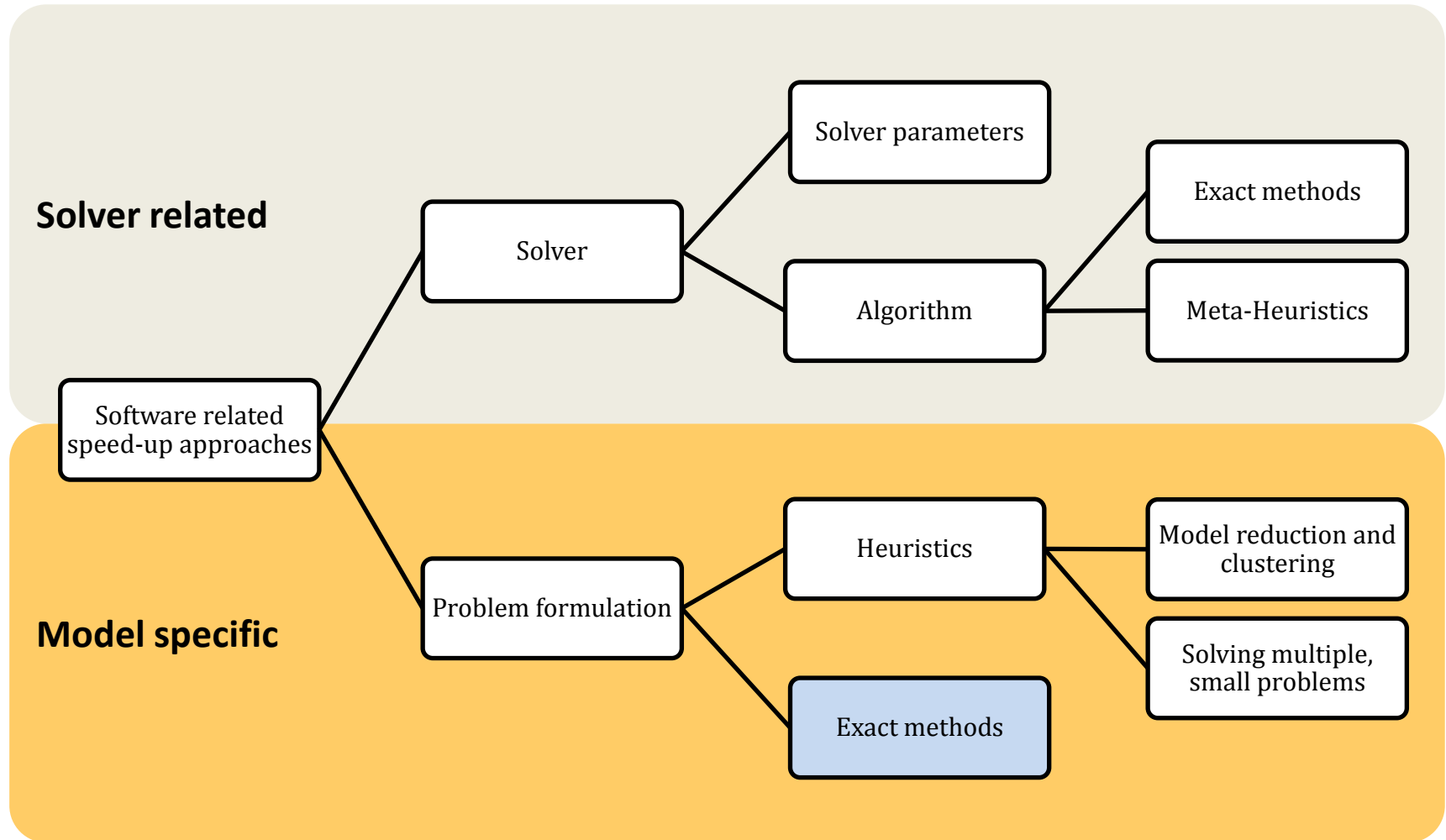
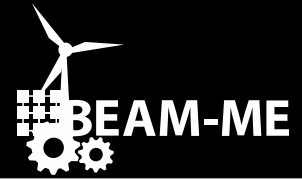
60 regions



20+ technologies

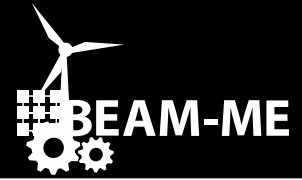
Interlinking between dimensions leads to decomposition options

# Categorization of speed-up approaches

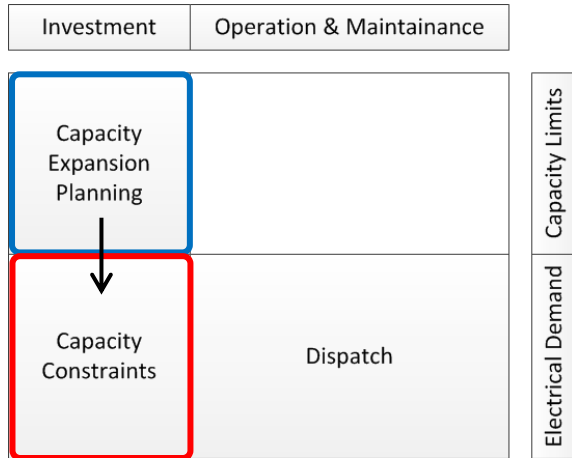




# Benders Decomposition



**Optimization of power plant capacities**  
based on expected future costs



$$\min c \cdot x$$

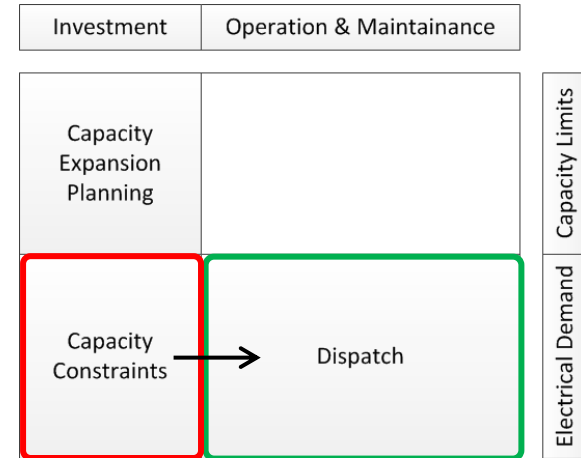
$$A \cdot x \leq b$$

+

$$\theta$$

Future costs of subproblems

**Optimization of power plant dispatch**  
based on given power plant capacities



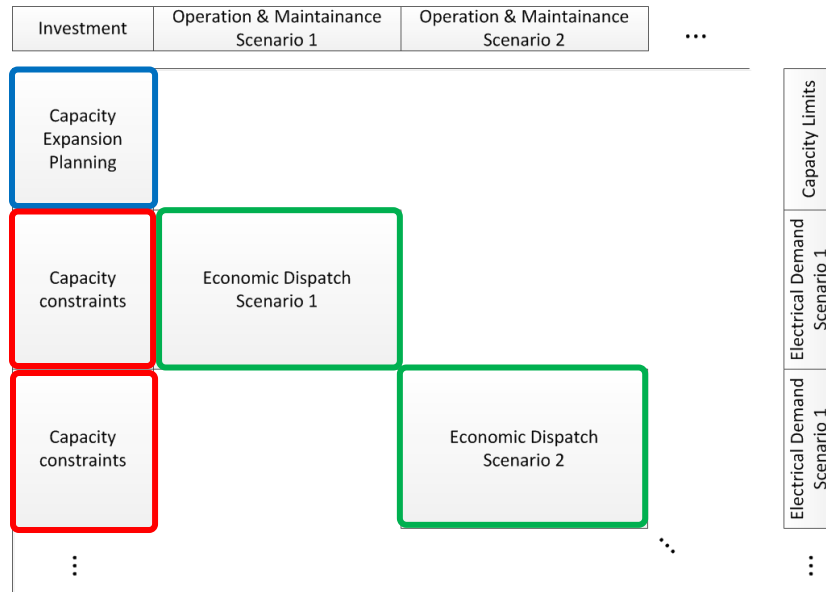
$$\min c \cdot x$$

$$A \cdot x \leq b$$

Actual costs of subproblems

Information about actual costs of the subproblems improves new estimation of future costs (optimality cuts)

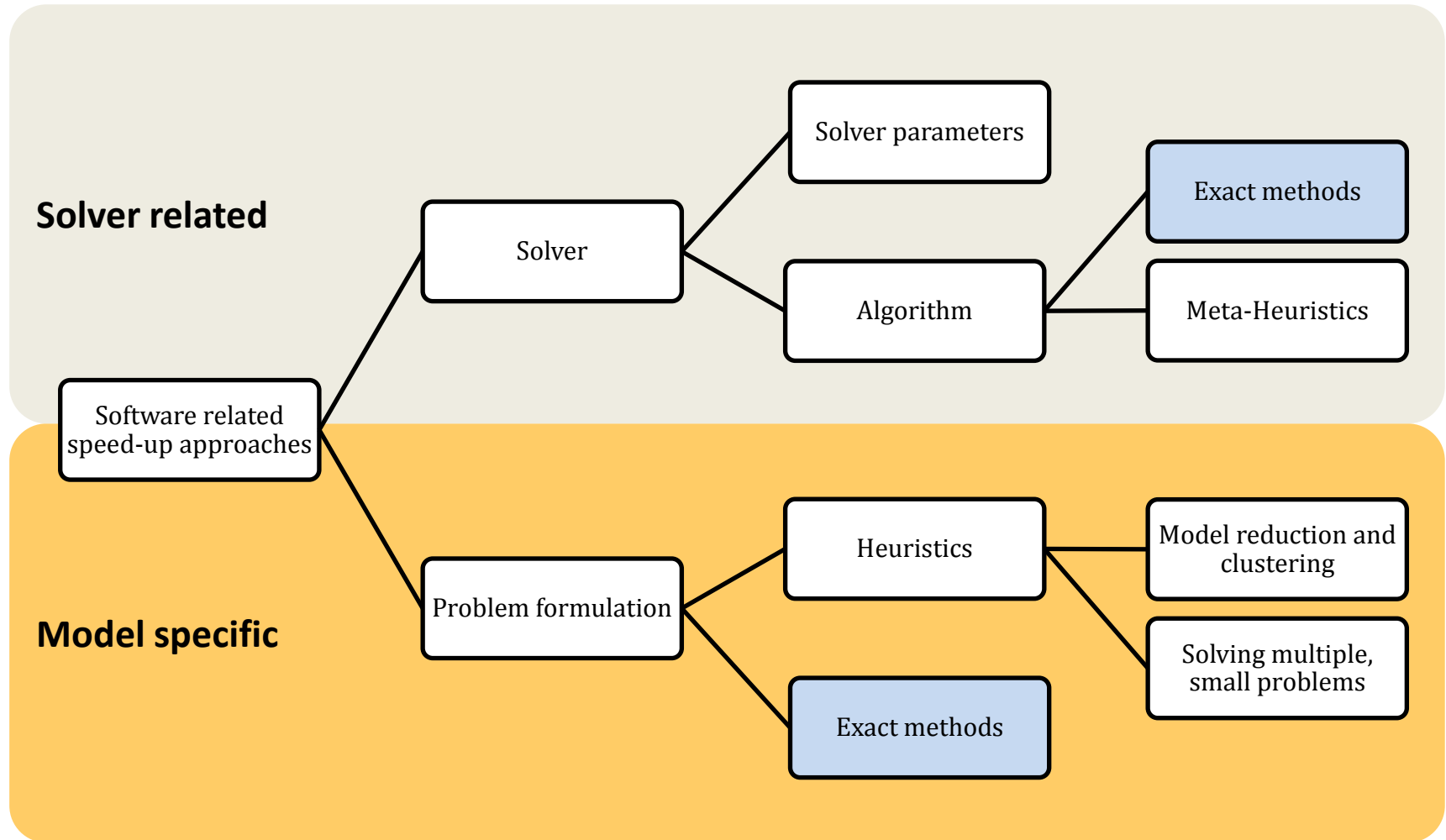
Stochastic Optimization leads to large LP structures (**deterministic equivalent**)



$$\begin{aligned}
 & \min \quad c^T x \\
 \text{s.t.} \quad & \boxed{T_0 x_0} \\
 & \boxed{T_1 x_0} + \boxed{W_1 x_1} \\
 & \boxed{T_2 x_0} + \boxed{W_2 x_2} \\
 & \quad \vdots \\
 & \boxed{T_N x_0} + \boxed{W_N x_N}
 \end{aligned}$$

- Capacity expansion decisions influence the stochastic dispatch scenarios  
 → Linking variables connecting the investment and dispatch decisions
- Different dispatch scenarios are not linked to each other only via the master problem  
 → No linking constraints

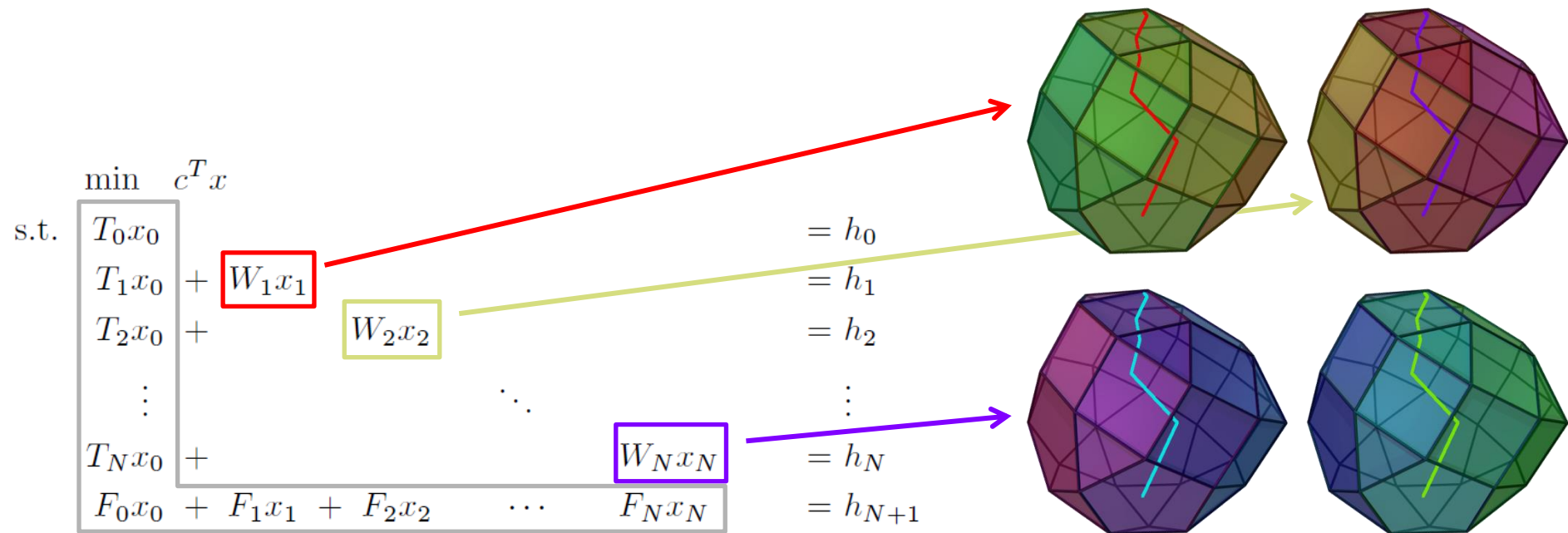
# Categorization of speed-up approaches



# Introducing PIPS-IPM

Parallel Interior Point Solver – Interior Point Method (PIPS-IPM)

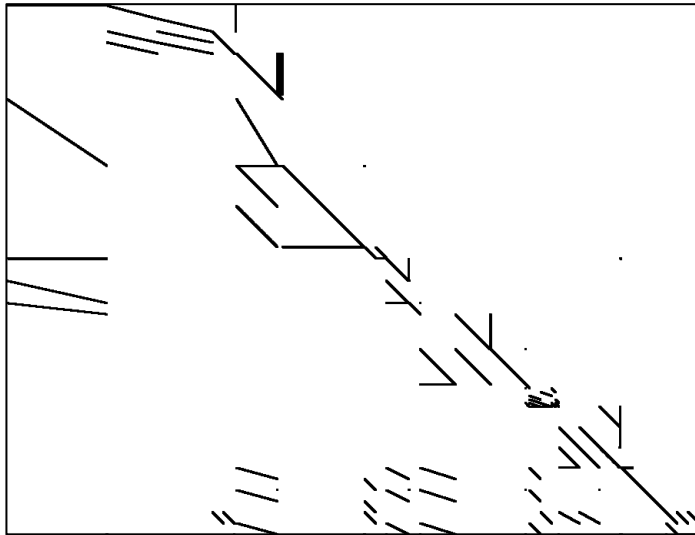
- Petra et al. 2014: *“Real-Time Stochastic Optimization of Complex Energy Systems on High-Performance Computers”*
- Wind feed-in planning in electrical power systems under uncertainty



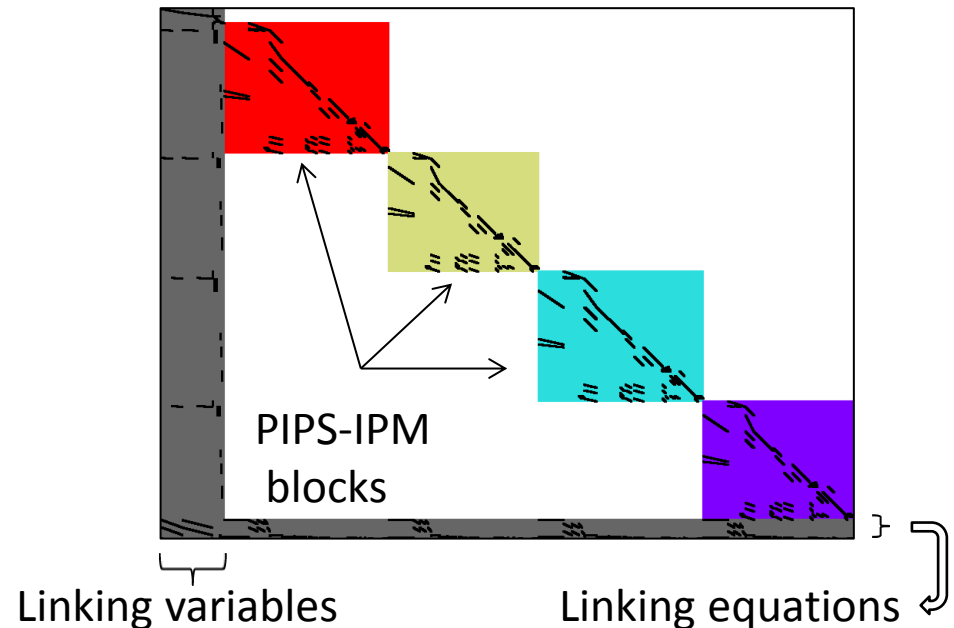
➔ TB-02-4: D. Rehfeldt „Optimizing large-scale linear energy problems with block diagonal structure by using parallel interior-point methods“

- Annotation of REMix model to communicate block structure
  - Application of the *stage* functionality to **assign variables and constraints to blocks** (DLR/GAMS)
- Enhancement of PIPS-IPM
  - Extension to handle LPs with both **linking variables and constraints** (ZIB/TU Berlin)
  - Development of a link between **GAMS and PIPS-IPM** (GAMS)
  - Consideration of **requirements of high performance computers** (ZIB/GAMS/HLRS/JSC)

Matrix of **non-zero entries** of REMix LP



Permuted matrix revealing **block structure**

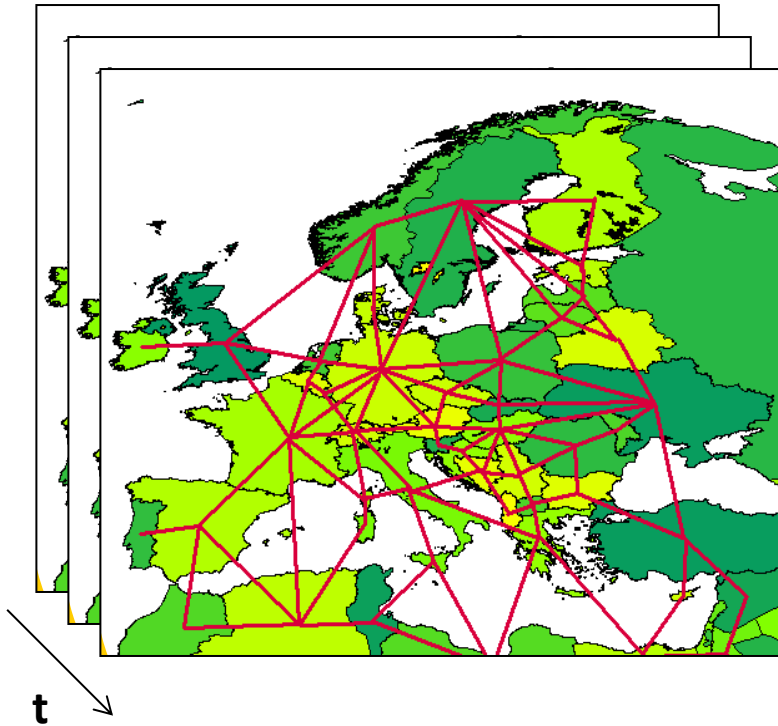


Annotation can be implemented directly in GAMS  
Modellers provide knowledge about problem and decompositions

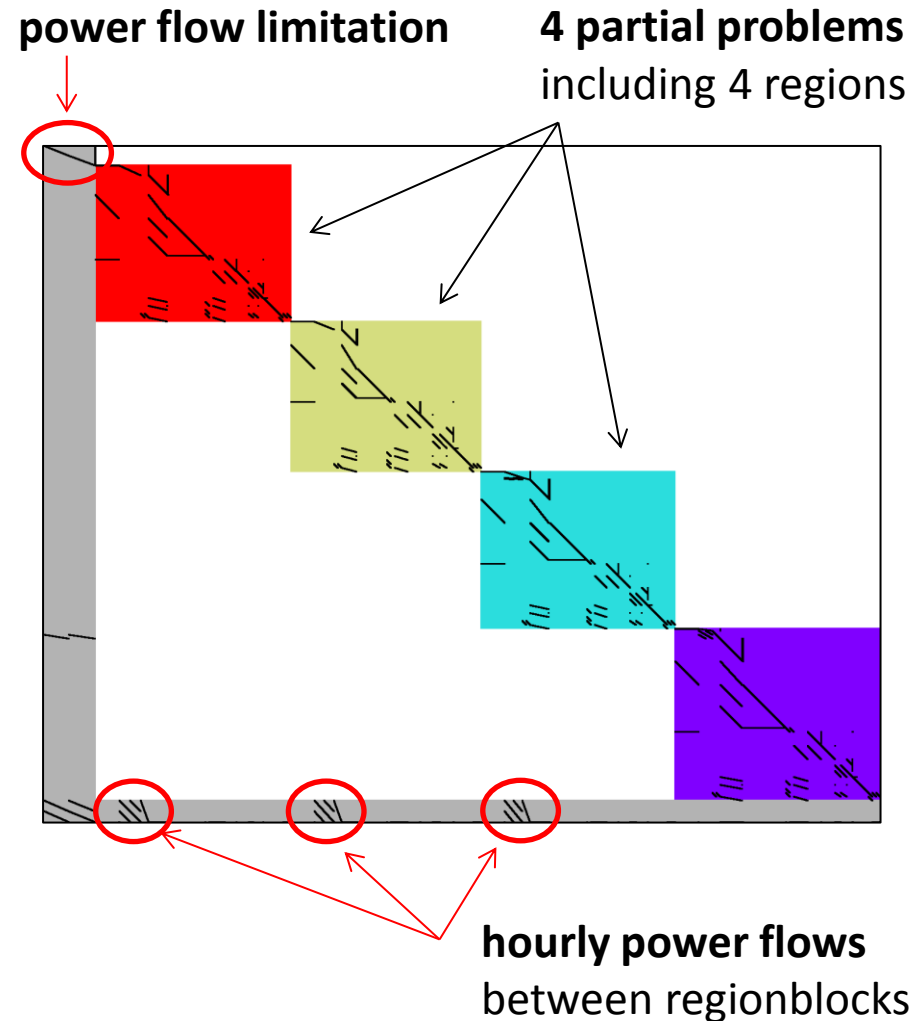
➔ TB-02-3: F. Fiand „*High Performance Computing with GAMS*“

# Decomposition by region I

Linking by region: electricity transports, fuel transports, global constraints (CO<sub>2</sub>)

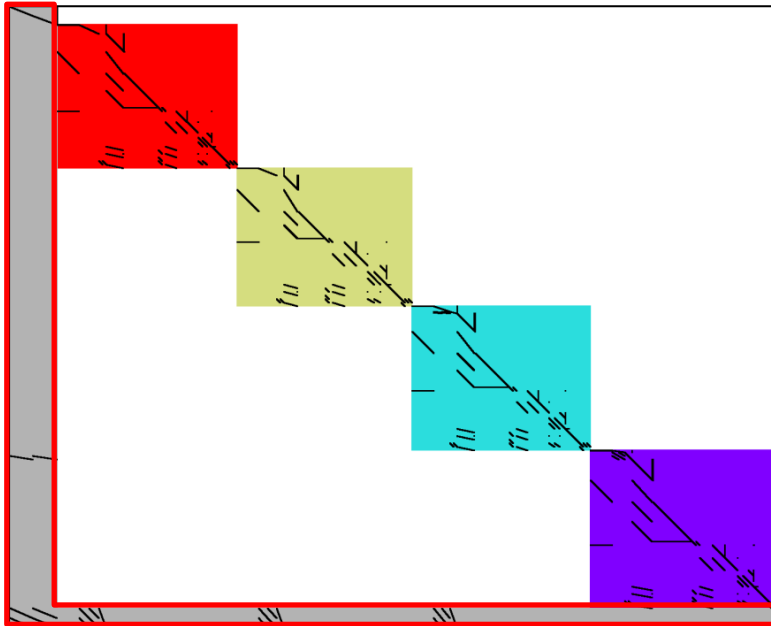


Temporal dimension of transport decisions leads to the largest number of linking variables

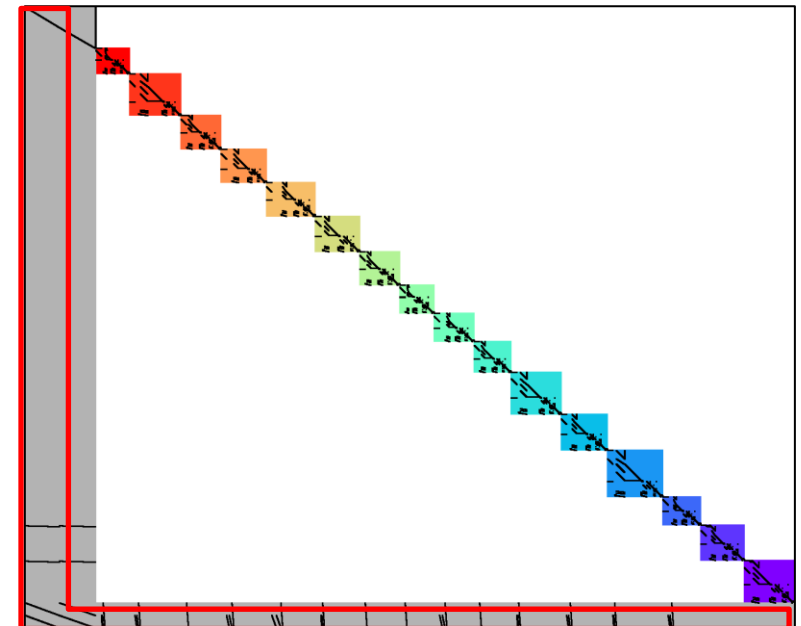


# Decomposition by region II

4 partial problems  
including 4 regions



16 partial problems  
including 1 region



low increase in linking variables and constraints  
due to **sparsely connected** regions

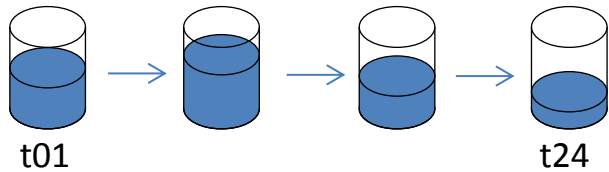
Target: Find **maximum number** of regionblocks of **similar size** which are **sparsely linked** to other regionblocks



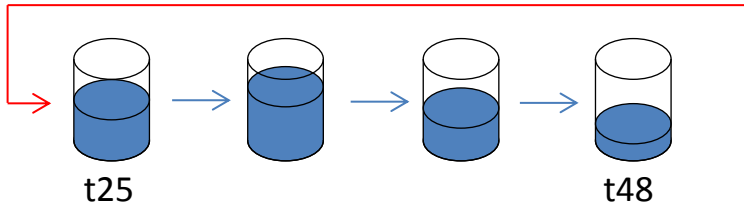
# Decomposition by time I

Linking by time: storages, demand side management, annual constraints

## timeblock 1



## timeblock 2

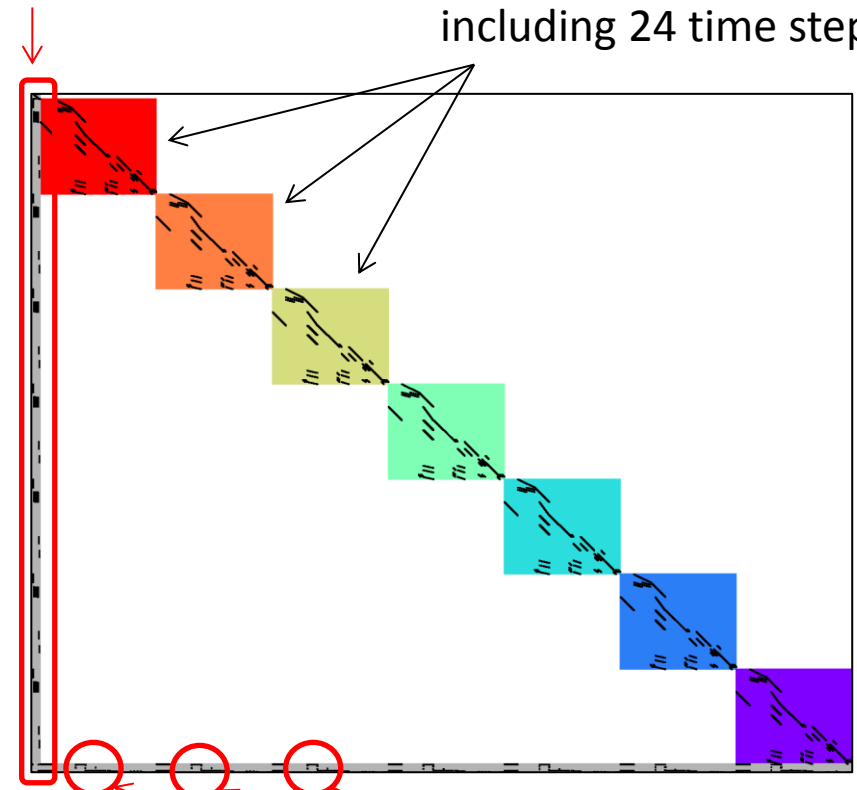


Linking of storage levels to their previous time step leads to linking constraints between timeblocks

annual emissions

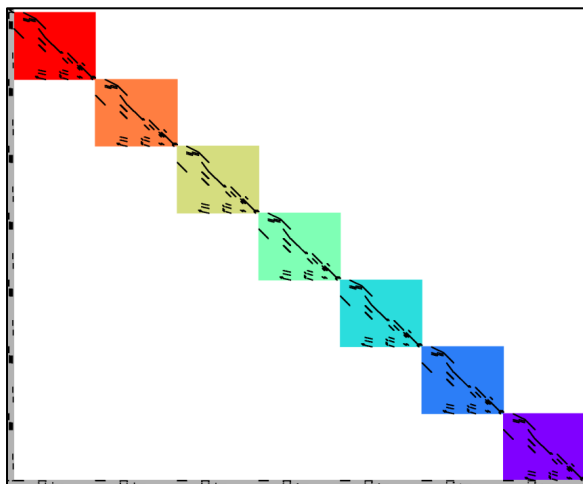
7 partial problems

including 24 time steps



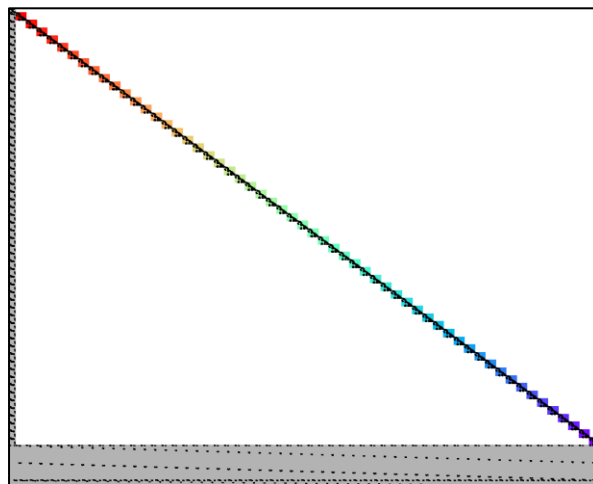
# Decomposition by time II

**7 partial problems**  
including 24 time steps



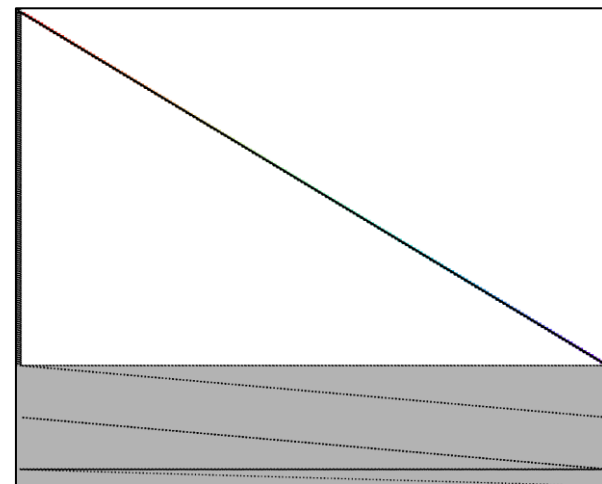
**1 out of 24** storage  
constraints linking

**56 partial problems**  
including 3 time steps



**3 out of 8** storage  
constraints linking

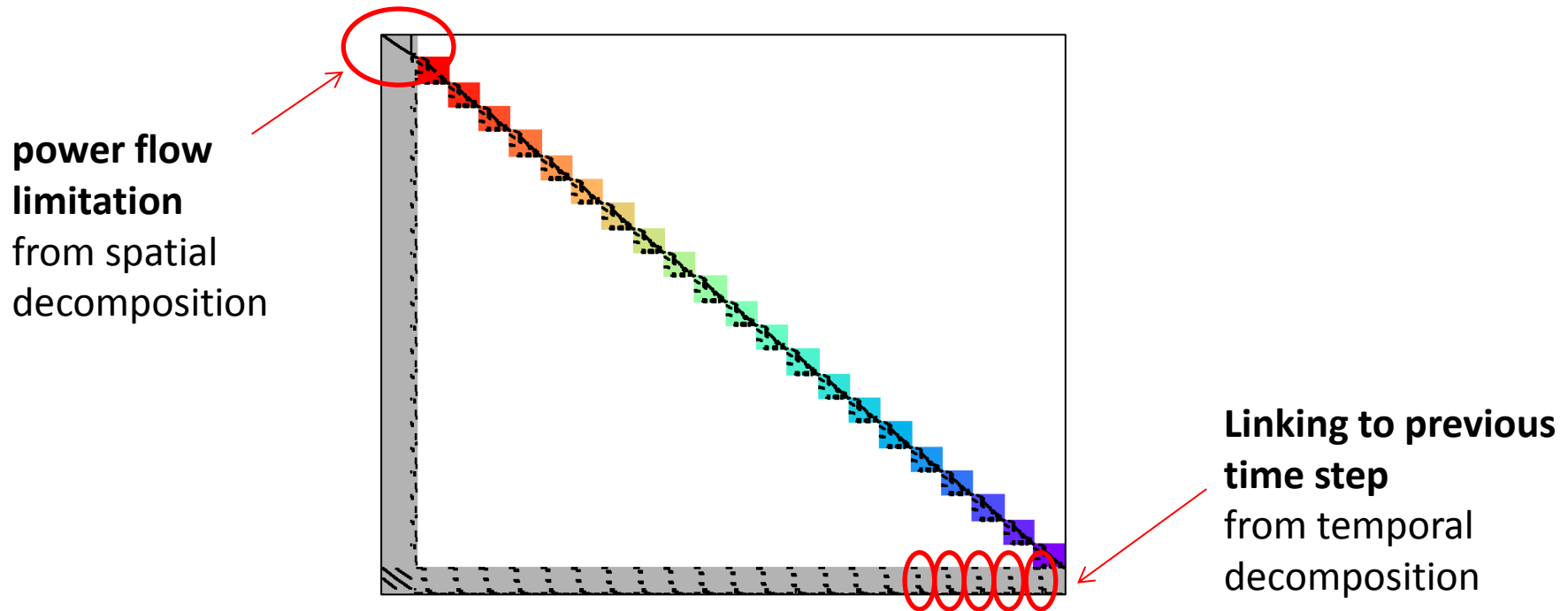
**168 partial problems**  
including 1 time step



**Every** storage  
constraint linking

Target: Find good **trade-off** between **number of time blocks** and  
**number of linking constraints**

Decomposition by **time and region** can be applied at the same time



All previously shown annotation plots describe exactly the **same ESM problem**  
→ **Systematic evaluation** of promising annotations required

➔ TB-02-4: T. Breuer „*High Performance Computing for Energy System Modelling*“

- Application of high performance computing requires substantial preparation  
→ identification of block structures, linking variables, linking constraints
- Systematic evaluations necessary to determine best decomposition strategies
- Strategies promising for REMix will be tested in other models as well
- Results to be summarized in a best-practice guide for energy system modelling

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DLR – German Aerospace Center

Institute of Engineering Thermodynamics

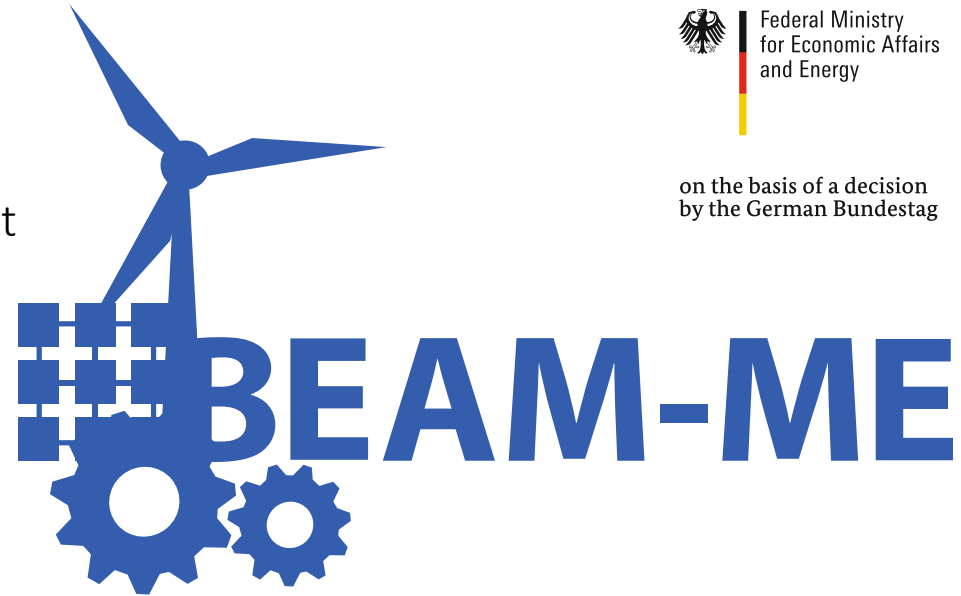
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